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1 **Numerical Study of Flow Characteristics**

2 **Around a 30° Yawed Circular Cylinder at $Re = 10^4$**

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Abstract

Unstable motions of bridge stay cables have been observed on site and in wind tunnel tests when a cable is yawed at certain orientations to wind. To uncover the underlying mechanisms, flow around a circular cylinder at a yaw angle of 30° has been numerically analyzed in the current study using delayed detached eddy simulation (DDES) at $Re = 10^4$. A comparison with the reference normal flow case indicates the presence of a more coherent span-wise flow structure when the cylinder is yawed at 30°. The application of Proper Orthogonal Decomposition (POD) further reveals that at this orientation, a synchronized flow structure exists which is characterized by continuous anti-symmetric pressure blocks. In addition, a low frequency flow fluctuation has been identified, the Strouhal number of which is roughly a quarter of that of the conventional Kármán vortex shedding. The pivotal role of axial flow in the intermittent amplification of cylinder sectional lift and the subsequent span-wise propagation of this enhanced local lift event has been revealed. The former is evident from the low frequency sectional lift peaks occurred during vortex shedding, whereas the propagation speed associated with the latter is in good agreement with the span-wise component of the incoming flow speed. The temporal and spatial impact of axial flow on the surrounding flow structure of the cylinder may serve as a periodic excitation source, which could trigger an unstable response of a cylinder. This, in the context of bridge stay cables, could possibly contribute to the onset mechanism of dry cable galloping.

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9 INTRODUCTION

10 Due to low inherent damping, low lateral stiffness, and small mass, stay cables on
 11 cable-stayed bridges are prompt to wind excitation. Because of that, considerable amount
 12 of research effort has been made to understand the aerodynamics of stay cables. Ma-
 13 jority of the existing analytical^{1,2}, experimental³⁻⁵ and numerical⁶ studies assumed stay
 14 cable as a smooth circular cylinder. In real life, however, stay cables are neither circular
 15 nor smooth. Furthermore, atmospheric wind tends to form a highly three-dimensional
 16 flow field around a stay cable, rendering unique aerodynamic forces depending on fac-
 17 tors such as wind-cable orientation. Recently, a type of stay cable vibration characterized
 18 by low frequency and large amplitude has received special attention from the engineer-
 19 ing community due to its potential threat to the safety of cable-stayed bridges. Among
 20 others, Saito *et al.*⁷ conducted a dynamic test on a full-size stay cable model in a wind
 21 tunnel experiment. In a testing case where the cable was yawed at 45° and $Re = 7 \times 10^4$,
 22 the vibration amplitude of the inclined cable was tended to diverge. The relative angle
 23 between the cable axis and the oncoming flow is often used to describe the orientation of
 24 a stay cable. This angle is often referred to as the yaw angle or the angle of attack in litera-
 25 ture, which is presumed to be a key factor in triggering unstable cable motion. Moreover,
 26 the unstable cable motion appeared to be difficult to restrain when wind speed exceeded
 27 a certain threshold. What is concerning is that the results from this study implied that
 28 majority of the existing stay cables on site would easily satisfy the identified critical con-
 29 dition and exhibit excessive oscillations. Though this new type of cable aerodynamic
 30 instability phenomenon has been studied for more than two decades, a consensus on its
 31 mechanism has yet to be reached.

32 Bursnall and Loftin⁸ studied flow-induced surface pressure distribution of a circular
 33 cylinder over a yaw angle range of 0° to 60° , from the sub-critical Reynolds number
 34 range up to about 5.0×10^5 . The observed pressure distribution on the cylinder surface
 35 showed some variations along its axial direction in the sub-critical Reynolds number
 36 range, indicating the presence of a highly three-dimensional flow structure. Further, it
 37 was noticed that this kind of surface pressure variation existed even in the normal flow
 38 case. They emphasized the importance of the axial flow effect on the cylinder surface
 39 pressure distribution.

40 King⁹ experimentally visualized the flow pattern surrounding a stationary and an
 41 oscillating yawed circular cylinder for $2000 < Re < 20000$ in flowing water. They
 42 pointed out that yawing a cylinder would not necessarily protect the cylinder from
 43 vortex-excitation, but could enhance cylinder vibration at certain yaw angle positions.
 44 Zhou *et al.*¹⁰ studied the fluid-structure interaction in the intermediate wake of a sta-
 45 tionary circular cylinder. Based on the phase-averaging technique, they concluded that
 46 the three dimensionality of the wake was enhanced significantly by the span-wise flow.
 47 They found that the peak regions of the span-wise vorticity spectra were enlarged but the
 48 peak value of the energy was reduced, indicating a dispersion of the vortex shedding. It
 49 is worth noting that although the results obtained by Zhou *et al.*¹⁰ indicated that vortex
 50 shedding was mitigated when the yaw angle was increased to 45° , King⁹ reported that
 51 the vortex-induced vibration of an oscillating cylinder was enhanced at the same yaw
 52 angle. Chiba and Horikawa¹¹ calculated the viscoelastic fluid field around an inclined
 53 circular cylinder. They found that the fluid was prone to move axially in the vicinity of
 54 the cylinder and then gradually return to the direction of the oncoming flow.

55 Kawamura and Hayashi¹² computed incompressible three-dimensional flow around a
 56 finite and an infinite circular cylinder at a 30° yaw angle without considering turbulence
 57 effect when the Reynolds number was 2000. Axial flow was found to propagate down-
 58 stream to the wake along the cylinder axis. Marshall¹³ applied a quasi-two-dimensional
 59 approximation to study the wake dynamics of a yawed cylinder. The axial flow in the
 60 near wake of a yawed cylinder was found to have a speed 20% to 30% lower than that
 61 of the free-stream axial flow. They suspected that this axial velocity deficit within the
 62 downstream vortex cores might lead to instability of the vortex street. Zhao *et al.*¹⁴ stud-
 63 ied flow past a stationary yawed circular cylinder within a yaw angle range of 0° to 60° at
 64 $Re = 1000$ using direct numerical simulation. They observed that the span-wise vortices
 65 were parallel to the cylinder axis. Bourguet and Triantafyllou¹⁵ calculated the response
 66 of a flexible cylinder inclined at 80° when $Re = 500$ by means of direct numerical sim-
 67 ulation. They observed that in the absence of vibration, the wake behind the circular
 68 cylinder showed an oblique shedding mode.

69 The above studies showed that the relative angle between the oncoming flow and
 70 the cylinder axis had a decisive impact on the aerodynamic instability of a cylinder. In
 71 particular, a cylinder under certain angle of attack was found more prone to be excited
 72 and eventually develop into large amplitude unstable motion. For example, divergent
 73 response of a circular cylinder with an attack angle of 30° was observed in a wind tunnel
 74 study by Saito *et al.*⁷ at $Re = 7 \times 10^4$. In another wind tunnel experiment by Cheng *et*
 75 *al.*³, a cable segment model, when oriented with a relative angle of 30° between the cable
 76 axis and the oncoming flow, exhibited unstable galloping-like motion at $Re = 3.3 \times 10^5$.
 77 By conducting computational fluid dynamics (CFD) simulations at $Re = 10^4$, Wang *et*
 78 *al.*¹⁶ identified a low-frequency but large amplitude sectional lift force at an attack angle
 79 of 30°. Yeo and Jones¹⁷ investigated the 3D characteristic of flow around a yawed and
 80 inclined circular cylinder using detached eddy simulation (DES) at a Reynolds number of
 81 1.4×10^5 . They observed a coherent swirling flow structure developed from the separated
 82 shear layer. A unique moving peak of force, with a frequency lower than that of the
 83 conventional von Kármán vortex shedding, was generated as a result of the movement
 84 of these swirling flow structures at an attack angle of 22.2°. Due to the inherent three-
 85 dimensional characteristics of flow around a circular cylinder, locating the source of the
 86 low frequency force is arduous. A satisfactory explanation of how an attack angle would
 87 affect the aerodynamic response of a cylinder has yet to be reached.

88 CFD simulations provide abundant information related to the flow under investiga-
 89 tion, including the ability to extract key characteristics from a statistical perspective. This
 90 method not only identifies coherent structures in the simulated flow but also serves as
 91 the foundation for constructing reduced-order models. The current study uses delayed
 92 detached eddy simulation (DDES) in Open-source Field Operation And Manipulation
 93 (OpenFOAM) to investigate the flow past a circular cylinder with a yaw angle of 30° at a
 94 Reynolds number of 10^4 . Proper Orthogonal Decomposition (POD) analysis¹⁸⁻²⁰ is con-
 95 ducted for the surrounding flow to reveal the spatial and temporal flow characteristics.
 96 A normal flow case is also studied and used as a reference. The outcomes of the current
 97 study are expected to offer a deeper insight into the impact of cylinder orientation on the
 98 surrounding flow feature, helping to clarify mechanisms associated with wind-induced
 99 cable vibrations and contribute to the fundamentals of bluff body aerodynamics.

100 NUMERICAL ASPECTS

101 An O-type of grid is adopted in the current study. The computational grid has a cylin-
 102 drical geometry. As shown in Fig. 1 (a), the cylinder is located at the centre of the com-
 103 putational domain, whose diameter and length are, respectively, $40D$ and $20D$, where
 104 D is the cylinder diameter. A Cartesian coordinate system is used such that the x -axis
 105 represents the stream-wise direction, the z -axis coincides with the cylinder axis, and the
 106 y -axis is perpendicular to both the x -axis and the z -axis. Fig. 1 (b) shows the definition of
 107 attack angle α . When $\alpha = 0^\circ$, it represents the normal flow condition. A total number of
 108 4141200 hexahedral cells were used.

109 The following boundary conditions were used in the current study: a) At the inlet
 110 plane, a turbulent inlet was adopted, of which the corresponding turbulence intensity
 111 was around 1%; b) At the outlet plane, the pressure was assumed to be zero; c) On the
 112 cylinder surface, a no-slip boundary was applied for the velocity; and d) On the span-
 113 wise walls, the periodic boundary conditions were applied to minimize the end effect.

