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Kinetics of catalytic oxidation of methane application of initial rate technique for mechanism determination.

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KINETICS OF CATALYTIC OXIDATION OF METHANE

APPLICATION OF INITIAL RATE TECHNIQUE

FOR MECHANISM DETERMINATION

A THESIS

Submitted to the Faculty of Graduate Studies through the

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the requirements for the degree of Master of Applied Science at

University of Windsor

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ABSTRACT

A kinetic investigation on the oxidation of methane using a palladium catalyst was conducted. A differential bed reactor was used, and the conversions of methane were limited to about 10%. The small conversions facilitated the use of the initial rate approach to find the reaction mechanism. Plots of initial rate against total pressure were used to interpret the data qualitatively. Linearised rate equations were used to find the regression coefficients for various plausible mechanisms. The criteria of best fit to experimental data eliminated many improbable mechanisms.

Data on the variation of initial rate with feed composition were very helpful in arriving at a definite mechanism for the oxidation reaction. The experimental results indicated that the reaction rate was controlled by surface reaction in which the adsorbed oxygen and adsorbed methane react to produce adsorbed carbon dioxide and adsorbed water. The corresponding rate equation has the form:

$$r = \frac{C\left[P_{CH_4}\, P_{O_2}^{2} - P_{H_2O}^{2}\, P_{CO_2}/K\right]}{\left[1 + K_{CH_4}P_{CH_4} + K_{O_2}P_{O_2} + K_{CO_2}P_{CO_2} + K_{H_2O}P_{H_2O}\right]^3}$$

(i)

ACKNOWLEDGEMENTS

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(ii)

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CHAPTER I

INTRODUCTION

Air pollution, in general, is a direct result of smoke,
dust or fumes from a variety of sources. Processes like
combustion, roasting, mining and quarying contribute greatly
to air pollution.

The objectionable components from incomplete combustion
of fuels in industry and automobiles are the hydrocarbons and
oxides of nitrogen. Hydrocarbons and nitrogen oxides are
present in such small concentrations that they probably have
no direct effect on health. But, as reported by Yocom[1], the
hydrocarbons react photochemically with nitrogen oxides to
produce unstable peroxides which act as a nuclei in smog production.
In major industrial cities, high concentrations of carbon monoxide,
coming from combustion processes and automobiles, can cause toxic
effect on humans.

At present the world's use of fuels is rising rapidly
because of industrialisation and development. As a result the
pollution hazard is growing. Reduction of smog forming components
and carbon monoxide in tail gases would be a necessary step towards
reducing air pollution.

Many devices[2] have been advanced so far for the prevention
of these undesirable components in tail gases of automobiles.
The following devices have been examined critically from a com-
mercial point of view:

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1. After burners
2. Liquid washing devices
3. Adsorption units
4. Catalytic converters

The major problem in the design of after burners is maintenance of a flame which will allow auto-ignition of hydrocarbons under all conditions. Liquid washing devices and adsorption with porous solids have not been very successful so far, because of the unwieldy size of such devices. Catalytic conversion is a promising alternative to other devices.

Extensive investigations on catalytic converters for carbon monoxide and hydrocarbons, were made by Lamb and co-workers[3] towards the end of World War I. The investigations of Lamb and co-workers and of Yant and Hawk[4] showed that the catalysts effective for carbon monoxide oxidation are also effective for hydrocarbons oxidation. Recently reported laboratory evaluations of catalysts for the automotive exhausts by Cannon and Welling[5] confirm the earlier results.

Table 6, 7 and 8[6] in Appendix 1 show typical compositions of automotive exhaust gases under different operating conditions. These tables show that methane constitutes 25 to 40% of the total hydrocarbons in tail gases. Furthermore, Anderson and co-workers[7] have reported that, in the light hydrocarbons family, methane is the most difficult gas to oxidise.

The data obtained from the catalytic oxidation of methane should be helpful in the design of a suitable catalytic reactor for automobile exhaust control. In addition to this, a kinetic investigation of the methane oxidation should be very interesting from a scientific point of view.

In the present investigation the objective was to establish the mechanism of catalytic oxidation of methane by using an initial rate approach. Obviously, the initial rate technique limited to low conversion experiments, does not provide data for design of catalytic converters for auto exhausts. Experiments at nearly complete conversion would be necessary to provide such information. However, integral rate data are difficult to evaluate from a mechanistic point of view.

For a study of a catalytic reaction, a two step process is recommended

(i) Initial rate analysis to establish the mechanistic equation.

(ii) High conversion study to fit the mechanistic equation in the desired conversion range.

The assumption that is inherent in the above scheme is that the adsorption characteristics of the components do not change over the range of conversion. This is considered a reasonable assumption for most catalytic reactions. The equilibrium quantities being function of temperature only, do not change with composition.

This investigation is concerned with the first stage of the scheme discussed above. Data at low conversion and varying pressure would be employed to establish the mechanistic equation. The rate equation obtained by initial rate approach, after addition of the proper product terms should be applicable for high conversion range.

CHAPTER II

LITERATURE REVIEW

A. <u>Survey of Oxidation Catalysts for Exhaust Gases</u>

Many investigations[8] have been reported on the partial oxidation of hydrocarbons to valuable organic substances as acids, aldehydes, alcohols, esters and ketones. In addition to this, a large amount of work has been done on the catalytic oxidation of exhaust gases and individual hydrocarbon constituents.

As early as 1825, the effect of platinum on the combustion of methane at $290°C$ was investigated by Henry[9]. Yant and Hawk[4] found that platinum had a catalytic effect at temperatures between 150 to $300°C$ for approximately 4% methane in air. Conversion was less than 10% in this temperature range.

The catalytic activity of copper oxide for methane oxidation has been studied by Campbell[10], Wheeler[11] and Araki[13]. According to them, copper oxide has a catalytic activity at rather elevated temperatures, in the range of $400 - 700°C$.

Yant and Hawk[4], Thompson[14], and Anderson and co-workers[7] found oxides of Ni, Cr, Mn, V and Co quite effective for methane oxidation. In particular, Co_3O_4 gave promising results with respect to conversion and catalyst life. According to recent experiments of Kazarnovskya and Dykhno[15], the most effective catalyst for oxidation of methane is manganic ore enriched with silver. The complete combustion of 0.10 - 0.15% methane in oxygen was observed at $300°C$. The detailed description of this catalyst is not given.

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Towards the end of World War I, a commercial material called Hopcalite was discovered for carbon monoxide gas masks. Hopcalite is a registered trade name with the Mine Safety Appliance Company, and is really a mixture of compounds which indlude, among others, manganese dioxide and cuprous oxide. After extensive investigations, Lamb and co-workers[3] found that the mixture of oxides of copper, manganese, silver and cobalt was most effective for oxidation of carbon monoxide. Yant and Hawk[4] have reported that commercial Hopcalite could oxidise 4% methane in air to carbon dioxide and water with 10 - 60% conversion over the temperature range 200 - 350°C. This catalyst is quite effective for dry gas, but poisoned very rapidly in presence of water vapour. It also loses activity on prolonged heating at temperatures above 250°C, due to sintering.

Anderson and co-workers[7] have concluded that the catalytic activity of metals and their oxides, decreases in the following order: Pd, Pt, Cr, Mn, Cu, Ce, Co, Fe, Ni, and Ag. This order of effectiveness was the same as previously reported by Cohn and Haley[16].

B. Kinetic Studies on the Oxidation of Hydrocarbons

Anderson and co-workers[7] did a kinetic study on the oxidation of methane. The catalyst bed was 7 to 7.5 cc. deep with a cross section of 2.435 sq. cm., methane concentration was 1% and air flow 2 liters/min. at room temperature. Thirty kinds of catalysts were tested over the temperature range 450 - 800°K, using a constant value of space velocity. The experimental data were approximated by an empirical equation with respect to methane concentration.

Rosenbaum[17] worked on the oxidation of very
dilute methane (51 ppm in air) at 1075°F by using the
pelletized catalyst supplied by Engelhard Industries. The
relationship between space velocity and conversion is given
in Table 9 in Appendix I. The volume of catalyst used was
0.0005 cu. ft. No details were given for the size and
composition of the catalyst.

Mezaki[18] used vanadia, cobalt, copper-chromite,
chrome alumina, hopcalite and palladium catalysts for me-
thane oxidation. He found palladium to be the most ef-
fective catalyst from the stand point of ignition temperature,
stability, freedom from side reactions, and good conversion.
However, palladium is not necessarily free from objectionable
features. It has a reported tendency of poisoning by lead
compounds.

Mezaki studied the catalytic oxidation of methane using
0.5% palladium on alumina catalyst. Methane concentrations
in feed were 1 to 2%. The reaction temperature was varied
between 320 to 380°C and the pressure was kept atmospheric.
The feed in addition to reactants contained reaction products
as well. In this connection, Mezaki has correctly pointed
out that when the feed to reactor contains the reaction
products, one cannot use the initial rate - total pressure
correlation to screen the postulated mechanisms.

In an initial survey, Mezaki[19] used 84 models in
which adsorption of reactants or desorption of products was
the postulated rate-controlling step. The linearised models
were fitted to the experimental rate-data by least square
technique, but this fitting resulted in two or more negative
constants. This led to the rejection of these models.

Then, assuming that surface reaction is the rate controlling step, Mezaki used integral kinetic equations for fitting the experimental data to postulated models. He eventually concluded that the controlling step in the oxidation of methane is surface reaction between adsorbed oxygen and gaseous methane to give adsorbed carbon dioxide and water. There is no apriori reason to suspect that in a catalytic reaction, at different temperatures, the same step is rate controlling. Recent applications of the initial rate technique have established that for the same catalytic reaction at different temperatures, different steps could be rate controlling. Thaller and Thodos[20] and Mathur[21] have reported changes in controlling step at different temperatures for two quite different types of catalytic reactions. In view of this, Mezaki's treatment of kinetic data appears to be somewhat empirical.

C. Important Considerations in the design of a Catalytic Converter

Many factors have to be considered for the design of a catalytic converter for auto exhausts. Different makes and life of automobiles, fuels and wide range of operating conditions lead to great variation in physical and chemical properties of exhaust gases. A brief review of the current situation follows.

(i) Exhaust Gas Temperature

Exhaust gas temperatures are changed by operating conditions. Temperatures from 150 to 1500°F have been observed depending on engine operation and location of measurement in tail gas pipe. Therefore, it is essential to determine the lowest temperature at which the

catalytic conversion starts and highest working
temperature of catalyst.