114 Detached eddy simulation (DES) is a hybrid model of Reynolds-averaged Navier-
 115 Stokes equation (RANS) and large eddy simulation (LES). DES assumes a destruction
 116 term and a production term such that it can adjust the eddy viscosity according to the
 117 relation between the distance to the closest wall and the size of the grid²¹. However, DES
 118 suffers from an artificial grid-induced separation if the switch mechanism from RANS to
 119 LES does not accurately reflect the flow properties within this transition region²². Due to
 120 this shortcoming, the delayed detached eddy simulation (DDES) was proposed to mit-
 121 igate the weakness of the original DES²³. Central to the DDES methodology is a set of
 122 equations that govern the transition from RANS to LES modes. The transition criterion
 123 is defined by the variable r_d :

$$r_d \equiv \frac{\nu_t + \nu}{\sqrt{U_{i,j}U_{i,j}}\kappa^2 d^2} \quad (1)$$

124 Here, ν_t is the kinematic eddy viscosity, ν is the molecular viscosity, $U_{i,j}$ is the velocity
 125 gradients, κ is the von Kármán constant, and d is the distance to the nearest wall. Based
 126 on this criterion, the DDES shielding function f_d is formulated as:

$$f_d \equiv 1 - \tanh\left([8r_d]^3\right) \quad (2)$$

127 This function ensures a smooth transition between RANS and LES modes, preventing
 128 premature activation of LES in regions of attached boundary layers. It modifies the effec-
 129 tive wall distance used in DES, enhancing the model's performance in areas with strong
 130 adverse pressure gradients. Lastly, a modified effective wall distance parameter d_{DDES} is
 131 introduced as:

$$d_{DDES} \equiv d - f_d \max(0, d - C_{DES}\Delta) \quad (3)$$

132 Here, C_{DES} is the DES constant and Δ is the grid spacing. These equations collectively
 133 constitute the mathematical foundation of the DDES method, enabling it to accurately
 134 capture a broad spectrum of turbulent flow regimes while maintaining computational
 135 efficiency.

136 The current study applies DDES with the finite volume method implemented in
 137 OpenFOAM²⁴ (version 4.1). The backward scheme was chosen for the time integra-
 138 tion. The Pressure Implicit with Splitting of Operators algorithm was chosen to solve the
 139 discretized Navier-Stokes equations. At each time step, there were three loops to update

140 the pressure field after the momentum equations were solved using the pressure from
 141 the previous time step. The convergence criteria for solving the velocity and the pressure
 142 field were set to be 10^{-6} and 10^{-7} , respectively.

143 The numerical model was validated in terms of the mean drag coefficient and Strouhal
 144 number of a normal flow cylinder at $Re = 10^4$. The mean drag coefficient obtained from
 145 the current numerical model, observed to be 1.14, aligns reasonably well with the wall-
 146 resolved LES by Cheng et al.²⁵, which yielded $\overline{C_D} = 1.08$ at $Re = 10^4$. The Strouhal
 147 number, another critical validation metric, is also in line with the existing experimental
 148 data. Our numerical model produced a Strouhal number of $St = 0.20$ at the sub-critical
 149 Reynolds number of 10^4 . This result exhibits close agreement with the experimental work
 150 of Roshko²⁶, which reported $St = 0.21$. Further, we observed in our analysis that the
 151 surface pressure distribution around the circular cylinder corresponded well with the
 152 experimental data presented by Norberg²⁷, as depicted in Fig. 2 by red dots. These results
 153 confirm the validity of our numerical model. The computational domain was established
 154 with a span-wise length of 20D. Details on the grid configuration can be found in Table
 155 I. Our previous studies show that the numerical solution was grid-independent with the
 156 current setups. For a deeper exploration of the validation process, please refer to our
 157 study²⁸. Given that the normal flow scenario of the circular cylinder yields satisfactory
 158 results which are comparable with the existing experimental data and also manifest grid-
 159 independence, it validates the sufficiency of our numerical model, the meshing strategy,
 160 and the selected grid size for the simulation.

161 The fluctuating pressure $p'(x, t)$ is a function of the sampling location and time. POD
 162 can be used to approximate the original fluctuating pressure field using a spatial function
 163 $\Phi_k(\mathbf{x})$ multiplied by time coefficients $a_k(t)$ such that:

$$p'(\mathbf{x}, t) = \sum_{k=1}^{\infty} a_k(t) \Phi_k(\mathbf{x}), \quad (4)$$

164 where $\Phi_k(\mathbf{x})$ ($k = 1, 2, \dots, \infty$) are the POD modes and $a_k(t)$ are the corresponding time
 165 coefficients.

166 Because it is challenging to prescribe physical meaning to higher order modes²⁹,
 167 the current study considered only the first six POD modes. According to Tamura and
 168 Suganuma³⁰, considering the mean value component in POD analysis of pressure field
 169 would be detrimental and could lead to a physical invalidity. Thus, the current POD
 170 analysis excluded the mean value component and focuses on the fluctuating compo-
 171 nents. A non-dimensional time is defined as $t^* \equiv tU_{\infty}/D$, where t is the dimensional
 172 time, U_{∞} is the free-stream velocity, and D is the diameter of the cylinder. The number of
 173 time steps for POD analysis is chosen to be 1200, corresponding to 120 non-dimensional
 174 time duration. The reasons for choosing this time step are justified in the Appendix.

175 RESULTS AND DISCUSSION

176 To find out why the unstable aerodynamic behaviour of a circular cylinder is prone to
 177 occur at a yaw angle of 30° , flow structure surrounding a cylinder at this orientation will
 178 be explored in depth in this section by applying POD to the cylinder surface pressure
 179 and the transverse velocity of the flow in the near and far wake. In addition, the near
 180 wake vortical structures, the axial flow and the flow-induced forces will be scrutinized in

181 detail. The normal flow case ($\alpha = 0^\circ$) will be used as a reference to reveal the impact of
 182 cylinder orientation on the surrounding flow and manifest the unique flow structure at
 183 an attack angle of 30° .

184 Surface pressure

185 *Yawed cylinder case* ($\alpha = 30^\circ$)

186 Figure 3 shows the first six POD modes for the surface pressure in a yawed cylinder
 187 case at $\alpha = 30^\circ$. A total number of 1200 snapshots of the instantaneous surface pres-
 188 sure data, all subtracted by the time-average surface pressure field, are used to conduct
 189 the POD analysis. The surface pressure POD modes are obtained by applying the single
 190 value decomposition to the time history of the fluctuating component of the surface pres-
 191 sure data. In each subplot, the horizontal axis represents the circumferential direction,
 192 θ . The stagnation point is located at $\theta = 180^\circ$ or $\theta = -180^\circ$. The base point is located
 193 at $\theta = 0^\circ$. The vertical axis defines the dimensionless span-wise location. The pressure
 194 coefficient at each location is contoured and mapped by its magnitude. In general, the
 195 pressure modes show more variations in the region between $\theta = -130^\circ$ and $\theta = 130^\circ$,
 196 which corresponds to the wake region. The variations are largely driven by the alternat-
 197 ing von Kármán vortex shedding that leads to periodic changes in the surface pressure
 198 distribution.

199 Modes 1 and 2 show an anti-symmetric pattern about the baseline $\theta = 0^\circ$, which is re-
 200 lated to von Kármán vortex shedding. The pressure/suction blocks in these two modes
 201 are observed to extend over the entire cylinder span. This means that localized von Kár-
 202 mán vortex shedding events are synchronized. While Mode 1 shows a very strong and
 203 well-coordinated von Kármán vortex shedding effect along the cylinder length, it is much
 204 weaker in Mode 2.

205 Modes 5 and 6 also exhibit an anti-symmetric pattern about the baseline, so they are re-
 206 lated to von Kármán vortex shedding as well. More alternating pressure/suction blocks,
 207 two blocks for Mode 5 and three blocks for Mode 6, can be seen along the cylinder span.
 208 This clearly indicates the three-dimensionality of flow field around a yawed cylinder.

209 Modes 3 and 4 show a symmetric pattern about the baseline where these pres-
 210 sure/suction blocks cover the range of $-140^\circ < \theta < 140^\circ$. In Mode 3, the upper and
 211 lower parts of the cylinder are in high suction, whereas the mid-portion is subjected to
 212 high pressure. In Mode 4, the symmetric pattern can still be observed in the suction
 213 block of the upper part for $10 < Z/D < 18$, whereas the pressure block on the lower
 214 part of the cylinder loses the symmetry. The physical significance of these two modes
 215 is much more difficult to determine²⁹, but it could be the averaged flow that leads to
 216 pressurization on the windward side and suction on the leeward side.

217 *Normal flow case* ($\alpha = 0^\circ$)

218 Figure 4 shows the first six POD modes for the surface pressure of the cylinder under
 219 the normal flow condition. Modes 1 and 2 show a clear anti-symmetric pattern about
 220 the baseline $\theta = 0^\circ$. Unlike the 30° yaw angle case, when $\theta = 0^\circ$, two pairs of pres-
 221 sure/suction blocks appear along the cylinder span in these two modes. The first pair is

222 seen to present in the top half of the cylinder, and the second pair in the bottom half with
 223 reversed sign. In addition, it is observed in Fig. 4 (a) that while strong pressure/suction
 224 exists in the upper part of the cylinder in Mode 1, they are much weaker in the lower
 225 half. Similar phenomenon can be seen in Fig. 4 (b) for Mode 2, except in this case, the
 226 upper part of the cylinder is subjected to weaker pressure/suction, and the lower half to
 227 stronger ones. Clearly, each pair of such pressure/suction blocks is associated with von
 228 Kármán vortex shedding, and the sign reversal between the upper and lower suggests
 229 that the formation and shedding of von Kármán vortices occur on the opposite sides and
 230 thus results in a three-dimensional flow field.

231 Modes 5 and 6 also exhibit an anti-symmetric pattern about the baseline $\theta = 0^\circ$. Com-
 232 pared to Modes 1 and 2, more pairs of alternating pressure/suction blocks are formed
 233 along the cylinder span for Mode 5 and 6, i.e. four pairs in Mode 5 and 3 pairs in Mode 6.
 234 This implies that numerous localized von Kármán vortex formation and shedding events
 235 with alternating shedding directions occurs along the cylinder span in these two modes
 236 which prompt the level of three-dimensionality in the surrounding flow.

237 Modes 3 and 4, however, show distinctively different mode shapes from the other
 238 modes. Both of them are symmetric about the baseline, so they are not related to von
 239 Kármán vortex shedding. In Mode 3, the upper ($15 < Z/D < 20$) and lower ($0 <$
 240 $Z/D < 8$) cylinder surface both show a high suction distribution over $-130^\circ < \theta <$
 241 130° , whereas the surface pressure in the cylinder mid-portion is nearly zero. In Mode
 242 4, though the top ($16 < Z/D < 20$) and lower ($0 < Z/D < 7$) cylinder surface is
 243 still subjected to high suction, the presence of strong surface pressure is found when
 244 $10 < Z/D < 16$. All these three pressure/suction blocks extend from $\theta = -130^\circ$ to
 245 $\theta = 130^\circ$. Again, these two modes might be the averaged flow that leads to pressurization
 246 on the windward side and suction on the leeward side.

247 Surrounding flow structure

248 *Near-wake vortical structures*

249 Figure 5 shows the instantaneous vortex structures using iso-surface contour of the
 250 second invariant, Q^{31} . The Q-criterion defines the vortex in an area where the vorticity
 251 magnitude is greater than the rate of strain. When $Q > 0$, it signifies there is a vortex. The
 252 presence of the primary and the secondary vortical structures can be clearly observed in
 253 Fig. 5. The former can be identified by the vortex tubes denoted by the red dash lines in
 254 the figure, whereas the latter appear as rib-like structures in between the primary vortical
 255 structures denoted by the green elliptical rings. These two types of vortical structures can
 256 be observed in both 30° and 0° cases.