(ii) Exhaust Gas Flow Rate

From measured air intakes of passenger cars,
computed exhaust volumes, at 1 Atm. and $70°F$, range
from 6 to 10 cfm. at idle, to 50 cfm. at 50 mph. The
flow rate at accelration might reach 250 cfm.

(iii) Exhaust Gas Composition

Hydrocarbons, hydrogen and carbon monoxide are
the major combustible components in the exhaust gases.
The concentrations of these components vary greatly
depending on operating conditions and air-fuel ratio.
Tables 6, 7 and 8[6] in Appendix I show some typical
compositions of automobile exhaust gases under dif-
ferent operating conditions.

If automobiles were running at fairly constant
rates, the kinetics of exhaust gas oxidation could be
solved for a steady state condition. When an automo-
bile starts to run, the oxidation process gives a compli-
cated unsteady state problem. Generally, an automobile
starts in a residential area, goes through more.populated
zones at variable engine conditions, and runs through
sparsely populated areas at rather constant conditions.
When the engine starts, it stays at a rather low tempe-
rature and the exhaust contains a large amount of carbon
monoxide and hydrocarbons. Therefore, the oxidation
catalyst needs to be specially active at low temperature.

It should also have good conversion, good life, and inertness to lead compounts.

The pressure drop through the catalytic converter should be low to reduce power cost for compression of gases. The converter should also be compact in construction.

CHAPTER III

THEORETICAL CONSIDERATIONS

In a solid catalyzed reaction the physical steps are the transfer of the fluid reactants upto the catalyst surface, diffusion of reactants into the interior of the pellet, diffusion of products back to the surface and transfer of products from the exterior surface to the main stream. To simplify the kinetic interpretation of the experimental data, these physical steps have to be minimised.

The chemical steps involve activated adsorption of reactants with or without dissociation, surface reaction on active sites and activated desorption of products. From an absolute theory point of view, the adsorption process is a bimolecular reaction involving a molecule or an atom from the gas phase and an active point on the catalyst surface.

In order to determine the mechanism of a catalytic reaction on the basis of the Hougen Model[21], various possible reaction schemes are investigated. The acceptability criteria for any rate equation is that all equilibrium constants have to be positive.

As an illustration, consider a scheme in which the surface reaction is between an adsorbed methane molecule and two oxygen molecules dissociated and adsorbed on dual sites. The rate equations for adsorption, surface reaction and desorption steps are deduced from the treatment given by Hougen[21]

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ADSORPTION STEPS

(i) Adsorption of oxygen:-

$$2\ O_2 + 2\ 1_2 \rightleftharpoons 2\ O_2 1_2 \tag{1}$$

$$2\ O_2 1_2 + 4\ 1 \rightleftharpoons 4\ O1 + 2\ 1_2 \tag{2}$$
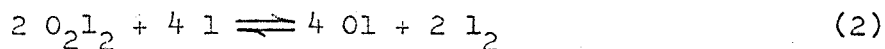
Eq. (1) is rate controlling and equilibrium maintained in (2), net rate of adsorption of oxygen

$$R\ ads. = k_{O_2}\ a^2_{O_2}\ c^2_{1_2} - k'_{O_2}\ \frac{\left[c_{O1}\right]^4 \left[c_{1_2}\right]^2}{K'_{O_2}\left[c_1\right]^4} \tag{3}$$

(ii) Adsorption of methane:-

$$CH_4 + 1 \rightleftharpoons CH_4 1 \tag{4}$$

net rate of adsorption of methane

$$r = k_{CH_4}\ a_{CH_4}\ c_1 - k'_{CH_4}\ c_{CH_4 1} \tag{5}$$

SURFACE REACTION

Surface reaction between four adsorbed oxygen atoms and adsorbed methane molecule to give activated complex involving one carbon dioxide molecule and two water molecules and two active centres

$$4\ O1 + CH_4 1 \rightleftharpoons CO_2 1 + 2\ H_2 O1 + 2\ 1 \tag{6}$$
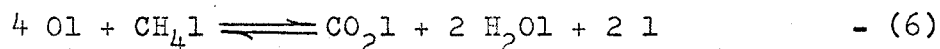
net rate of surface reaction

$$R\ s.r. = \frac{s(s-1)\ k s.r.}{L^2}\left[c_{CH_4 1}\ c^4_{O1} - \frac{c_{CO_2 1}\ c^2_{H_2 O1}\ c^2_1}{K' s.r.}\right] \tag{7}$$

DESORPTION STEPS

(i) Desorption of Carbon dioxide

$$CO_2 l \rightleftharpoons CO_2 + l \qquad\qquad (8)$$
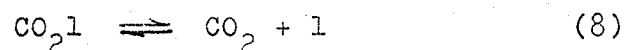
net rate of desorption of CO_2

$$r\ des. = k'_{CO_2}\ C_{CO_2 l} - k_{CO_2}\ a_{CO_2}\ C_l \qquad (9)$$

(ii) Desorption of water

$$2H_2Ol \rightleftharpoons 2H_2O + 2\ l \qquad\qquad (10)$$

net rate of desorption of H_2O

$$r\ des. = k'_{H_2O}\ C^2_{H_2Ol} - k_{H_2O}\ a^2_{H_2O}\ c^2_l \qquad (11)$$

If the adsorption of oxygen is rate controlling step and
the adsorption of methane, the surface reaction, the desorption
of CO_2 and H_2O are equilibrium steps. The rate of reaction
would be

$$r = k_{O_2}\ \left(\frac{s}{2L}\right)^2\ c^4_l \left[a^2_{O_2} - \frac{1}{K}\ \frac{a_{CO_2}\ a^2_{H_2O}}{a_{CH_4}}\right] \qquad (12)$$

C_l, total concentrations of vacant active centres, is
given by

$$C_l = L - C_{CH_4 l} + C_{CO_2 l} + C_{H_2Ol} + C_{Ol} \qquad (13)$$

or, $$C_l = \cfrac{L}{\left[1 + K_{CH_4}\ a_{CH_4} + K_{CO_2}\ a_{CO_2} + K_{H_2O}\ a_{H_2O} + \sqrt[4]{\cfrac{K_{O_2}\ a_{CO_2}\ a^2_{H_2O}}{K\ a_{CH_4}}}\right]}$$

$$(14)$$

from (12) and (14)

$$r = \frac{k_{O_2} s^2 L^2 \left[a^2_{O_2} - \frac{1}{K} \frac{a_{CO_2} a^2_{H_2O}}{a_{CH_4}} \right]}{4 \left[1 + K_{CH_4} a_{CH_4} + K_{CO_2} a_{CO_2} + K_{H_2O} a_{H_2O} + \sqrt[4]{\frac{K_{O_2}}{K} \frac{a_{CO_2} a^2_{H_2O}}{a_{CH_4}}} \right]^4} \qquad - (15)$$

If product concentrations are very small as compared to reactant concentrations, the rate of reaction can be written, as,

$$r = K \left[a^2_{O_2} \right] \bigg/ \left[1 + K_{CH_4} a_{CH_4} \right]^4 \qquad - (16)$$

For a constant ratio of methane to oxygen, and assuming ideal gas law condition, equation (16) can be written in terms of total pressure, π , as follows

$$r_O = a \pi^2 \bigg/ \left[1 + b \pi \right]^4 \qquad - (17)$$

The simplicity and directness of the initial rate equation (17), as compared to the complete rate expression, equation (15), is obvious.

Yang and Hougen[22] pointed out that initial rate analysis is one of the best techniques to establish the mechanism of a catalytic reaction. They have discussed in detail the type of results that are to be anticipated when the initial rates are plotted against total pressure and feed composition.

By systematic and independent variations in total
pressure and feed composition, the plots of initial rates
against total pressure and feed composition are obtained.
Through an interpretation of these plots, it is possible
to establish the rate controlling step or steps of the
catalytic reaction with assurance. Moreover, initial rate
approach does not assume that the same controlling step or
steps are operative at all temperatures.

As pointed out in the introduction the initial rate
equations are not complete rate equations for a catalytic
reaction. The initial rate approach nevertheless provides
for a much more direct determination of the mechanism of
a catalytic reaction.

In this investigation the objective is to establish
the mechanism of methane oxidation at different temperatures.
The overwhelming advantages of the initial rate technique,
as apposed to the conventional approaches, recommended for
this investigation.

CHAPTER IV

EXPERIMENTAL EQUIPMENT AND MATERIALS

The reaction rate data for the oxidation of methane was
obtained using a differential bed reactor confined in a
cylinderical tube. A schematic diagram of the set up is shown
in Figure 1. The details of the equipment and materials used are
given below:-

(A) Reactor, Preheater and Accessories

The reactor tube and the differential bed are shown
in Figure 2. The reactor tube was made of 1½ inch I.D.,
schedule 40, 304 stainless steel tubing. The ends of the
tube were fitted with 300 psig. welding neck flanges and
matching blind flanges. Copper gaskets of 1/8 inch thickness
were used for leakproof closure of the tube. Thermowells
were welded to top and bottom flanges. To facilitate
insertion of ¼" berl saddles, 3/8" O.D.S.S. tube was also
welded to top and bottom flanges.

The differential bed consisted of a 1 3/8" O.D., 1/8"
thick, 5 1/2" long S.S. cartridge. Its ends were closed
by screens and washers. The screens fitted snugly with
the inside of the reactor tube with little clearance.
Catalyst mixed with ceramic berl saddles was charged into
the cartridge. This minimised the non-uniformity of bed
and channeling effects. The catalyst bed occupied the
space between the ends of the thermowells, rest of reactor
space was packed with 1/4" ceramic berl saddles.