257 As can be seen from the pattern of the red dash lines in Figs. 5 (a) and (b), the vortex
 258 tubes in both attack angle cases are parallel to each other. However, a noticeable differ-
 259 ence in the primary vortical structure is the shape of the vortex tubes along the cylinder
 260 axial direction. In the case of $\alpha = 30^\circ$, the vortex tubes are parallel to the cylinder axis.
 261 However, this is not the case when the cylinder is normal to the flow. Since these vortex
 262 tubes represent the von Kármán vortices, their shape would show the state of von Kár-
 263 mán vortex shedding process at different span-wise locations. In the case of $\alpha = 30^\circ$, the
 264 vortex formation and shedding are synchronized along the cylinder span. In the time
 265 instant shown in Fig. 5 (a), there are three vortex tubes. The vortex tube labelled as L1 is

266 resulted from the newest von Kármán vortex that is shed, whereas L2 and L3 are formed
 267 in the two previous von Kármán vortex shedding events. In the normal flow case, four
 268 vortex tubes are captured at the shown time instant, as can be seen in Fig. 5 (b). For the
 269 most recent von Kármán vortex shedding event denoted by L1, a time lag between the
 270 two local von Kármán vortex shedding events at span-wise locations A1 and A2 can be
 271 clearly observed in Fig. 5 (b). At A1, the vortex tube is closer to the cylinder leeward
 272 surface than that at A2. This means that the vortex formation and shedding at A1 occurs
 273 later than that at A2. Thus, at the time instant when von Kármán vortex shed at loca-
 274 tion A1, the vortex formation and shedding at location A2 occurs on the opposite side of
 275 the cylinder. In other words, the shape of the four vortex tubes in the normal flow case
 276 suggests that at a given time instant, von Kármán vortex shedding and formation in the
 277 upper and lower part of the cylinder occurs on the opposite side of the cylinder.

278 *POD of transverse velocity in wake region of $0.5 < x/D < 10$*

279 Figure 6 shows the iso-surfaces of transverse velocity POD modes for $\alpha = 30^\circ$ and
 280 $\alpha = 0^\circ$. These modes were computed from the transverse velocity with a magnitude of
 281 ± 1 m/s in the wake region where $0.5 < x/D < 10$. For each snapshot, the time-average
 282 transverse velocity field is subtracted. The The approach of obtaining the wake transverse
 283 velocity POD modes is similar to that for the pressure POD modes except that the former
 284 is in a three-dimensional space. The red contour corresponds to 1 m/s, whereas the blue
 285 color represents -1 m/s.

286 In the column of $\alpha = 30^\circ$ case in Fig. 6, all tube-like structures are parallel to each
 287 other and continuous over the entire cylinder span in Mode 1 and Mode 2, except the
 288 tubes in Mode 2 are advanced in the streamwise direction by roughly $1D$ compared to
 289 their respective counterparts in Mode 1. Modes 1 and 2 represent a well-coordinated von
 290 Kármán vortex shedding process along the entire cylinder span. Since POD modes give
 291 an averaged value of the transverse velocity, the shape of Mode 1 and Mode 2 physically
 292 means that at any specific time instant, the formation and shedding of von Kármán vor-
 293 tices along the cylinder always occur on the same side of the cylinder. This is consistent
 294 with the earlier discussion of the surface pressure POD results of the $\alpha = 30^\circ$ case shown
 295 in Fig. 3 (a), where Mode 1 shows a uniform distribution pattern of the surface pressure
 296 and suction along the cylinder span on two opposite sides of the cylinder, implying the
 297 synchronization of the local von Kármán vortex shedding events along the cylinder.

298 Modes 3, 4, 5 and 6 have a similar feature in that the tube structures are divided into
 299 two or three segments along the cylinder span, with a streamwise lag between two ad-
 300 jacent segments, indicating that the occurrence of von Kármán vortex shedding events
 301 on these two segments are on the opposite side of the cylinder. Therefore, these modes
 302 represent a strong 3D characteristic of the wake region. As discussed in Figs. 3 (e) and
 303 (f), the anti-symmetric pressure modes (Mode 5 and Mode 6) likewise show two or three
 304 pairs of reversed pressure/suction blocks along the cylinder spanwise direction.

305 For the normal flow case ($\alpha = 0^\circ$) shown in Fig. 6, the contour of the transverse
 306 velocity exhibits a tube-like structure in the wake. Modes 1 and 2 have the same spatial
 307 structure, except for a difference of roughly $1D$ in the tube position along the stream-
 308 wise direction. In these two modes, all tube-like structures are found to be parallel to
 309 each other. However, unlike Mode 1 and Mode 2 in the $\alpha = 30^\circ$ case, when $\alpha = 0^\circ$,
 310 the tubes are seen to be divided into two parts, with those in the lower half region being

311 advanced by approximately $4D$ in the streamwise direction. This indicates that the vortex
 312 formation and shedding events are not synchronized along the cylinder, but rather they
 313 occur on the opposite sides of the cylinder in the upper and lower portions. As discussed
 314 earlier, the POD analysis of the cylinder surface pressure shows that Mode 1 and Mode
 315 2 share similar spatial structures, as can be seen in Figs. 4 (a) and (b). These suggest that
 316 compared to the 30° yaw angle case, the coherence of von Kármán vortex shedding events
 317 along the cylinder axis exists in a much narrower region in the normal flow condition.

318 Each tube structure in Mode 3 is divided into three segments, covering a span-wise
 319 range of $14 < Z/D \leq 20$, $7 < Z/D \leq 14$, and $0 \leq Z/D \leq 7$, respectively. The top and
 320 the bottom tube segments are located roughly at the same streamwise position, whereas
 321 the middle segment is advanced by about $0.5D$, implying that at a specific time instant,
 322 the formation and shedding of von Kármán vortices occur on the same cylinder side at
 323 the top and bottom of the cylinder, whereas that in the middle part of the cylinder is not
 324 synchronized. Such an example can also be seen in Fig. 5 (b) where the vortex tube is
 325 farther away from the cylinder at A2 than that at A1. Mode 4 manifests the same spatial
 326 features as Mode 3. The main difference between these two modes is the sequence of the
 327 red and blue tubes in the stream-wise direction, which represents the presence of a phase
 328 shift between these two modes.

329 Modes 5 and 6 are similar to Modes 3 and 4, except some discontinuities in the tube
 330 structures at certain span-wise locations are observed. For example, in the zoom-in figure
 331 of Mode 5, a green circle highlights this kind of discontinuity which occurs at $z/D = 7$.
 332 In addition, Mode 6 shows a weaker von Kármán process in the upper wake region.
 333 Overall, Modes 3 to 6 in the normal flow case all represent the three-dimensional flow
 334 structures in the cylinder wake.

335 *POD of transverse velocity in near wake* ($0.5 < x/D < 1.5$)

336 The analysis of the transverse velocity in the near wake is a crucial element in under-
 337 standing the aerodynamic subtleties of a cylinder. Alterations in this velocity component
 338 can reveal key fluid flow attributes, particularly those that trigger instability and gener-
 339 ate large amplitude motions under specific conditions. These fluctuations can be linked
 340 directly to distinctive flow patterns and vortex structures, thereby enhancing our under-
 341 standing of the complex aerodynamics. Subsequent sections focus on a detailed POD
 342 analysis of this specific flow region, $0.5D$ to $1.5D$ away from the cylinder, when the cylin-
 343 der is at $\alpha = 30^\circ$.

344 The transverse velocity POD analysis results, as depicted in Fig. 7, show the mode
 345 shapes and time coefficients. The dominance of von Kármán vortex is evident from the
 346 Fast Fourier Transform (FFT) results in Fig. 7 (a). It's worth noting that the POD analysis
 347 is unable to completely isolate von Kármán vortex, but instead display it across almost all
 348 of the modes. Nevertheless, the FFT analysis on the POD time coefficients of modes 5 and
 349 6 show a noticeable difference in the pattern from that of the other four modes. Besides
 350 a peak at or in the vicinity of $St = 0.20$ which reflects the effect of von Kármán vortex
 351 shedding, a low frequency peak, slightly broad-banded and approximately centered at
 352 $St = 0.12$, is observed.

353 Figures 7 (b) to (d) display the shape of Mode 5, which consists of four blocks. Con-
 354 sidering the spatial distribution of this mode shape is repetitive in the z -direction, and
 355 factoring in the fluctuating nature of the time coefficient, it appears that a coherent struc-

356 ture is propagating in the z-direction. This information allows for the calculation of the
 357 propagation speed. On average, the length of each block is 0.45 m. The FFT results from
 358 Mode 5, as shown in Fig. 7 (a), indicate a slightly broad-banded frequency centered at
 359 $St = 0.1156$. With a normal velocity of 1.44 m/s and a cable diameter of 0.09 m, this cal-
 360 culation yields a dimensional frequency of $f = St \times U/D = 1.85$ Hz, which corresponds
 361 to a time period of 0.54 seconds. This leads to an observed propagation velocity of 0.83
 362 m/s along the cylinder's span. It is important to note that under conditions of $Re = 10^4$
 363 and $\alpha = 30^\circ$ for a circular object with a diameter of 0.09 m, the axial component of the
 364 free-stream velocity is determined to be 0.83 m/s, implying that the span-wise propaga-
 365 tion of the observed coherent structure is highly associated with the axial flow formed on
 366 the leeward side of the cylinder.

367 *Sectional resultant forces and wake*

368 To further explore the flow structure associated with $\alpha = 30^\circ$ and $\alpha = 0^\circ$ cases, the
 369 shear layers at six different span-wise locations of $1.11D$, $4.44D$, $7.78D$, $11.11D$, $14.44D$,
 370 and $17.78D$ are portrayed in Fig. 8 for five representative time instants within one von
 371 Kármán vortex shedding period. These sections are denoted by a , b , c , d , e and f for refer-
 372 encing purpose. The shear layers in the figure are contoured using the vorticity compo-
 373 nent perpendicular to the selected section. In addition, the associated sectional resultant
 374 forces are also shown in these plots in blue. They are calculated from the integration of
 375 the surface pressure. The resultant forces are scaled by a factor of 5 for better visibility.
 376 For referencing purpose, a stream-wise center plane is defined by the cylinder axis and
 377 the stagnation point, which is shown as grey rectangles in Fig. 8, assuming readers face
 378 the stream-wise direction.

379 For the 30° attack angle case, at each of the five selected time instants, the sectional
 380 resultant forces at all six span-wise locations are found to point more or less toward the
 381 same direction, especially at $T^* = 674.74$, 679.54 , and 680.54 , implying that at a yaw angle
 382 of 30° , the resultant flow-induced force at different span-wise locations would "push" the
 383 cylinder towards the same direction, which would potentially lead to a large amplitude
 384 cylinder motion. On the other hand, the synchronization of sectional resultant forces is
 385 only observed over part of the cylinder in the normal flow case, i.e., the effect of the
 386 sectional resultant forces on different portions of the cylinder is partially cancelled out.
 387 Thus, the overall impact of the flow-induced forces on a normal flow cylinder is much
 388 less significant as compared to the 30° attack angle case.

389 *Effect of axial flow*

390 The orientation of a yawed cylinder renders the formation of a secondary flow struc-
 391 ture along its span, which could have a sizable impact on the neighboring flow and the
 392 cylinder response. In this section, the influence of axial flow on the temporal and spatial
 393 variation of cylinder sectional lift will be examined. 3D flow visualization techniques will
 394 be used to acquire a better understanding of the flow characteristics in the near wake.

395 *Impact on Temporal Variation of Sectional Lift* To gain insights into the temporal varia-
 396 tion of the sectional lift along the cylinder span, the sectional lift coefficient (C_L) at 100
 397 equally-spaced span-wise locations are analyzed. Figure 9 (a) portrays a sample lift co-

398 efficient of Section 60 ($z = 12D$), the periodic variation of which is attributed to the
399 shedding of von Kármán vortices. Besides, the existence of a low-frequency variation of
400 C_L is also observed in Fig. 9 (a), such that the sectional lift is enhanced once ever few von
401 Kármán vortex shedding cycles. A red envelope curve for C_L time history is added in
402 Fig. 9 (a) to better encapsulate this kind of low frequency variation.

403 These observed features are further confirmed by the FFT analysis results, which re-
404 vealed the presence of two dominant peaks in the frequency domain. The first peak oc-
405 curs at a Strouhal number (St) of 0.20 and is associated with the frequency of von Kármán
406 vortex shedding. The second peak is slightly broad-banded and centered near $St = 0.05$,
407 reflecting the low-frequency variation observed in the C_L time history plot. It is worth
408 noting that the POD analysis of transverse velocity in the cylinder near wake reveals the
409 existence of secondary axial flow characterized by approximately $St = 0.05$, as shown
410 in Fig. in 7 (a) for mode 5 and mode 6. The matching low-frequency component in the
411 transverse velocity of the near wake and the intermittent amplification of sectional lift
412 suggest that the secondary axial flow could be the cause of the intermittent enhancement
413 of C_L . The sectional lift time history and the corresponding FFT analysis results have
414 been examined for the rest 99 span-wise sections. The same two dominant peaks in C_L
415 have been identified. The consistency of the results support our understanding of the
416 role of axial flow in affecting temporal variation of cylinder sectional lift.

417 *Impact on Spatial Variation of Sectional Lift* To examine the spatial variation of sec-
418 tional lift, the C_L time history at Sections 43, 50, 68, 70, and 78, spanning from $8.6D$
419 to $15.6D$ along axial direction of the cylinder, are presented together in Fig. 10 for com-
420 parison. In the figure, the intermittent amplification events of sectional lift, encapsulated
421 by C_L envelopes, are marked with black elliptical rings. These events are observed to
422 propagate along the span of the cylinder. Three such propagation events have been iden-
423 tified within the timeframe shown in Fig. 10. They are designated by the purple, green,
424 and blue lines, respectively.

425 Events T_f and T_g on the blue line are used as an example to illustrate how the propaga-
426 tion speed of these lift amplification events was calculated. The distance between Section
427 43 and 50 is 0.112m. The time lag between events T_f at Section 43 to event T_g at Section
428 50 is 0.14s. The propagation speed is then calculated as $0.112 \text{ m}/0.14 \text{ s} = 0.80 \text{ m/s}$. The
429 same calculation was extended to all nine identified lift amplification events identified
430 in Fig. 10. The average propagation speed was found to be 0.80 m/s and listed in Table
431 II, which is very close to the axial component of the free-stream velocity, 0.83 m/s. This
432 consistency implies that the span-wise propagation of the amplified sectional lift event
433 is also caused by the effect of axial flow.

434 The above observations of the temporal and spatial varying characteristics of cylinder
435 sectional lift reveal the pivotal role of the secondary axial flow in causing the intermittent
436 amplification of sectional lift and their propagation along the cylinder span, both resulted
437 from the interaction between von Kármán vortex and axial flow.

438 *Visualization of Flow Characteristics* Flow visualization is an integral technique for in-
439 terpreting complex flow fields. In this study, a stream-trace visualization technique is
440 utilized to gain deeper insight into the flow characteristics in the near wake. Figure 11
441 illustrates the flow around a circular cylinder at $\alpha = 30^\circ$ and $\alpha = 0^\circ$. Two types of
442 stream-traces, red and black, are used. The red stream-traces, originating from the inlet
443 boundary, assist in capturing the primary flow features, while the black stream-traces,
444 stemming from the cylinder surface, trace the flow close to the cylinder leeward surface,

445 providing insights into the secondary axial flow dynamics.

446 As shown in Fig. 11, upon reaching and passing the cylinder at any given span-wise
447 location, a fraction of the flow is entrapped in the recirculation zone, which subsequently
448 treaded along the cylinder. The aggregation of such entrapped flow across all span-wise
449 locations gives rise to what is often termed as the "axial flow" in literature⁴. The axial
450 flow exerts a "pushing" influence on flow close to the leeward side of the cylinder surface
451 and those near wake, causing them to move along the cylinder span.

452 However, the axial flow is not stable and will "escape" from the recirculation zone via
453 periodic axial vortex formation and shedding into the wake. The formation and shedding
454 of axial vortices have an impact on the existing flow structure, including the conventional
455 von Kármán vortices. If the formation and shedding of axial vortex occurs concurrently
456 with von Kármán vortex an enlarged von Kármán vortex would be formed and shed,
457 leading to an amplification of sectional lift.

458 Figure 12 demonstrates the interaction between the axial and von Kármán vortices.
459 Massless particles are injected into the near wake and tracked by a red tube. Section 72
460 ($z/D = 14.44$) and Section 83 ($z/D = 16.67$) are selected to illustrate the surrounding
461 flow structure. The contour represents the vorticity magnitude perpendicular to the free-
462 stream velocity. At time $t^* = 754.96$, as shown in Fig. 12 (a), the particle is moving in
463 the region close to Section 72. At the red region, marked by a black arrow Va , a vortex
464 is forming. Moving to the time instance $t^* = 757.77$, as depicted in Fig. 12 (b), the
465 massless particle is moving towards Section 83. Simultaneously, a relatively large vortical
466 structure, marked by a black arrow Vb , begins to emerge, creating a low-pressure zone,
467 which draws the particle toward. When the axial flow moves into the core of the von
468 Kármán vortex and interacts with it, it creates a significantly larger vortex. This particle
469 is eventually shed into the far wake, indicated by the time instance $t^* = 759.77$ as shown
470 in Fig. 12 (c).

471 Given the frequency of axial vortex formation and shedding is a fraction of the von
472 Kármán vortex frequency, the sectional lift is amplified intermittently. Under the cur-
473 rent simulation conditions, the axial vortex sheds approximately once every four von
474 Kármán vortex sheddings, as illustrated with the help of Fig. 9 (b). This intermittent am-
475 plification of sectional lift, if persists and occurs at different span-wise locations, could
476 possibly become an excitation source to trigger unstable cylinder response. This, in the
477 context of bridge stay cables, could potentially contribute to the onsite mechanism of a
478 dry cable galloping. In a recent wind tunnel study³², the dynamic response of stay cable
479 in dry condition was examined. Results showed that at lower wind speeds, von Kármán
480 vortices were mainly linked to minor vibrations. As wind speed increased, the impact of
481 von Kármán vortices decreased, whereas low-frequency vortices became more prevalent,
482 thereby enhancing the cable vibrations. The current findings regarding the mingling of
483 axial flow with von Kármán vortices, leading to the shedding of larger, as presumably
484 stronger, vortices shedding at lower than von Kármán frequency, offer an intriguing av-
485 enue for further exploration and validation in future research.

486 CONCLUSION

487 Flow around a circular cylinder yawed at 30° has been numerically studied by con-
488 ducting delayed detached eddy simulation and compared with that around a normal
489 flow cylinder. POD analysis has been performed to the cylinder surface pressure and

490 wake flow transverse velocity. The near wake vortical structures have been identified
 491 using instantaneous iso-surface contour of Q . In addition, the stream-trace flow visual-
 492 ization technique has been applied to assist in revealing flow characteristics in the near
 493 wake. The axial flow, which is a secondary flow formed by the entrapped flow in the
 494 recirculation zone, has been extensively analyzed in this study. The unique features of
 495 the flow around a cylinder yawed at $\alpha = 30^\circ$ have been scrutinized. The main findings
 496 of the current study are summarized as follows:

- 497 • A low-frequency flow structure in a cylinder oriented at a yawed angle of 30° has
 498 been identified. This structure, with a slightly broad-banded frequency range centered
 499 around $St = 0.05$, differs from classical von Kármán vortex shedding patterns. Confirmation
 500 of the existence of this structure through Proper Orthogonal Decomposition (POD), time history of sectional lift, and stream-trace visualization deepens
 501 our understanding of the complex flow dynamics involved.
 502
- 503 • The presence of axial flow has been captured on the leeward side of a cylinder
 504 when it is yawed at 30° . This disturbs the local von Kármán vortex structures and
 505 tends to "correct" the direction of the sectional resultant forces along the cylinder
 506 span, aligning them more or less towards the same direction. This could generate
 507 a greater overall effect to displace the cylinder from its neutral position. Such a
 508 harmony in the direction of sectional resultant forces is not observed in a normal
 509 flow cylinder without axial flow.
- 510 • For a cylinder yawed at 30° , it was observed that the axial flow tends to enhance
 511 the local lift and propagate this amplified event along the span, leading to an inter-
 512 mittent amplification of sectional lift. This could impose a periodical low frequency
 513 excitation on the cylinder, which, if sufficiently significant, could eventually lead
 514 to large amplitude unstable motion of the cylinder. This mechanism is believed to
 515 contribute to dry cable galloping of bridge stayed cables.
- 516 • Synchronized flow structures are observed at $\alpha = 30^\circ$. This is also characterized
 517 by the continuous anti-symmetric pressure blocks over the entire cylinder span as
 518 appeared in the surface pressure POD mode shapes, and the coordination of local
 519 von Kármán vortex shedding events along the cylinder span observed from the
 520 instantaneous iso-surface contour of Q . In contrast, such a flow structure coherence
 521 only exists within limited range along the cylinder span in the normal flow case.
- 522 • POD is capable of capturing the most cohesive spatial features in the flow around
 523 a cylinder. The POD mode shapes of the cylinder surface pressure show both anti-
 524 symmetric and symmetric patterns of pressure/suction blocks in the cylinder cir-
 525 cumferential direction, of which the former is associated with the von Kármán vor-
 526 tex shedding and the latter could be the averaged flow that leads to pressurization
 527 of the windward side and suction on the leeward side. Besides, the complex three-
 528 dimensional flow field surrounding a circular cylinder is evidenced by the pres-
 529 ence of multiple pressure/suction blocks along the cylinder span in the POD mode
 530 shapes.
- 531 • The temporal characteristics of the flow around a cylinder are captured by the POD
 532 mode shapes of the transverse velocity of the wake flow. Continuous tube struc-

533 tures in the first two modes of the 30° yawed cylinder represent the synchroniza-
 534 tion of local von Kármán vortex shedding along the span. The multi-segment tube
 535 structures observed in the remaining four modes of the 30° yawed cylinder and
 536 all six modes of the normal flow cylinder case suggest that there is a time lag in
 537 the shedding of local von Kármán vortices at different span-wise locations of the
 538 cylinder.