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SYMBOL	DESCRIPTION
P.C.V.	PRESSURE CONTROL VALVE
C.V.	CHECK VALVE
S.R.V.	SAFETY RELIEF VALVE
P.G.	PRESSURE GAUGE
T	THERMOMETER
F	FURNACE
N.V.	NEEDLE VALVE
R	ROTAMETER

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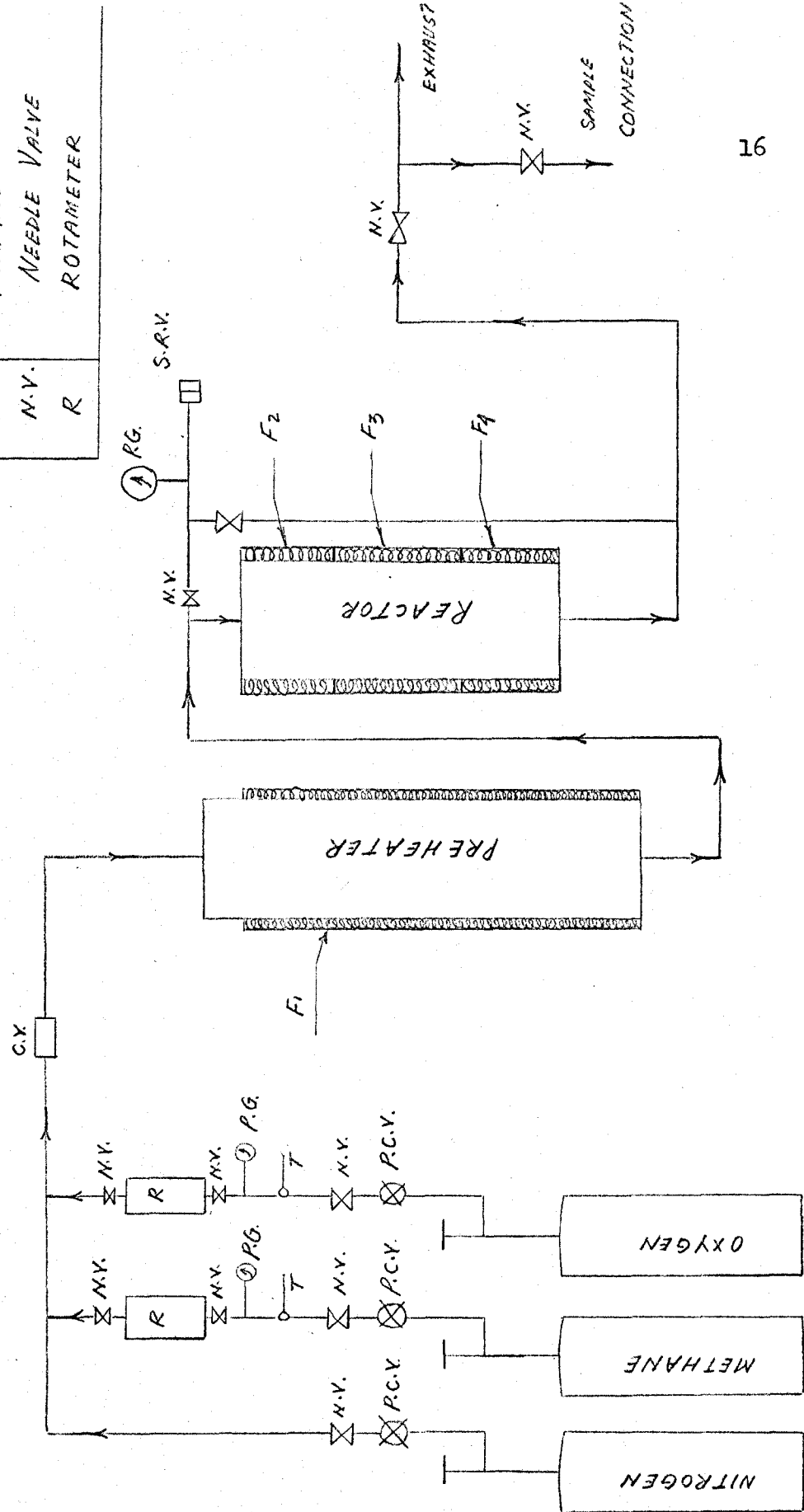
FIG. 1 SCHEMATIC DIAGRAM OF EXPERIMENTAL EQUIPMENT
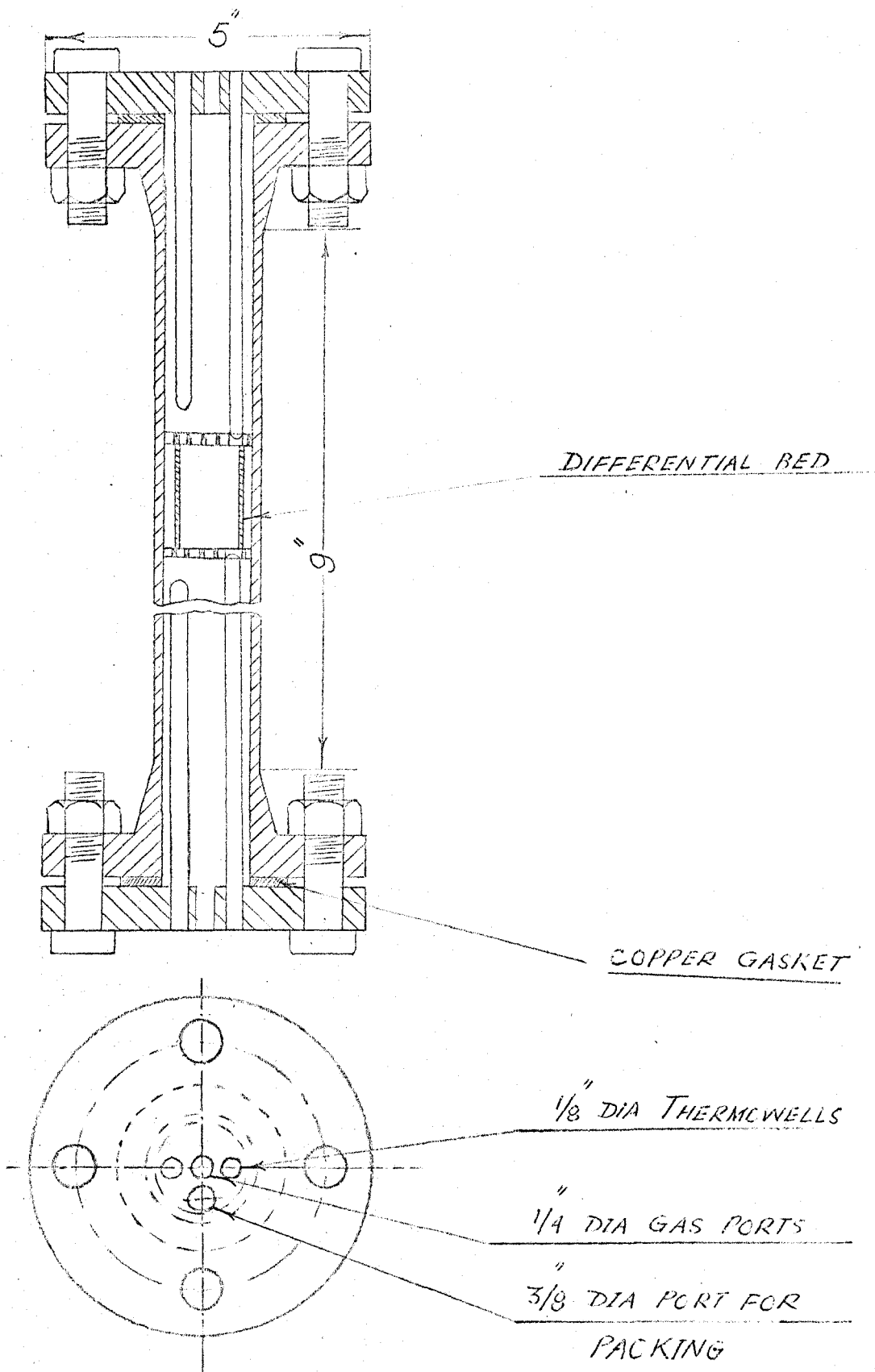
FIG. 2   SECTIONAL VIEW OF REACTOR TUBE AND DIFFERENTIAL BED

The preheater construction was basically identical to that of the reactor. A minor difference was that reactor tube was 3 inches shorter than the preheater tube. The preheater was packed with 1/4" ceramic berl saddles.

The tubing connecting the gas cylinders to preheater was 1/4" O.D. Copper. From preheater exit to sampling connection, the tubing was 1/4" O.D. S.S. Standard screwed swagelok fittings were used for all connections.

The preheater was heated by 12" long, 1400 watts cylinderical heating units. The reactor had three independently controlled heating sections of lengths 3 1/2", 5" and 3 1/2" rated at 700, 1160 and 700 watts respectively. The furnaces were insulated with refractory fibre felt supplied by Johns Manville. To prevent condensation of water vapours in the system, the tubing from preheater exit to sampling connection was heated with electric heating tape.

Chromel-alumel thermocouples in 1/16" O.D. stainless steel sheaths were used for temperature measurement.

A pressure gauge of range 0-400 psig. with valve connections at the inlet and the outlet of the reactor, was used to measure the operating pressure of the system. A spring loaded pressure relief valve set at 500 pounds, was used as the safety device.

(B) Flow Measurement Devices

Rotameters were used to measure the flow rates
of oxygen and methane. These were equipped with dual
floats, one of pyrex, the other of stainless steel.
The maximum flow ranges with the two floats were 4.4
and 8.8 SCFH of air. The rotameters for oxygen and
methane were identical in all respects. These were
supplied by Matheson Co.

(C) Analytical Equipment

The analytical equipment for reactants and products
was a gas chromatograph. It was a 5000 series selecta
system model supplied by Barber Colman Ltd. It had dual
column bath and six port thermal conductivity detector.
The arrangement of the columns connected to the six ports
is given in Figure 17 of Appendix II. The first column
was a 1/4" O.D.; 1 ft. silica gel type followed by 1/4"
O.D. 7 ft. molecular sieve column. The second column
was 1/8" O.D.; 15 ft. carbowax 1500.

Other major parts of the chromatograph were carrier
gas supply regulators, injector bath, column bath, detector
filaments current supply and the recorder. All syringes
were gas tight.

(D)   The catalyst, 0.5% palladium on alumina supplied by
Engelhard Industries Inc., had the following physical
properties:-

Bulk density	56 pounds per cu. ft.
Surface area	120 square metres per gram.
Size	1/8" x 1/8" cylinderical pellets

(E) <u>Selection of Gases</u>

(i) Oxygen gas was supplied by Liquid Carbonic Corporation and was of 99.9% purity.

(ii) Methane gas was of chemically pure grade supplied by Matheson Co. It was of minimum 99% purity. The typical average composition of the gas in given in Table 10, Appendix I.

(iii) Nitrogen and carbon dioxide used for calibration were of 99.9% purity and supplied by Liquid Carbonic Corporation.

(iv) Carbon monoxide used for calibration was of C.P. grade supplied by Matheson Co. It was of minimum 99.5% purity.

(v) The helium gas used as carrier in the chromatograph was of 99.99% purity. It was supplied by Liquid Carbonic Corporation. An alumina packed filter was used in the helium line to prevent, any trace of water vapour in the helium gas from entering the system.