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543 AUTHOR DECLARATIONS

544 Conflict of Interest

545 The authors have no conflicts to disclose.

546 DATA AVAILABILITY

547 The data that support the findings of this study are available from the corresponding
 548 author upon reasonable request.

549 APPENDIX

550 Time sensitivity analysis

551 To ensure using the same time window in the analysis for the case $\alpha = 0^\circ$, a time
 552 sensitivity analysis was conducted. The number of time instants used in the study are
 553 1800, 1200 and 1000, respectively. The first six POD mode shapes of the cylinder surface
 554 pressure obtained by using these three different time sequences are contoured in Figs. 13,
 555 14, and 15, respectively. A comparison between these three sets of results showed that
 556 the patterns of the pressure POD mode shapes yielded from 1200 and 1800 time instants
 557 agree well. Therefore, the number of time instants used in the current study was chosen
 558 to be 1200.

559 POD script validation

560 To validate the POD script, the span-wise vorticity is processed with the current POD
 561 code. Figure 16 shows a comparison between the current results with those in a recently
 562 published study by Janocha *et al.*³³, both at $Re = 100$.

563 As can be seen in Fig. 16 (a), three types of mode shapes are captured in the current
 564 study. Mode 1 and Mode 2 show the largest block structure in the near wake. Mode 3 and

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⁵⁶⁵ Mode 4 show an anti-symmetric pattern of block structure about $y/D = 0$. The size of
⁵⁶⁶ blocks in Mode 5 and Mode 6 are much smaller and they are symmetric about $y/D = 0$.
⁵⁶⁷ All these distinctive patterns are in good agreement with the span-wise vorticity POD
⁵⁶⁸ analysis results by Janocha *et al.*³³.

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PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0172648

Accepted to Phys. Fluids 10.1063/5.0172648

569 REFERENCES

- 570 ¹A. Raeesi, S. Cheng, and D. S.-K. Ting, "A two-degree-of-freedom aeroelastic model for
571 the vibration of dry cylindrical body along unsteady air flow and its application to aero-
572 dynamic response of dry inclined cables," *Journal of Wind Engineering and Industrial*
573 *Aerodynamics* **130**, 108–124 (2014).
- 574 ²M. He and J. H. Macdonald, "An analytical solution for the galloping stability of a 3
575 degree-of-freedom system based on quasi-steady theory," *Journal of Fluids and Structures*
576 **60**, 23–36 (2016).
- 577 ³S. Cheng, G. L. Larose, M. G. Savage, H. Tanaka, and P. A. Irwin, "Experimental study
578 on the wind-induced vibration of a dry inclined cable-Part I: Phenomena," *Journal of*
579 *Wind Engineering and Industrial Aerodynamics* **96**, 2231–2253 (2008).
- 580 ⁴M. Matsumoto, T. Yagi, H. Hatsuda, T. Shima, M. Tanaka, and H. Naito, "Dry galloping
581 characteristics and its mechanism of inclined/yawed cables," *Journal of Wind Engi-
582 neering and Industrial Aerodynamics* **98**, 317–327 (2010).
- 583 ⁵W. Ma, Q. Liu, and M. Matsumoto, "Excitation of the large-amplitude vibrations of a
584 circular cylinder under normal wind conditions in the critical reynolds number range,"
585 *Journal of fluids and structures* **84**, 318–328 (2019).
- 586 ⁶D. Yeo and N. P. Jones, "A mechanism for large amplitude, wind-induced vibrations of
587 stay cables," in *Proceedings of the Eleventh Americas Conference on Wind Engineering, San*
588 *Juan, Puerto Rico* (2009).
- 589 ⁷T. Saito, M. Matsumoto, and M. Kitazawa, "Rain-wind excitation of cables on cable-
590 stayed Higashi-Kobe Bridge and cable vibration control," in *Proceedings of the Interna-
591 tional Conference on cable-stayed and suspension bridges (AFPC)*, Vol. 2 (1994) pp. 507–510.
- 592 ⁸W. J. Bursnall and L. K. Loftin, "Experimental investigation of the pressure distribu-
593 tion about a yawed circular cylinder in the critical Reynolds number range," *National*
594 *Aeronautics and Space Administration*, NACA-TN-24 (1951).
- 595 ⁹R. King, "Vortex excited oscillations of yawed circular cylinders," *Journal of Fluids En-
596 gineering* **99**, 495–501 (1977).
- 597 ¹⁰T. Zhou, H. Wang, S. F. Razali, Y. Zhou, and L. Cheng, "Three-dimensional vorticity
598 measurements in the wake of a yawed circular cylinder," *Physics of Fluids* **22**, 10–15
599 (2010).
- 600 ¹¹K. Chiba and A. Horikawa, "Numerical solution for the flow of viscoelastic fluids
601 around an inclined circular cylinder," *Rheologica Acta* **254**, 243–254 (1987).
- 602 ¹²T. Kawamura and T. Hayashi, "Computation of flow around a yawed circular cylinder,"
603 *JSME International Journal Series B Fluids and Thermal Engineering* **37**, 229–236 (1994).
- 604 ¹³J. S. Marshall, "Wake dynamics of a yawed cylinder," *Journal of Fluids Engineering*
605 **125**, 97–103 (2003).
- 606 ¹⁴M. Zhao, L. Cheng, and T. Zhou, "Direct numerical simulation of three-dimensional
607 flow past a yawed circular cylinder of infinite length," *Journal of Fluids and Structures*
608 **25**, 831–847 (2009).
- 609 ¹⁵R. Bourguet and M. S. Triantafyllou, "The onset of vortex-induced vibrations of a flexi-
610 ble cylinder at large inclination angle," *Journal of Fluid Mechanics* **809**, 111–134 (2016).
- 611 ¹⁶R. Wang, S. Cheng, and D. S.-K. Ting, "Effect of yaw angle on flow structure and cross-
612 flow force around a circular cylinder," *Physics of Fluids* **31**, 014107 (2019).
- 613 ¹⁷D. Yeo and N. P. Jones, "Investigation on 3-D characteristics of flow around a yawed and
614 inclined circular cylinder," *Journal of Wind Engineering and Industrial Aerodynamics*

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0172648

Accepted to Phys. Fluids 10.1063/5.0172648

- 615 **96**, 1947–1960 (2008).
- 616 ¹⁸Z. Feng and Q. Ye, “Turbulent boundary layer over porous media with wall-normal
617 permeability,” *Physics of Fluids* **35** (2023).
- 618 ¹⁹K. V. Pham, A. D. Le, C.-T. Dinh, *et al.*, “Frequency characteristics of axisymmetric conical
619 boattail models with different slant angles,” *Physics of Fluids* **35** (2023).
- 620 ²⁰H. Li, R. Peng, L. Hu, X. He, and A. Kareem, “On the surface flow patterns and associated
621 aerodynamics of an asymmetrical flat-box section,” *Physics of Fluids* **35** (2023).
- 622 ²¹P. R. Spalart, “Detached-eddy simulation,” *Annual review of fluid mechanics* **41**, 181–
623 202 (2009).
- 624 ²²F. R. Menter and M. Kuntz, “Adaptation of eddy-viscosity turbulence models to unsteady
625 separated flow behind vehicles,” in *The Aerodynamics of Heavy Vehicles: Trucks, Buses, and Trains*
626 *Buses, and Trains*, The Aerodynamics of Heavy Vehicles: Trucks, Buses, and Trains
627 (Springer Berlin Heidelberg, 2004) pp. 339–352.
- 628 ²³P. R. Spalart, S. Deck, M. L. Shur, K. D. Squires, M. K. Strelets, and A. Travin, “A new
629 version of detached-eddy simulation, resistant to ambiguous grid densities,” *Theoretical and computational fluid dynamics* **20**, 181 (2006).
- 630 ²⁴H. G. Weller, G. Tabor, H. Jasak, and C. Fureby, “A tensorial approach to computational
631 continuum mechanics using object-oriented techniques,” *Computers in Physics*
632 **12**, 620–631 (1998).
- 633 ²⁵W. Cheng, D. I. Pullin, R. Samtaney, W. Zhang, and W. Gao, “Large-eddy simulation of
634 flow over a cylinder with Re_D from 3.9×10^3 to 8.5×10^5 : a skin-friction perspective,”
635 *Journal of Fluid Mechanics* **820**, 121–158 (2017).
- 636 ²⁶A. Roshko, “On the development of turbulent wakes from vortex streets,” NACA Technical
637 Report 1191 (1954).
- 638 ²⁷C. Norberg, “Pressure forces on a circular cylinder in cross flow,” in *IUTAM Symposium on Bluff Body Wakes, Dynamics and Instabilities*, edited by H. Eckelmann, J. M. R. Graham, P. Huerre, and P. A. Monkewitz (Springer Berlin Heidelberg, Berlin, Heidelberg, 1993) pp. 275–278.
- 639 ²⁸R. Wang, S. Cheng, and D. S.-K. Ting, “Numerical study of roundness effect on flow
640 around a circular cylinder,” *Physics of Fluids* **32**, 044106 (2020).
- 641 ²⁹Q. Zhang, Y. Liu, and S. Wang, “The identification of coherent structures using proper
642 orthogonal decomposition and dynamic mode decomposition,” *Journal of Fluids and Structures* **49**, 53–72 (2014).
- 643 ³⁰Y. Tamura, H. Ueda, H. Kikuchi, K. Hibi, S. Suganuma, and B. Bienkiewicz, “Proper orthogonal
644 decomposition study of approach wind-building pressure correlation,” *Journal of Wind Engineering and Industrial Aerodynamics* **72**, 421–431 (1997).
- 645 ³¹J. C. R. Hunt, A. A. Wray, and P. Moin, “Eddies, streams, and convergence zones in
646 turbulent flows,” *Center for Turbulence Research, Proceedings of the Summer Program*
647 , 193–208 (1988).
- 648 ³²D. T. Nguyen and D. H. Vo, “Further explanation on the excitation mechanism of stay
649 cable vibration in dry conditions,” *Buildings* **13**, 1543 (2023).
- 650 ³³M. J. Janocha, G. Yin, and M. C. Ong, “Modal analysis of wake behind stationary and
651 vibrating cylinders,” *Journal of Offshore Mechanics and Arctic Engineering* **143**, 041902
652 (2021).
- 653 ³⁴A. Travin, M. Shur, M. Strelets, and P. Spalart, “Detached-eddy simulations past a circular
654 cylinder,” *Flow, Turbulence and Combustion* **63**, 293–313 (1999).
- 655 ³⁵P. D. Weidman, “Wake transition and blockage effects on cylinder base pressures,”
656
657
658
659
660
661

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PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0172648

Accepted to Phys. Fluids 10.1063/5.0172648

⁶⁶² Ph.D. thesis, California Institute of Technology (1968).