CHAPTER V

OPERATIONAL DETAILS AND RESULTS

The operational procedure for conduction of kinetic runs is summarised in this chapter.

(A) Calibration Procedure

(i) Calibration of Rotameters

For rotameters operating under a constant pressure difference but with a constriction of variable area, the mass flow rate is related to the scale reading by the following expression[23]

$$W = C_r A_o \left[\frac{2 \, g \, \rho (\rho_f - \rho)}{A_f} \right]^{1/2} \qquad (18)$$

Since the float density is normally an order of magnitude larger than the density of the fluid whose flow is being measured, equation (18) can be approximated to

$$\frac{W}{\sqrt{\rho}} = C_r A_o \qquad (19)$$

The coefficient of discharge C_r is sensitive to the viscosity and to the flow lines through the constriction. For high flow rates, C_r tends to assume a constant value, and for this reason it is convenient to calibrate the flow meters according to the procedure suggested by equation (19).

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The calibration of methane and oxygen rotameters was done by measuring actual flow rates with a precision wet-test meter. The upstream pressures and temperatures of the gases were measured by pressure gauges and thermometers installed in the lines before the rotameters inlet. Since neither of the gases is soluble in water, the presaturator of the wet test meter was filled with distilled water. The calibration curves for the rotameters over the complete range of investigation are given by Figures 15 and 16 in Appendix II.

(ii) Calibration of Thermocouples

The chromel-alumel thermocouples used to measure temperatures were calibrated against the boiling point of distilled water and the melting points of chemically pure tin and zinc. The observed temperatures were extremely close to standard temperatures. Therefore, the error involved in measurement of experimental temperatures, is negligible.

(iii) Calibration of Chromatograph

(a) Principle

The carrier gas is introduced into the system at a specified flow rate. The column, injector and detector baths are heated to the required isothermal temperatures. These temperatures are chosen to prevent condensation of any component at any stage of the process. Another operational consideration is that separation of different components should be explicit. A sample mixture is then injected into the

injector part. As the sample is carried through the columns, the components are separated according to their respective solubilities in the column charge. The components having little affinity for the column material pass through the column rapidly, while those with greater affinities are retained in the column for longer periods.

As each component emerges from the column, it is driven into the sensing side of the detector located immediately after the column exit. The other side of the detector which is the reference side is upstream of the sample injection block and is filled with carrier gas prior to the point at which the sample is injected. Thermistors in each chamber of the detector are connected to a balanced bridge circuit and are cooled by the gases to which they are exposed. When a component enters the sensing chamber, the thermistor bridge circuit is un- balanced and generates a signal. The signal is propor- tional to the difference in thermal conductivities of the carrier gas and the component. The signal drives a re- corder pen to produce, in graphic form, a quantitative and qualitative description of the component.

(B) Calibration

Due to large number of components to be analyzed, the silica gel column, followed by molecular sieve column, were found to give explicit separation of all the desired components. The silica gel column gave combined peak and peak for carbon dioxide.

The molecular sieve column gave separation for oxygen, nitrogen, methane and carbon monoxide.

The operating conditions for the analytical set-up are given by Table 11, in Appendix I.

The concentration of any component is directly proportional to the peak area. However, in this case, a measurement of peak height gave a reasonably accurate proportionality to component concentration. This relation was valid for pure components as well as for the mixtures used. The calibration curves for different components are given by figures 18 to 22, in Appendix II. The concentration of water was found by difference. Absence of alcohol and aldehydes was established during the trial runs of methane oxidation, thus calibrations for these components were not done.

(B) Operational Procedure

The preheater and reactor furnaces were switched on and variacs adjusted to heat the system to the desired temperature. Oxygen gas was fed through the rotameter, with the feed rate and reactor exit valve being adjusted for the desired working pressure. After the temperatures had stabilised, methane gas was slowly fed to the system through the rotameter. The flow-rates of oxygen and methane, the reactor exit valve and the variacs were adjusted for desired working pressure and isothermal temperature of the differential bed.

The reaction was allowed to proceed for about one hour, at the desired conditions, before the first sample was taken for analysis. Three samples were taken for each run. The average

of the three readings was used to calculate the product composition. It took about fifteen minutes for analysis of each product sample. Therefore, each sample was withdrawn at an interval of fifteen to twenty minutes after the attainment of equilibrium conditions.

Preliminary runs confirmed Mezaki's [18] observations that the catalyst achieved uniform activity after twenty hours of service. Therefore, for each series of runs, the catalyst was first allowed to attain uniform activity.

Prior to the start of the runs, with the catalyst, blank runs were made with different oxygen methane ratios within the range of operating temperatures and pressures. These blank runs confirmed that no parts of the equipment contributed to the conversion.

(C) Results

Following the procedure outlined above, two series of runs were made. For both series the catalyst charge was 0.498 gm. One series of runs was with about 6% to 30% methane, at about 1.8 atmospheres total pressure and at temperatures of 300, 320 and $340^\circ C$. The second series of runs was made at almost constant feed composition of about 6.5% methane. The total pressure was varied from 1.8 to 9.7 atmospheres. The runs were at isothermal temperatures of 300, 320 and $340^\circ C$.

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The percentage of products was 0.4 to 1.2%, and conversions were 3.69 to 9.10%. For such small conversions, it is accurate enough to consider the reaction to be differential. Initial rates of reaction were computed from the expression

$$ro = \frac{X_{AO}}{W \, / \, F_{AO}} \qquad (20)$$

The method of computation of initial rate from experimental data, is given in Appendix III. The results of the experimental runs are given by Table 1.

Table - 1

Experimental Results of Oxidation Runs

Run No.	Temperature °C	Total Pressure Atm.	Flow Rate lb-moles/hr. Methane	Flow Rate lb-moles/hr. Oxygen	Conversion % $\dfrac{\text{lb-moles } CH_4 \text{ converted}}{\text{lb-moles } CH_4 \text{ in feed}} \times 100$	Rate of Reaction $\dfrac{\text{lb-moles } CH_4 \text{ converted}}{(\text{hr.})(\text{lb. of catalyst})}$
I - 1	300	1.817	0.00474	0.0664	8.66	0.373
I - 2	320	1.817	0.00481	0.0664	9.56	0.398
I - 3	340	1.817	0.00484	0.0664	9.10	0.421
II - 1	300	1.817	0.01179	0.0664	7.43	0.796
II - 2	320	1.817	0.01177	0.0664	7.82	0.836
II - 3	340	1.817	0.01175	0.0664	8.31	0.882
III - 1	300	1.817	0.0251	0.0664	3.69	0.842
III - 2	320	1.817	0.02497	0.0664	3.90	0.884
III - 3	340	1.817	0.0253	0.0664	4.15	0.932
IV - 1	300	2.975	0.00628	0.0906	8.43	0.481
IV - 2	320	2.975	0.00632	0.0906	8.89	0.511
IV - 3	340	2.975	0.00639	0.0906	9.41	0.552
V - 1	300	3.925	0.007125	0.1029	7.76	0.503
V - 2	320	3.925	0.00724	0.1029	8.06	0.531
V - 3	340	3.925	0.00720	0.1029	8.86	0.580

Table - 1 (Cont'd)

Experimental Results of Oxidation Runs

Run No.	Temperature °C	Total Pressure Atm.	Flow Rate lb-moles/hr. Methane	Flow Rate lb-moles/hr. Oxygen	Conversion % $\frac{\text{lb-moles } CH_4 \text{ converted}}{\text{lb-moles } CH_4 \text{ in feed}} \times 100$	Rate of Reaction $\frac{\text{lb-moles } CH_4 \text{ converted}}{(\text{hr.})(\text{lb. of catalyst})}$
VI - 1	300	5.22	0.00816	0.1173	7.54	0.559
VI - 2	320	5.22	0.00812	0.1173	7.89	0.581
VI - 3	340	5.22	0.00819	0.1173	8.60	0.640
VII - 1	300	6.24	0.0088	0.1270	7.42	0.594
VII - 2	320	6.24	0.0087	0.1270	7.74	0.616
VII - 3	340	6.24	0.00886	0.1270	8.36	0.673
VIII - 1	300	7.13	0.00961	0.1392	7.15	0.624
VIII - 2	320	7.13	0.00958	0.1392	7.57	0.658
VIII - 3	340	7.13	0.00971	0.1392	8.16	0.720
IX - 1	300	8.41	0.01117	0.1610	6.45	0.655
IX - 2	320	8.41	0.01123	0.1610	6.80	0.694
IX - 3	340	8.41	0.0112	0.1610	7.41	0.745
X - 1	300	9.70	0.01231	0.1753	5.99	0.671
X - 2	320	9.70	0.01225	0.1753	6.39	0.712
X - 3	340	9.70	0.01232	0.1753	6.89	0.771

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CHAPTER VI

ANALYSIS OF RESULTS

In the interpretation of experimental kinetic data, many experimental errors might be encountered. A detailed consideration of the errors that might affect the observed rate of reaction is essential to a valid interpretation of experimental results. Hougen[24] has discussed these errors, arranged below in the order of decreasing importance:

1. Variation in catalyst activity.
2. Departure from unity in effectiveness factor of catalyst.
3. External resistance due to mass and heat transfer.
4. Neglect of pressure drop due to flow.
   Besides these, the following sources of experimental errors should also be considered.
5. Side reactions.
6. Homogenised reaction and catalyzed reaction by reactor wall.
7. Errors associated with analysis, flow measurement and temperature measurement.

1. Variation in Catalyst Activity

Mezaki[18], who used the same catalyst as the one employed in this investigation, reported that catalyst activity decreases considerably during the twenty hour service period. After this period the activity reached a fairly constant value. Therefore for each series of runs, the catalyst was first allowed to attain uniform activity.

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2. <u>Departure from unity in effectiveness factor of Catalyst</u>

The effectiveness factor of a catalyst pellet is defined by Hougen[24] as follows:

"The effectiveness factor of a catalyst pellet is the ratio
of the actual reaction rate per unit mass of catalyst when
the catalyst is distributed throughout a porous pellet to
the rate where the available catalyst is restricted to the
exterior surface of the surface." The catalyst used in this
investigation consisted of small pellets, 1/8" x 1/8". In
this catalyst, the penetration of palladium into alumina
pallets was only superficial. The most active part of the
catalyst was distributed on the surface or located near
enough the surface. Therefore, it was assumed that the
effectiveness factor was very close to unity.