⁶⁶³ ³⁶S. Dong, G. E. Karniadakis, A. Ekmekci, and D. Rockwell, "A combined direct numerical simulation-particle image velocimetry study of the turbulent near wake," *Journal of Fluid Mechanics* **569**, 185–207 (2006).

⁶⁶⁴ ⁶⁶⁵ ⁶⁶⁶ ³⁷C. Norberg, "LDV-measurements in the near wake of a circular cylinder," ASME Paper
⁶⁶⁷ No. FEDSM98-521 (1998).

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

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668 TABLES

TABLE I. Mesh information and validation data.

Case	Re	L_z/D	N_r $(\Delta r^+)^a$	N_θ $(\Delta \theta^+)$	N_z (Δz^+)	$\overline{C_D}$	S_t	C'_L	$-C_p$	$ u_{\min} /U$	$\overline{L_B}/D$
Current	1.0×10^4	20	115 0.004	118 0.026	300 0.067	1.14	0.20	0.23	0.96	0.28	1.11
Cheng <i>et al.</i> ²⁵	1.0×10^4	3	384	384	96	1.08	1.20
Travin <i>et al.</i> ³⁴	5.0×10^4	2	118	105	30	1.05	0.22	0.21	0.98	...	1.3
Expt. Data	0.21 ^b	...	1.10 ^c	0.38 ^d	1.02 ^e

^a The dimensionless thickness of the near-wall mesh, $\Delta r^+ = d/D$, where d is the dimensional thickness and D is the diameter of the cylinder.

^b Ref.²⁶

^c Ref.³⁵

^d Ref.³⁶

^e Ref.³⁷

TABLE II. Calculation of the average axial flow interaction velocity shown in Fig. 8. Three events are captured, and they are indicated by purple, green, and blue lines. The amplified sectional C_l are being circled with elliptical rings.

Line	Color	# sections	t_{end} (s)	t_{start} (s)	dt (s)	velocity (m/s)
Line 1	Purple	8	38.376	38.214	0.162	0.790
Line 2	Green	10	39.472	39.273	0.199	0.804
Line 2	Green	18	39.786	39.472	0.314	0.917
Line 3	Blue	7	39.305	39.165	0.140	0.800
Line 3	Blue	18	40.477	40.066	0.411	0.701
Line 3	Blue	10	40.677	40.477	0.200	0.800
						(Avg.) 0.802

669 **FIGURE CAPTIONS**

FIG. 1. Schematic representation of the model: (a) sketch of full domain and (b) definition of attack angle α .

FIG. 2. Mean pressure distribution on cylinder surface at $Re = 10^4$ for the normal flow case (red rectangles are interpolated from Norberg's²⁷ experimental data). The red rectangles indicate the regions where our results closely align with Norberg's experimental data.

FIG. 3. The first six POD mode shapes for the surface pressure at $Re = 10^4$ and $\alpha = 30^\circ$: (a) Mode 1; (b) Mode 2; (c) Mode 3; (d) Mode 4; (e) Mode 5; and (f) Mode 6. Modes 1, 5, and 6 exhibit anti-symmetric distributions, which are closely related to von Kármán vortex shedding.

FIG. 4. The first six POD mode shapes for the surface pressure at $Re = 10^4$ and $\alpha = 0^\circ$: (a) Mode 1; (b) Mode 2; (c) Mode 3; (d) Mode 4; (e) Mode 5; and (f) Mode 6. Much like the $\alpha = 30^\circ$ case, anti-symmetric distribution emerges as the most dominant pattern.

FIG. 5. Instantaneous iso-surface of $Q = 50 \text{ s}^{-2}$ showing the near wake vortical structure at $Re = 10^4$: (a) $\alpha = 30^\circ$; and (b) $\alpha = 0^\circ$. The vortex tube in the $\alpha = 30^\circ$ scenario aligns more closely with the cylinder's centerline compared to the $\alpha = 0^\circ$ case.

FIG. 6. The first six POD mode shapes of transverse velocity in the cylinder wake region of $0.5 < x/D < 10$ in two cases: $\alpha = 30^\circ$; and $\alpha = 0^\circ$. Modes 1 and 2 show greater coherence along the cylinder's axis, suggesting more synchronized vortex shedding at $\alpha = 30^\circ$.

FIG. 7. POD analysis results on transverse velocity in the near wake region ($0.5 < x/D < 1.5$) of a cylinder at $\alpha = 30^\circ$ and $Re = 10^4$: (a) time coefficients and their respective FFT results; (b) mode shape of M5, perspective view; (c) mode shape of M5, side view; (d) mode shape of M5, leeward-side view. POD analysis identifies secondary flow features propagating along the cylinder's axis.

FIG. 8. Visualization of cylinder wake and sectional resultant forces at $\alpha = 0^\circ$ and 30° when $Re = 10^4$. In the $\alpha = 30^\circ$ case, vortex shedding is more coherent along the cylinder's axis, resulting in a stronger overall resultant force.

FIG. 9. Sectional lift coefficient at section 60 (a) time history and (b) corresponding FFT analysis result. A secondary flow pattern is observed, exhibiting a frequency much lower than that at which von Kármán vortex sheds.

FIG. 10. Time history of sectional C_l with corresponding envelopes at six span-wise locations ($z = 0.817$ m, 0.933 m, 1.100 m, 1.233 m, 1.267 m, 1.400 m) displayed from top to bottom. The enhanced local lift events are marked out by black elliptical rings. The span-wise propagation of enhanced sectional lift appears to be influenced by axial flow effects.

FIG. 11. Axial flow visualization at $Re = 10^4$ for the cases: (a) $\alpha = 30^\circ$ and (b) $\alpha = 0^\circ$. Axial flow tends to move along the center axis and interact with von Kármán vortices, a feature not observed in the normal flow case.

FIG. 12. Visualization of the interaction between axial and von Kármán vortices with a massless particle tracked by a red tube. Three time instances demonstrate the particles' movement through planes, and the evolving vortical structure, leading to a larger von Kármán vortex that eventually pulls the particle into the far wake.

FIG. 13. The first six POD mode shapes for the surface pressure at $Re = 10^4$ and $\alpha = 0^\circ$. The number of time sequence is 1800.

FIG. 14. The first six POD mode shapes for the surface pressure at $Re = 10^4$ and $\alpha = 0^\circ$. The number of time sequence is 1200.

FIG. 15. The first six POD mode shapes for the surface pressure at $Re = 10^4$ and $\alpha = 0^\circ$. The number of time sequence is 1000.

FIG. 16. A comparison of the mode shape for the span-wise vorticity at $Re = 100$: (a) current POD result (b) result from Janocha *et al.*³³.

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670 FIGURES

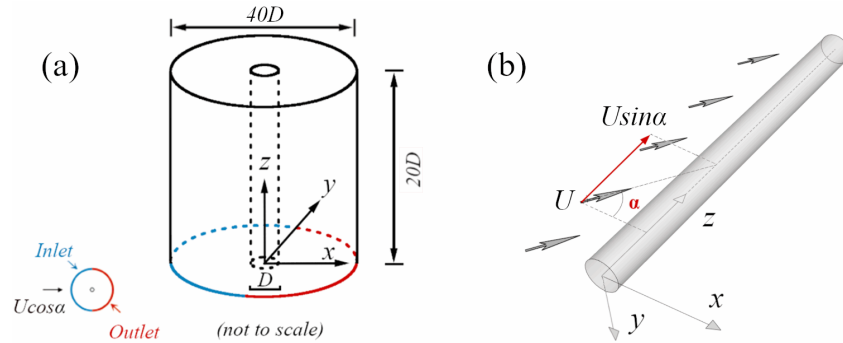


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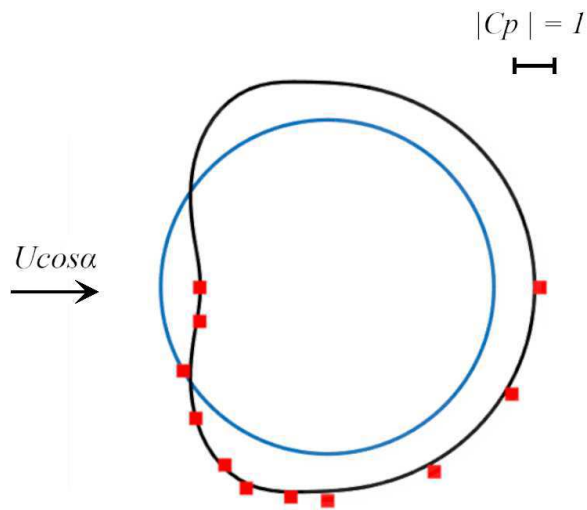


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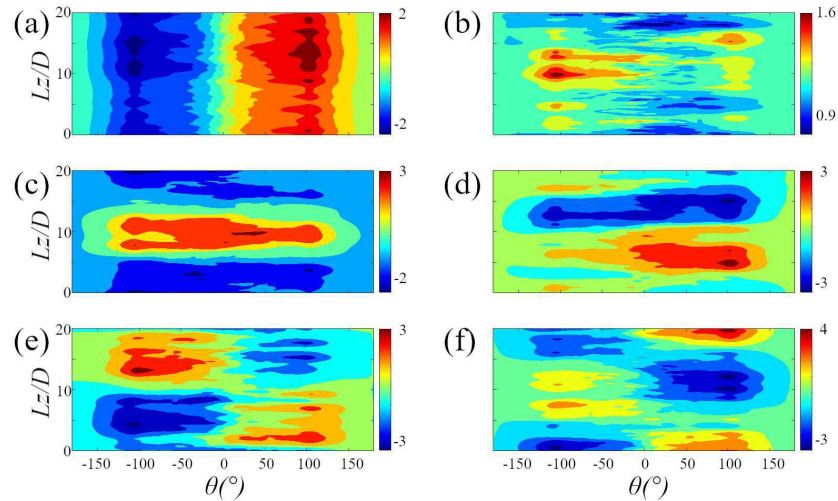


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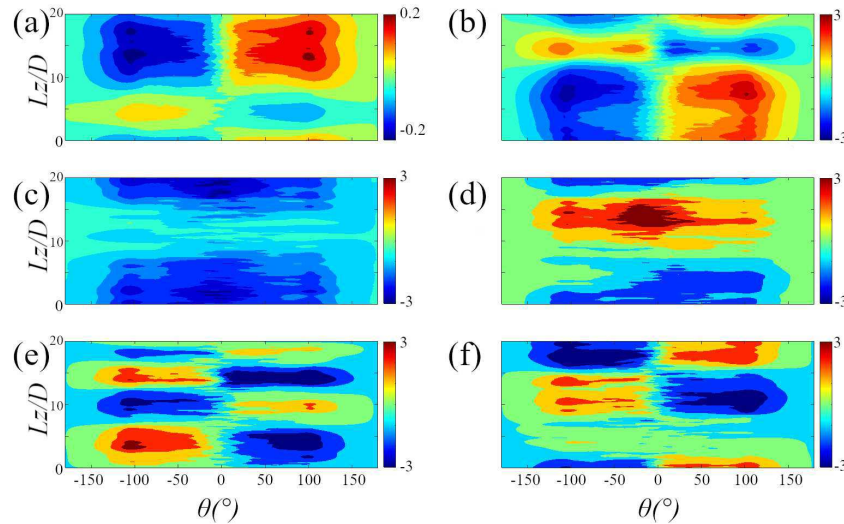


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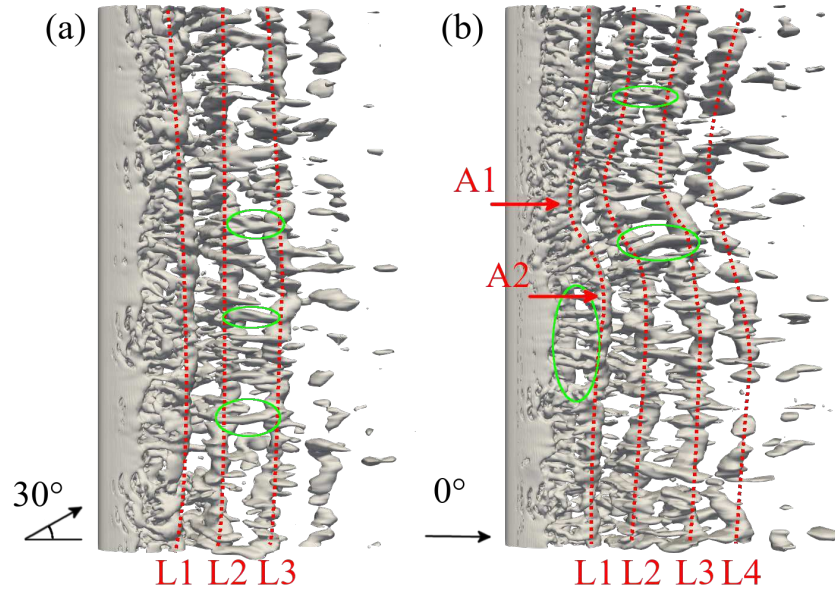


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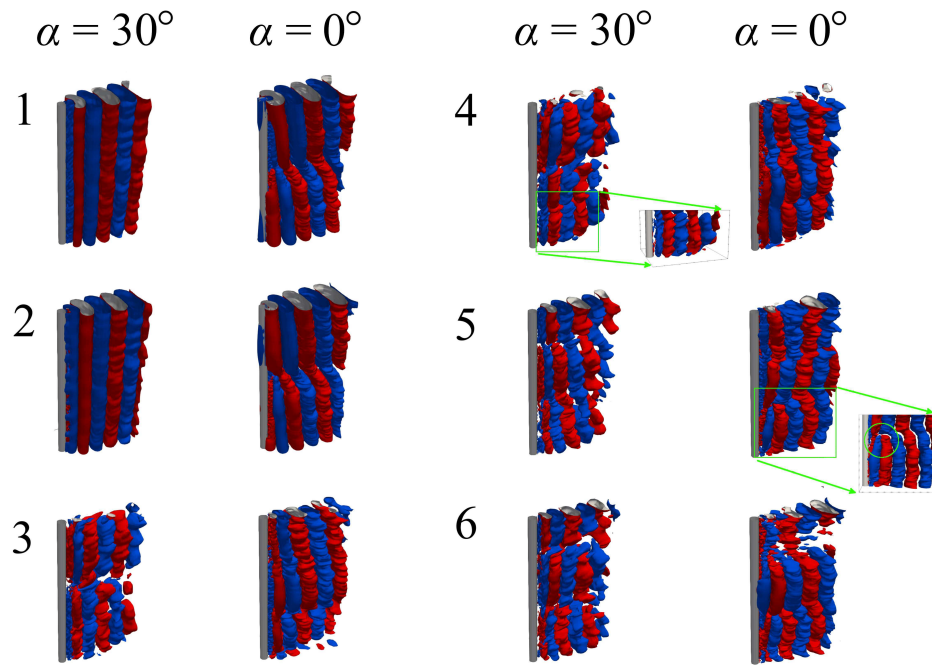


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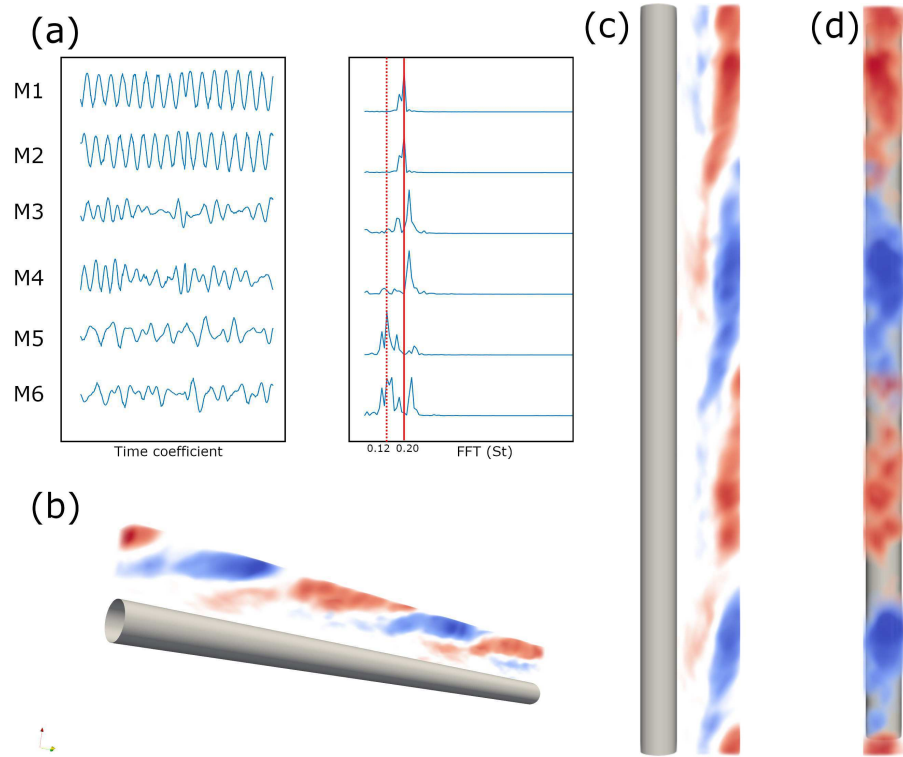


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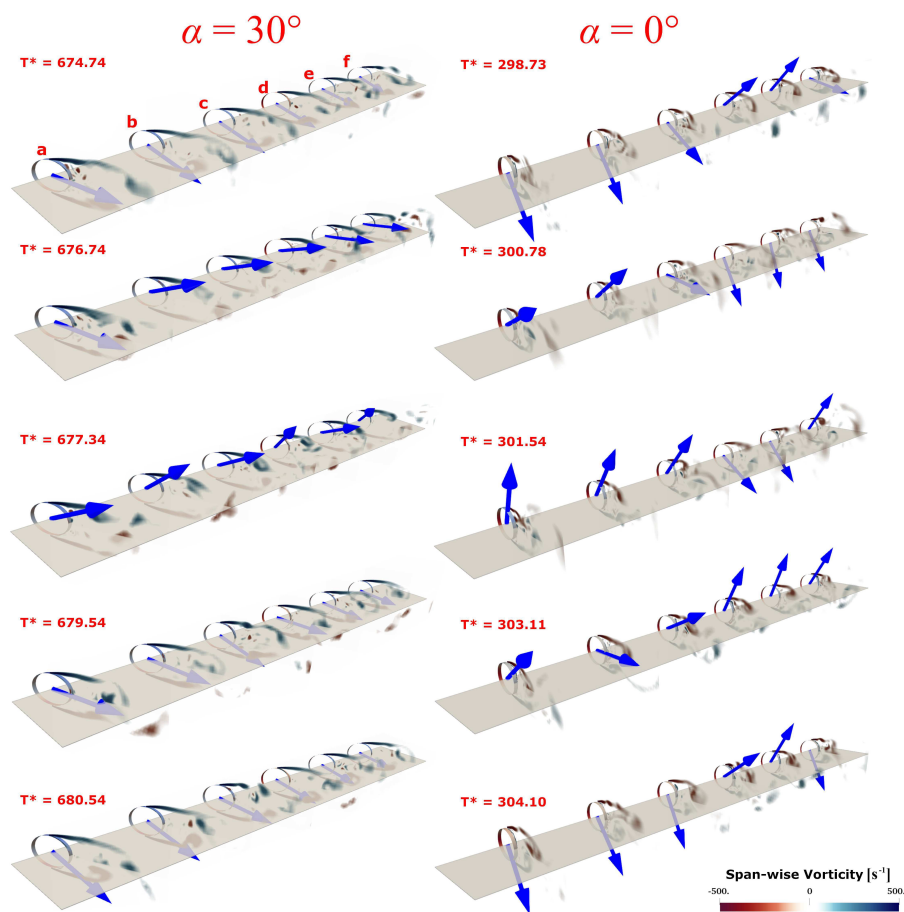


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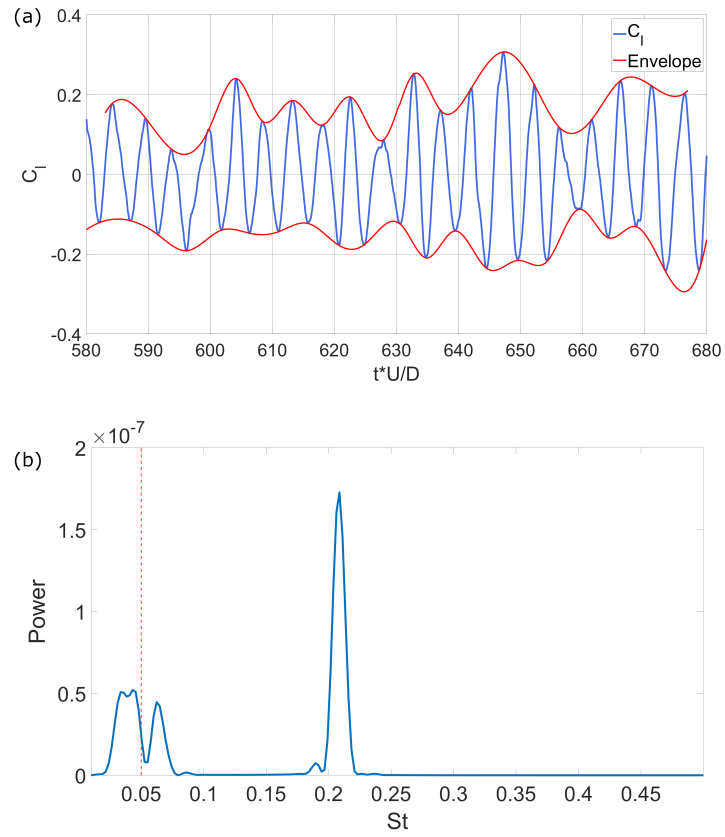