3. <u>External resistance due to mass and heat transfer</u>

Yang and Hougen[22] have detailed the equations for
calculating heat and mass transfer effects for different
operating conditions. The calculations for run 1 - I are
given in Appendix III.

Results of these calculations indicate that for all
runs, the heat and mass transfer effects were negligible.

4. <u>Neglect of pressure drop due to flow</u>

To take into account pressure drop due to flow, the
operating pressure was taken as the mean of reactor inlet
and outlet pressures.

5. <u>Side reactions</u>

In the trial runs over the range of operating con-
ditions, no side products were detected by the chromato-
graphic analysis.

6. <u>Homogenized reaction and catalyzed reaction by reactor walls</u>

In the blank runs over the range of operating con-
ditions, no reaction products were detected by the chroma-
tographic analysis.

7. <u>Errors associated with analysis, flow measurement and tempe-
rature measurement</u>

The errors due to analysis of feed streams and product
streams were less than 0.5%. The errors due to flow measu-
rement and temperature measurement were negligible.

<center>KINETIC INTERPRETATION OF RESULTS</center>

The interpretation of the initial rate results consists
usually of two parts, first, a qualitative interpretation based
on the nature of results obtained, and second, a statistical
interpretation to obtain a quantitative rate expression. The
acceptability criteria for statistical interpretation is that for
any rate equation, all equilibrium constants have to be positive.
The various plausible mechanisms for the reaction are given in
Table 2.

The initial rates obtained in this experimental study were
plotted against the total pressure value. The plots for the three
temperatures 300, 320 and 340°C are given in figures 3, 4 and 5.

TABLE 2(a) INITIAL RATE EQUATIONS FOR PROBABLE MECHANISMS

REACTION	REACTION MECHANISM	RATE CONTROLLING STEP			
		a) ADSORPTION of OXYGEN	b) SURFACE REACTION	c) DESORPTION of PRODUCTS	d) ABSORPTION of METHANE
I	Adsorbed oxygen, methane, carbon dioxide and water. Oxygen dissociated and adsorbed, Surface reaction: $CH_4 1 + 4O1 \rightleftharpoons CO_2 1 + 2H_2O1 + 2l$	$\dfrac{a\Pi^2}{(1+b\Pi)^4}$	$\dfrac{a\Pi^3}{(1+b\Pi + c\sqrt{\Pi})^5}$	C	$\dfrac{a\Pi}{(1+b\sqrt{\Pi})}$
II	Adsorbed oxygen, methane, carbon dioxide and water. Oxygen not dissociated and adsorbed on (i) dual sites (ii) single sites Surface reaction: $2O_2 1 + CH_4 1 \rightleftharpoons CO_2 1 + 2H_2O1$	i) $\dfrac{a\Pi^2}{(1+b\Pi)^4}$ ii) $\dfrac{a\Pi^2}{(1+b\Pi)^2}$	$\dfrac{a\Pi^3}{(1+b\Pi)^3}$	C	$\dfrac{a\sqrt{\Pi}}{(1+b\Pi)}$
III	Methane in gas phase, oxygen dissociated and adsorbed on dual sites or single sites (i) both products adsorbed (ii). One of the products adsorbed (iii) both the products in gas phase Surface reaction: $4O1 + CH_4 \rightleftharpoons CO_2 1 + 2H_2O1 + 1$	$c\Pi^2$	$\dfrac{a\Pi^3}{(1+b\sqrt{\Pi})^4}$	C	—
IV	Methane in gas phase, oxygen not dissociated and adsorbed on dual sites or single sites (i). One of the products adsorbed (ii) both the products in gas phase Surface reaction: $2O_2 1 + CH_4 \rightleftharpoons 2H_2O1 + CO_2$	$c\Pi^2$	$\dfrac{a\Pi^3}{(1+b\Pi)^2}$	C	—
V	Oxygen in gas phase, methane adsorbed molecularly (i) Carbon dioxide adsorbed (ii) Both products in gas phase $2O_2 + CH_4 1 \rightleftharpoons 2H_2O + CO_2 1$	—	$\dfrac{a\Pi^3}{(1+b\Pi)}$	C	$c\Pi$

TABLE 2(b) DESIGNATION OF INITIAL RATE EQUATIONS

INITIAL RATE EQUATION NO.	REACTIONS	INITIAL RATE EQUATION
(I)	II a (ii)	$a\pi^2/(1 + b\pi)^2$
(II)	II b	$a\pi^3/(1 + b\pi)^3$
(III)	IV b	$a\pi^3/(1 + b\pi)^2$
(IV)	V b	$a\pi^3/(1 + b\pi)$
(V)	II d	$a\pi/(1 + b\pi)$
(VI)	Ia, II a (i)	$a\pi^2/(1 + b\pi)^4$
(VII)	III b	$a\pi^3/(1 + b\sqrt{\pi})^4$
(VIII)	I d	$a\pi/(1 + b\sqrt{\pi})$
(IX)	I b	$a\pi^3/(1 + b\pi + c\sqrt{\pi})^5$
(X)	Ic, IIc, IIIc, IVc, Vc	c
(XI)	V d	$c\pi$
(XII)	IIIa, IVa	$c\pi^2$
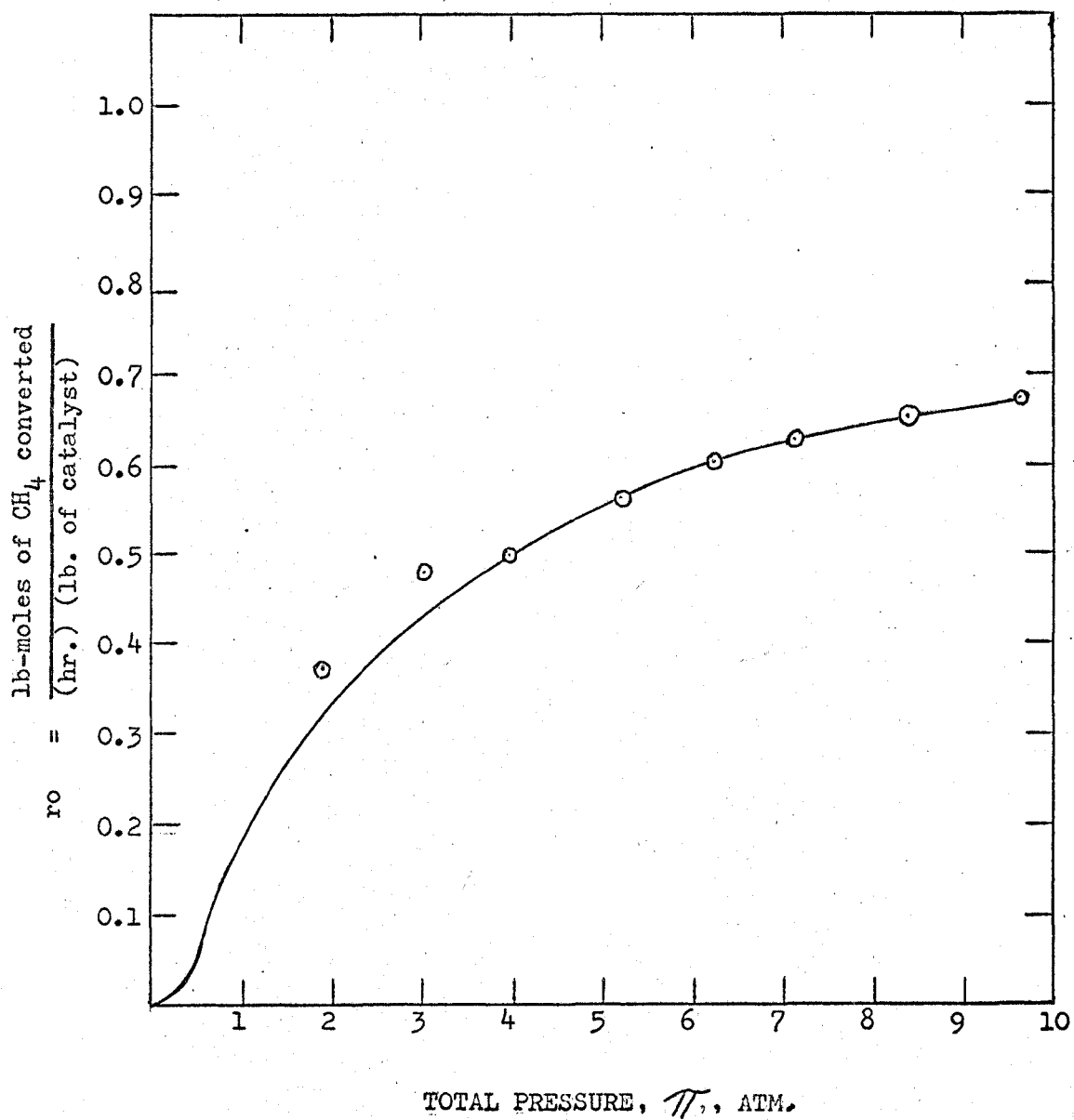
Fig. 3 INITIAL RATE OF REACTION VS TOTAL PRESSURE, 300°C
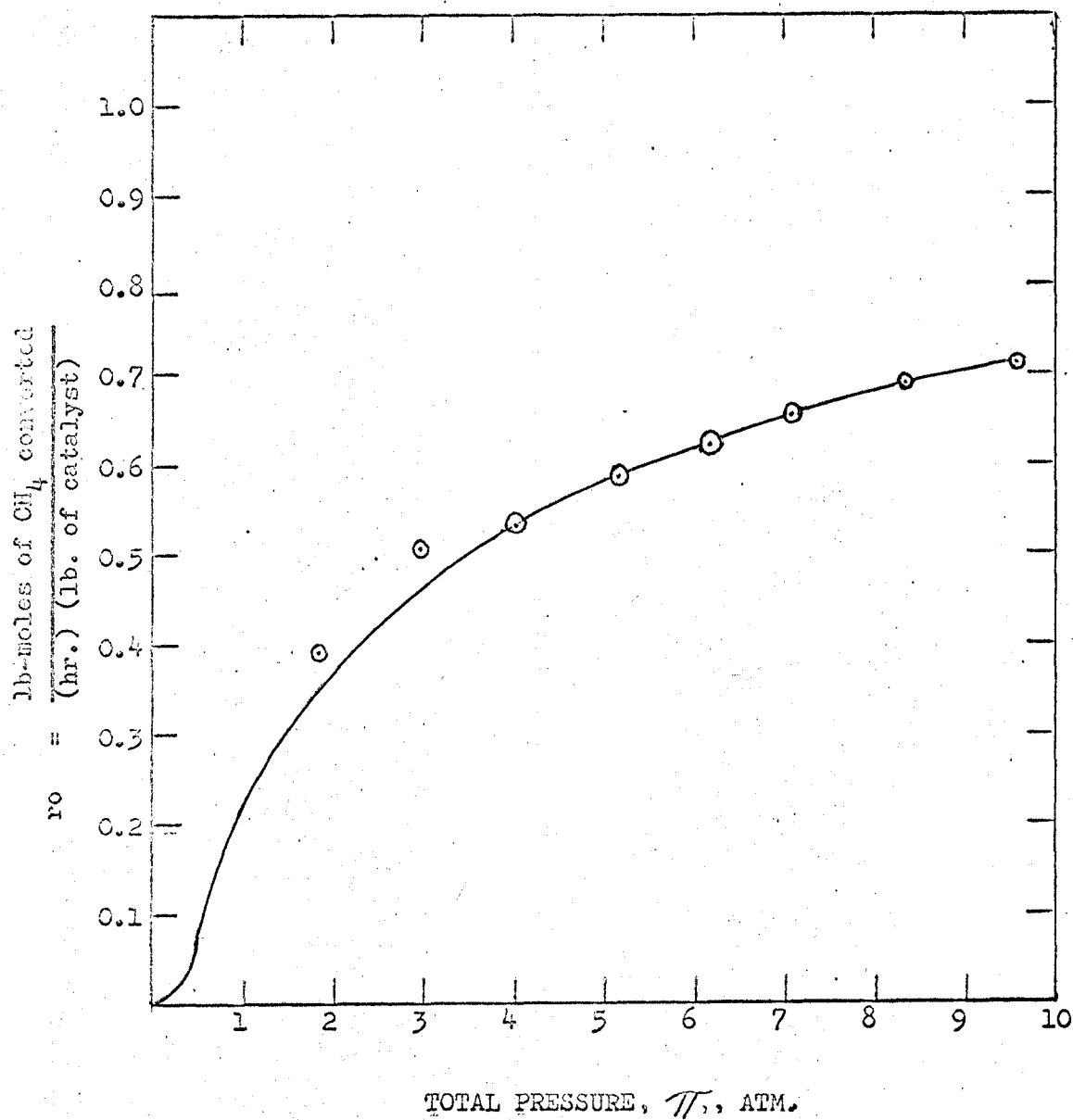
Fig. 4   INITIAL RATE OF REACTION VS TOTAL PRESSURE, 320°c
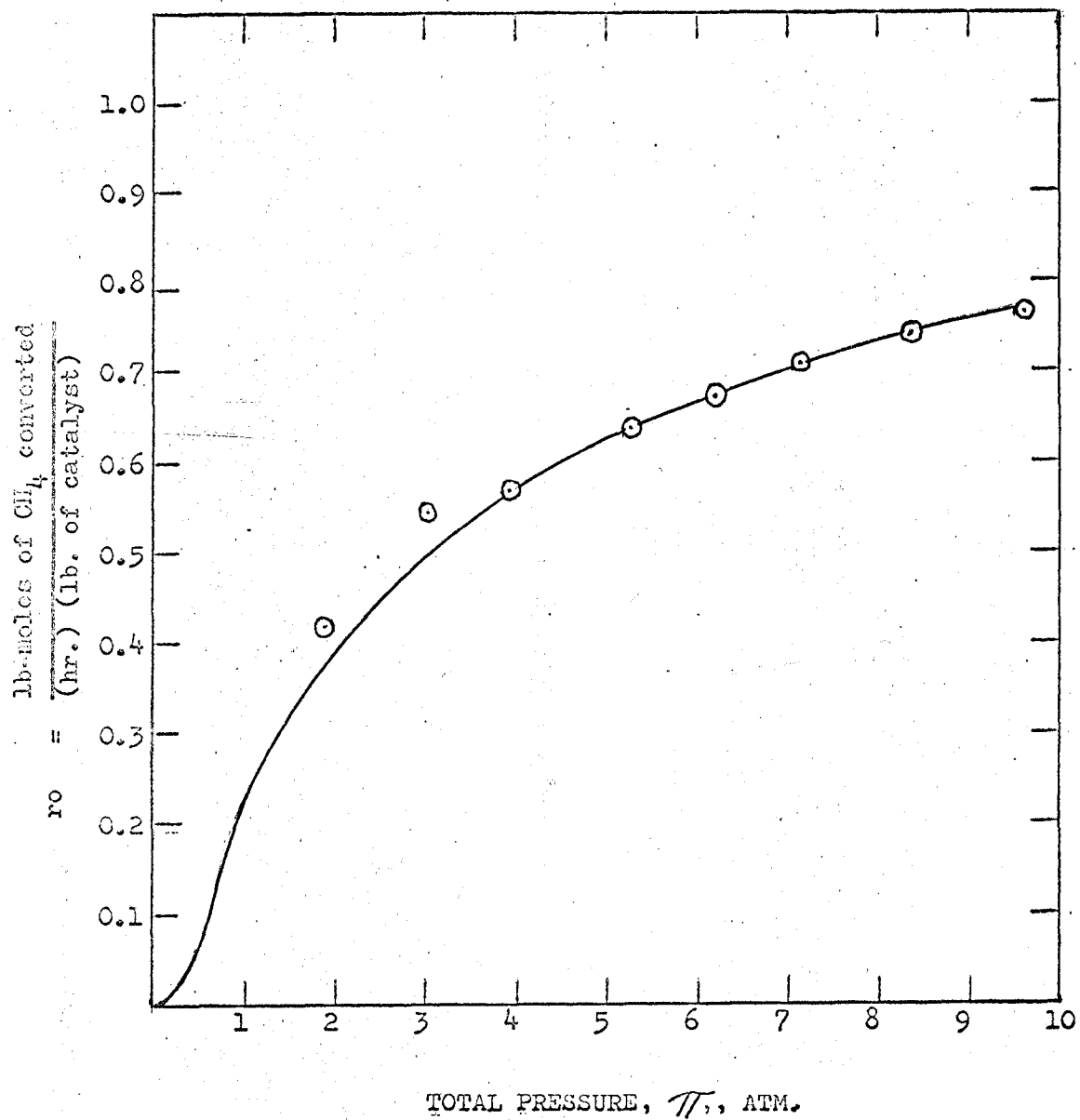
Fig. 5 INITIAL RATE OF REACTION VS TOTAL PRESSURE, 340°C

From these figures, the reaction mechanisms represented by equations ro C, $ro = C\pi$ and $ro = C\pi^2$ can be rejected, as their plots would be grossly different from the plots of figures 3, 4 and 5.

To examine the validity of other possibilities, coefficients of the remaining nine theoretical rate equations were estimated from the experimental data for three temperatures. The non-linear rate equations were transformed to linear equations by algebric manipulation. The coefficients of these linearised rate equations were estimated from the statistical methods of linear regression [25]. Considering the rate equation (I)

$$ro = a\pi^2 / (1 + b\pi)^2$$

Rearranging, this becomes

$$\frac{\pi}{(ro)^{\frac{1}{2}}} = \frac{1}{(a)^{\frac{1}{2}}} + \frac{b}{(a)^{\frac{1}{2}}} \pi$$

or, an expression of the type $Y = A + BX$

The regression coefficients A and B are given by

$$A = \frac{\Sigma X^2 \Sigma Y - \Sigma X \Sigma XY}{n \Sigma X^2 - (\Sigma X)^2}$$

$$B = \frac{n \Sigma XY - \Sigma X \Sigma Y}{n \Sigma X^2 - (\Sigma X)^2}$$

For an expression involving three coefficients, as in case of rate equation (IX)

$$ro = \frac{a\pi^3}{(1 + b\pi + C\sqrt{\pi})^5}$$

Rearranging, this becomes

$$\frac{\pi^{3/5}}{(ro)^{1/5}} = \frac{1}{(a)^{1/5}} + \frac{b}{(a)^{1/5}}\pi + \frac{C}{(a)^{1/5}}\sqrt{\pi}$$

or, an expression of the type $Z = B_0 + B_1 X + B_2 Y$

The coefficients B_0, B_1 and B_2 are given by three linear equations computed by the method of multiple regression[25]

$$\Sigma Z = n B_0 + B_1 \Sigma X + B_2 \Sigma Y$$
$$\Sigma XZ = B_0 \Sigma X + B_1 \Sigma X^2 + B_2 \Sigma XY$$
$$\Sigma YZ = B_0 \Sigma Y + B_1 \Sigma XY + B_2 \Sigma Y^2$$

The coefficients of nine equations were computed on an IBM-1620 computer. The programmes and results are given in Appendix V. The results are tabulated in Table 3.

From the nature of the plots in figures 3, 4 and 5, no shift in mechanism was noted over the temperature range 300, 320 and 340°C. Moreover, none of the figures 3, 4 and 5 showed a maxima. Therefore, the possibility of the reaction mechanism given by rate equation (VI), which exhibits a maxima for π max. $= \dfrac{1}{b}$, was rejected. The rate equations (III) and (IV) depicted negative regression coefficients, so these were also excluded as plausible mechanisms.

Rate equations I, II, V, VII, VIII and IX showed positive values for regression coefficients and remained possible mechanisms. These six possible equations were then subjected to goodness of fit criteria. Equations VII, VIII and IX showed a variation of more than 100% from experimental values of initial rates, thus eliminating them as possible mechanistic equations. Equations I, II and V showed an average variation of 1% from experimental data.