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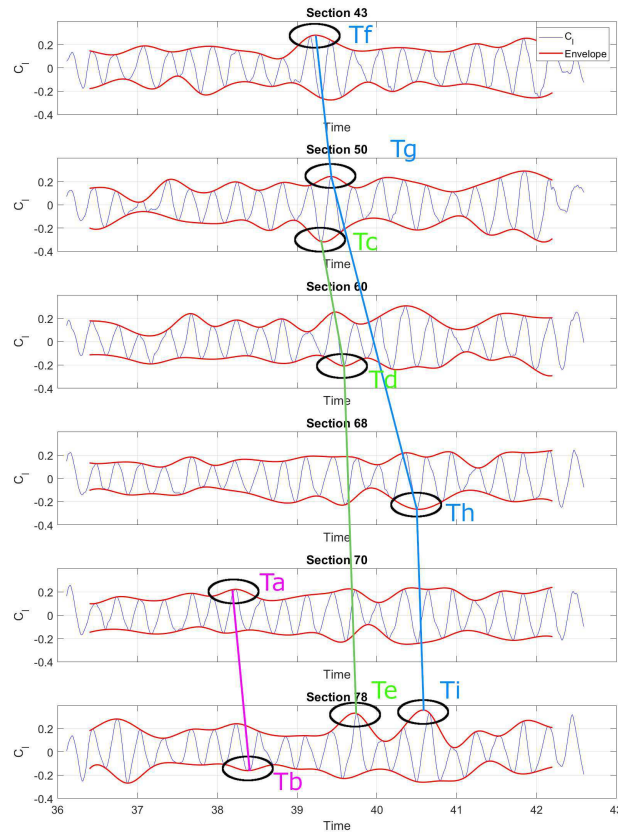


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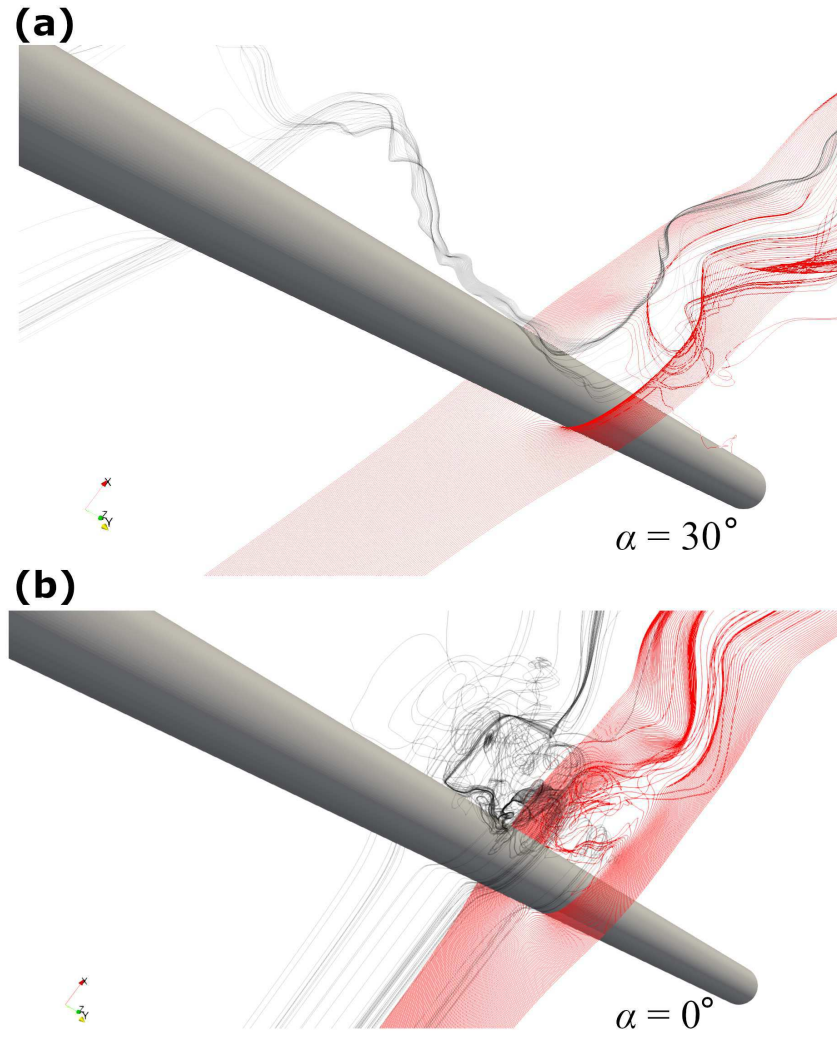


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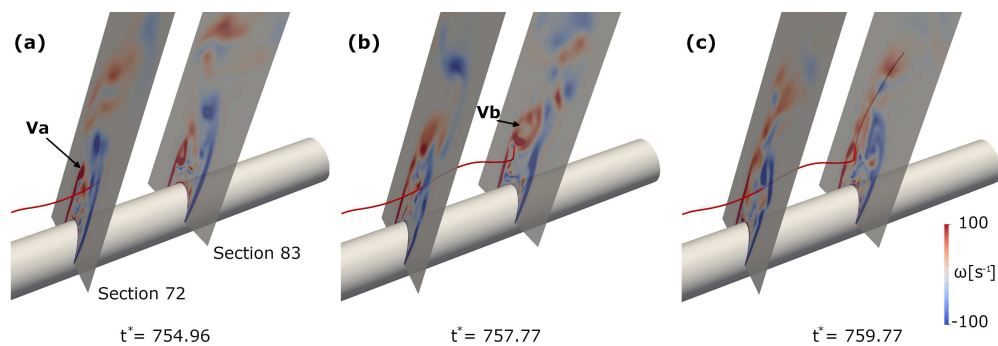


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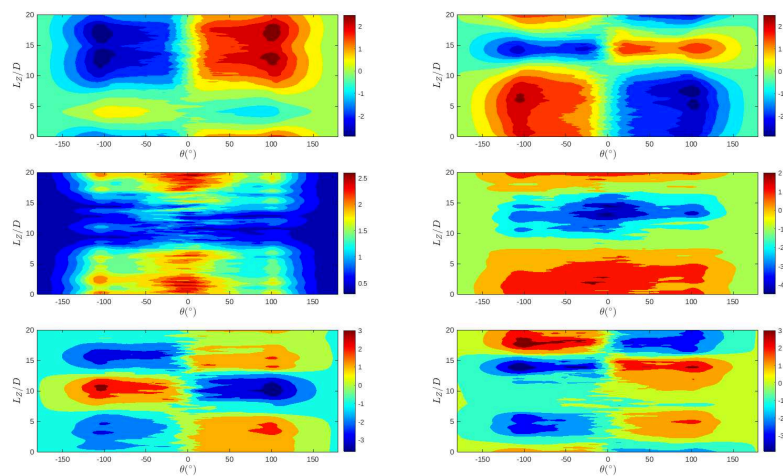


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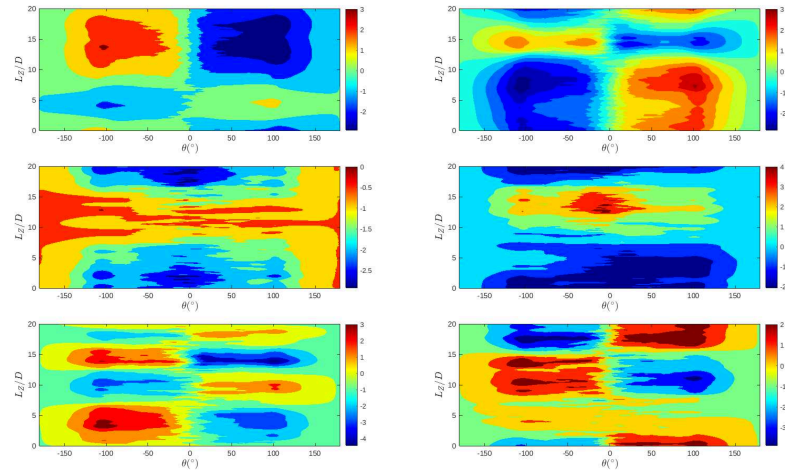


FIG. 14. The first six POD mode shapes for the surface pressure at $Re = 10^4$ and $\alpha = 0^\circ$. The number of time sequence is 1200.

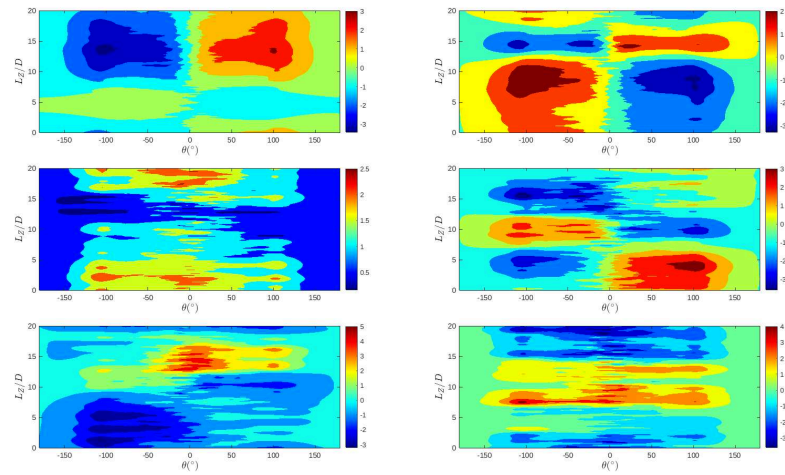


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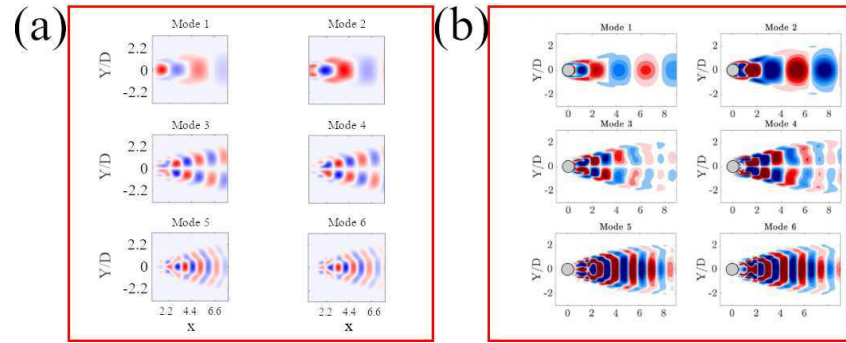


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