TABLE 3   REGRESSION COEFFICIENTS FOR LINEARISED RATE EQUATIONS

Rate Equation No.	Mechanism designation	Initial rate Equation	Regression Coefficients			VALUE OF REGRESSION COEFFICIENT								
						300°C			320°C			340°C		
			A	B	C	A	B	C	A	B	C	A	B	C
(I)	IIa (ii)	$r_0 = a\pi^2/(1+b\pi)^2$	$\frac{1}{a^{1/2}}$	$\frac{b}{a^{1/2}}$	-	1.0341	1.1199	-	1.0186	1.0889	-	0.9739	1.0456	-
(II)	IIb	$r_0 = a\pi^3/(1+b\pi)^3$	$\frac{1}{a^{2/3}}$	$\frac{b}{a^{1/3}}$	-	0.6227	1.0820	-	0.6196	1.0619	-	0.5995	1.0337	-
(III)	IVb	$r_0 = a\pi^3/(1+b\pi)^2$	$\frac{1}{a^{1/2}}$	$\frac{b}{a^{1/2}}$	-	-4.9805	4.1727	-	4.7978	4.0551	-	4.6422	3.8980	-
(IV)	Vb	$r_0 = a\pi^3/(1+b\pi)$	$\frac{1}{a}$	$\frac{b}{a}$	-	-471.924	164.676	-	-443.534	155.399	-	-411.557	143.724	-
(V)	IId	$r_0 = a\pi/(1+b\pi)$	$\frac{1}{a}$	$\frac{b}{a}$	-	2.8184	1.2083	-	2.6924	1.1434	-	2.4848	1.0523	-
(VI)	Ia, IIa(i)	$r_0 = a\pi^2/(1+b\pi)^4$	$\frac{1}{a^{1/4}}$	$\frac{b}{a^{1/4}}$	-	1.4481	0.2140	-	1.4292	0.2112	-	1.4021	0.2066	-
(VII)	IIIb	$r_0 = a\pi^3/(1+b\sqrt{\pi})^4$	$\frac{1}{a^{1/4}}$	$\frac{b}{a^{1/4}}$	-	1.2189	0.5118	-	1.2051	0.5048	-	1.1809	0.4944	-
(VIII)	Id	$r_0 = a\pi/(1+b\sqrt{\pi})$	$\frac{1}{a}$	$\frac{b}{a}$	-	2.8184	1.2083	-	2.6925	1.1434	-	2.4848	1.0523	-
(IX)	Ib	$r_0 = a\pi^3/(1+b\pi+c\sqrt{\pi})^5$	$\frac{1}{a^{1/5}}$	$\frac{b}{a^{1/5}}$	$\frac{c}{a^{1/5}}$	0.1007	0.0606	1.1385	0.1061	0.06126	1.1018	0.1151	0.06916	1.0936

As proposed by Yang and Hougen[22], the effect of feed composition upon rate of reaction was utilised to eliminate further implausible mechanisms. Plots of rate of reaction against methane percent in feed composition are given by figures 6, 7 and 8. Interpretation from these plots, rules out the survival of reaction mechanisms given by equations I and V. The plots of equations I and V would be entirely different from the plots of figures 6, 7 and 8.

Further more, as a check, values of initial rates from equations I, II and V were computed for the varying feed composition runs, by using the corresponding linear regression coefficients. The experimental data showed a variation of more than 100% from that predicted by equation I, about 25% from that predicted by equation V, only about 4% from that obtained by equation II.

Hence, from qualitative view points, equation II is the probable mechanism for methane oxidation. Also, from quantitative interpretations, it is the most accurate fit both for constant feed and varying feed composition runs.

Therefore, it is proposed that following is the rate controlling mechanism for methane oxidation.

" Oxygen and methane adsorbed on the catalyst surface, the surface is:

$$2 \ O_2 l + CH_4 l \rightleftharpoons 2 \ H_2 O l + CO_2 l$$
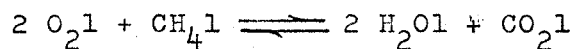
surface reaction is rate controlling ".
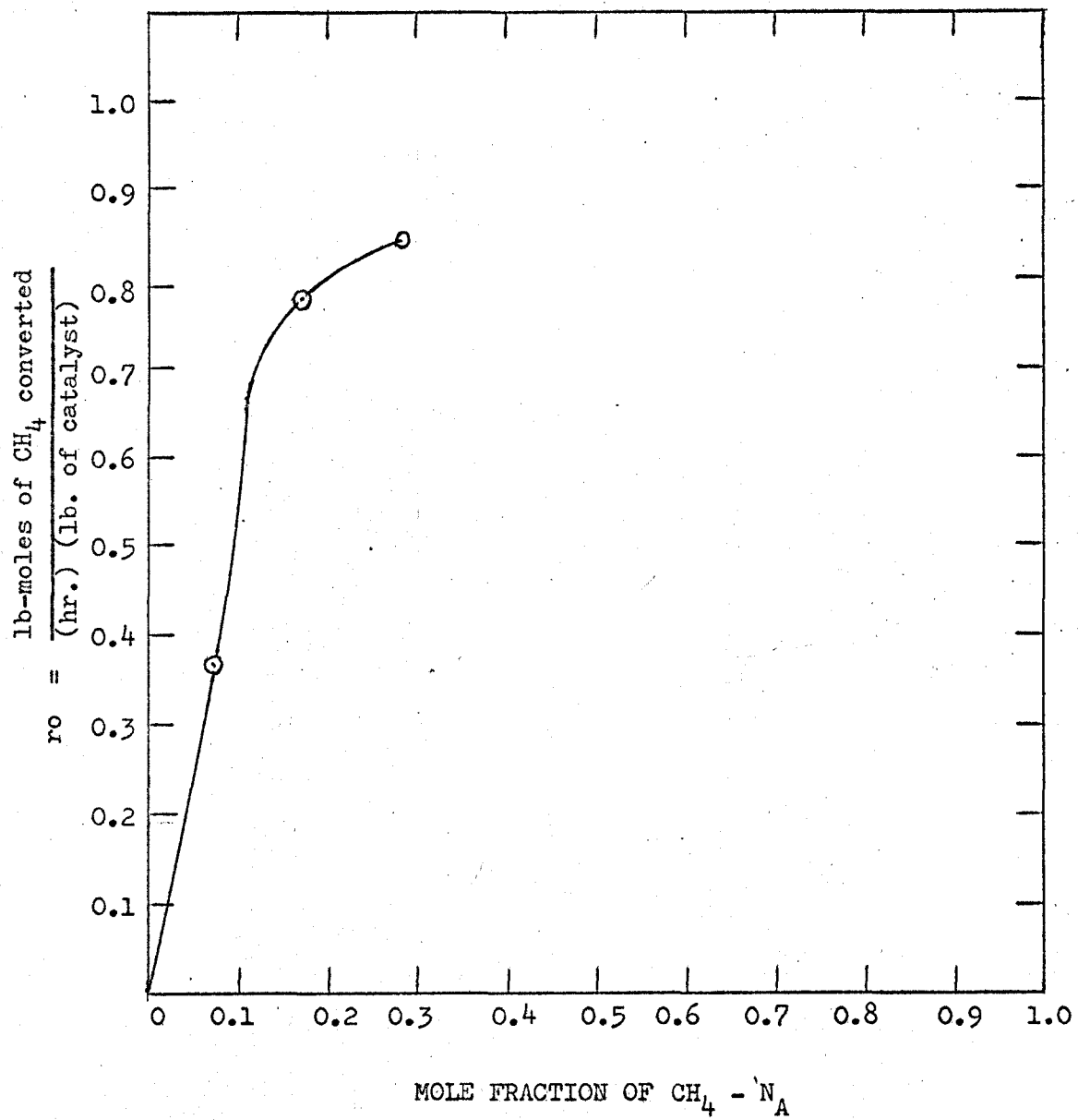
Fig. 6 INITIAL RATE OF REACTION VS FEED COMPOSITION, 300°C, 1.817 ATM.
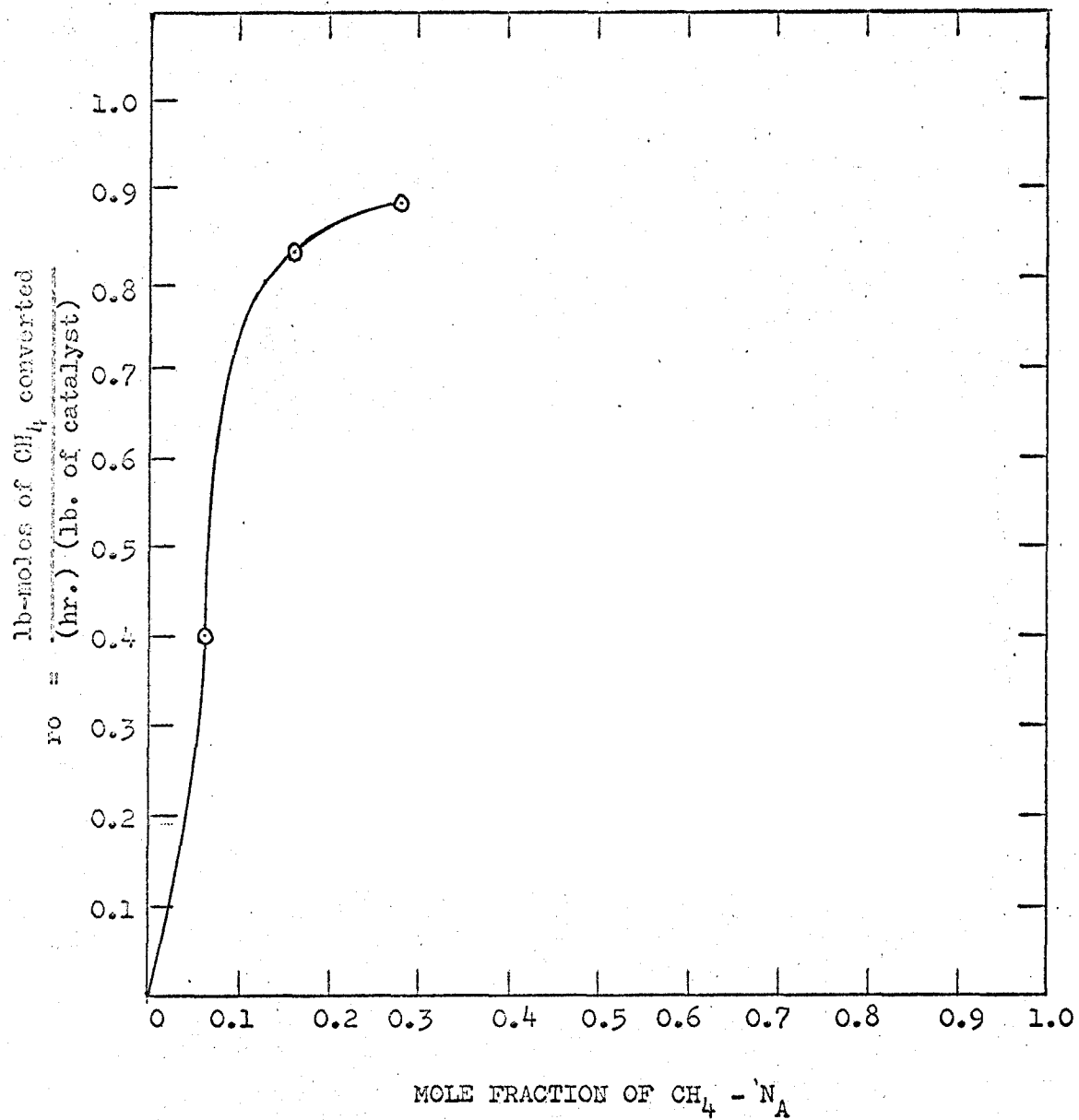
Fig. 7 INITIAL RATE OF REACTION VS FEED COMPOSITION, 320°C, 1.817 ATM.

MOLE FRACTION OF CH_4 - N_A
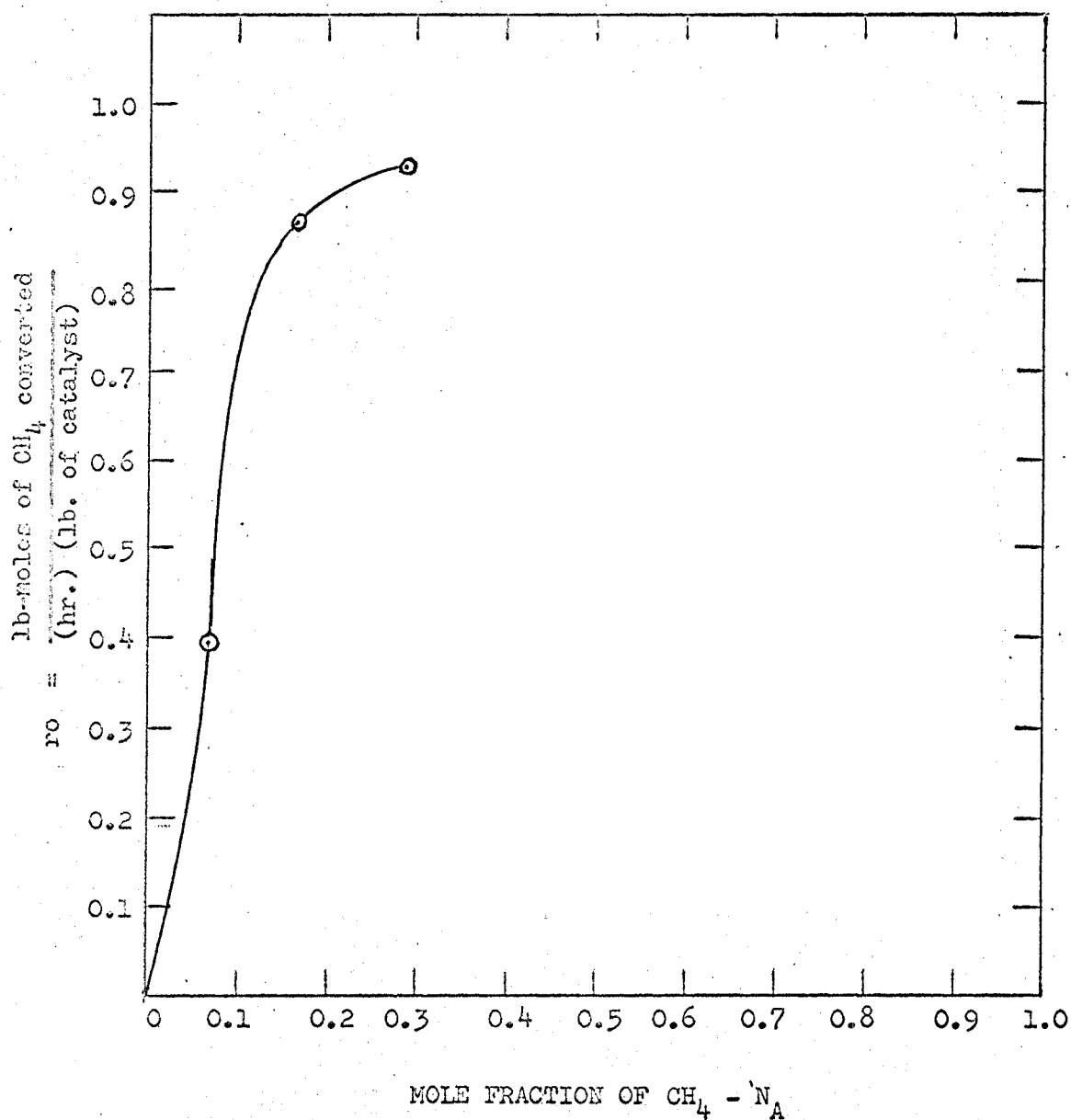
Fig. 8   INITIAL RATE OF REACTION VS FEED COMPOSITION, $340^{\circ}C$, 1.817 ATM.

The corresponding rate equation has the form

$$r = \frac{c\left[p_{CH_4}\, p^2_{O_2} - p^2_{H_2O}\, p_{CO_2}\, /\, K\right]}{\left[1 + K_{CH_4}\, p_{CH_4} + K_{O_2}\, p_{O_2} + K_{CO_2}\, p_{CO_2} + K_{H_2O}\, p_{H_2O}\right]^3}$$

the corresponding initial rate equation is:

$$r_o = a\, \pi^3 \,/\, (1 + b\pi)^3$$

at $300^\circ C \qquad r_o = 4.144\, \pi^3 /\, (1 + 1.737\,\pi)^3$

at $320^\circ C \qquad r_o = 4.206\, \pi^3 /\, (1 + 1.714\,\pi)^3$

at $340^\circ C \qquad r_o = 4.644\, \pi^3 /\, (1 + 1.723\,\pi)^3$

The initial rates computed from the proposed mechanistic equation and their variation from experimental data are given in Table 4.

Figures 9, 10 and 11 graphically illustrate the agreement of the computed rates with the observed reaction rate.

Mezaki's rate equation gives a deviation of about 17%, as compared to the deviation of 4% based on the equation arrived at in this investigation. Table 4-a gives the results based on proposed mechanistic equation as compared to results based on Mezaki's investigation.

Table - 4

Mechanistic Rate Equation Data

A. Constant Feed Composition runs at 300°C $a = 4.144$ $b = 1.737$

Run No.	Total Pressure Atm. (π)	Rate of Reaction Experimental	Rate of Reaction from $Ro = a\pi^3/(1 + b\pi)^3$	% Variation from Experimental value
I - 1	1.817	0.373	0.3463	+ 7.16
IV - 1	2.975	0.481	0.4652	+ 3.28
V - 1	3.925	0.503	0.5245	- 4.27
VI - 1	5.22	0.559	0.5833	- 4.34
VII - 1	6.24	0.594	0.6068	- 2.15
VIII - 1	7.13	0.624	0.6262	- 0.35
IX - 1	8.41	0.655	0.6494	+ 0.85
X - 1	9.70	0.671	0.6661	- 0.73

Average = 0.55%

B. Varying Feed Composition runs at 300°C, 1.817 Atm.; $a' = 71.38$, $b' = 1.737$

Run No.	Mole Fraction of Methane in Feed	Rate of Reaction Experimental	Rate of Reaction from $Ro = \dfrac{a'\left[p_{CH_4}\right]^2\left[p_{O_2}\right]}{\left[1 + b'(p_{CH_4} + p_{O_2})\right]^3}$	% Variation from Experimental value
I - 1	0.06669	0.373	0.3463	+ 7.16
II - 1	0.1517	0.796	0.723	+ 9.17
III - 1	0.2806	0.842	0.863	- 2.49

Average = 4.61%

Table 4 - (Cont'd)   Mechanistic Rate Equation Data

A. Constant Feed Composition Runs at 320°C $a = 4.206$ $b = 1.714$

Run No.	Total Pressure Atm. (π)	Rate of Reaction Experimental	Rate of Reaction from $Ro = a\pi^3/(1 + b\pi)^3$	% variation from Experimental value
I - 2	1.817	0.398	0.362	+ 9.04
IV - 2	2.975	0.511	0.488	+ 4.50
V - 2	3.925	0.531	0.5511	- 3.78
VI - 2	5.22	0.581	0.607	- 4.47
VII - 2	6.24	0.616	0.638	- 3.57
VIII - 2	7.13	0.658	0.660	- 0.30
IX - 2	8.41	0.694	0.6831	- 1.57
X - 2	9.70	0.712	0.7009	- 1.56

Average = 0.20%

B. Varying Feed Composition at 320°C, 1.817 Atm.; $a' = 71.52$ $b' = 1.714$

Run No.	Mole Fraction of Methane in feed	Rate of Reaction Experimental	Rate of Reaction from $Ro = a'\dfrac{\left[p_{CH_4}\right]\left[p_{O_2}\right]^2}{\left[1 + p_{CH_4} + p_{O_2}\right]^3}$	% variation from Experimental value
I - 2	0.06765	0.398	0.362	+ 9.04
II - 2	0.1529	0.836	0.775	+ 7.29
III - 2	0.2801	0.884	0.894	- 1.13

Average = 5.06%

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Table 4 - (Cont'd)   Mechanistic Rate Equation Data

A. Constant Feed Composition runs at 340°C   a = 4.644   b = 1.723

Run No.	Total Pressure Atm. (π)	Rate of Reaction Experimental	Rate of Reaction from $R_o = a\pi^3/(1 + b\pi)^3$	% variation from Experimental value
I - 3	1.817	0.421	0.3948	+ 6.22
IV - 3	2.975	0.552	0.5319	+ 3.64
V - 3	3.925	0.580	0.6003	− 3.50
VI - 3	5.22	0.640	0.6615	− 3.35
VII - 3	6.24	0.673	0.6956	− 3.36
VIII - 3	7.13	0.720	0.7188	+ 0.16
IX - 3	8.41	0.745	0.7433	+ 0.228
X - 3	9.70	0.771	0.7631	+ 1.02

Average = 0.13%

B. Varying Feed Composition runs at 340°C, 1.817 Atm.   a' = 78.64   b' = 1.723

$$R_o = \frac{a'\left[\dfrac{p_{CH_4}}{p_{O_2}}\right]^2}{\left[1 + b'\left(p_{CH_4} + p_{O_2}\right)\right]^3}$$

Run No.	Mole Fraction of Methane in Feed	Rate of Reaction Experimental	Rate of Reaction from (above)	% variation from Experimental value
I - 3	0.06800	0.421	0.3948	+ 6.22
II - 3	0.1537	0.882	0.829	+ 6.00
III - 3	0.2811	0.932	0.9732	− 4.42

Average = 2.60%
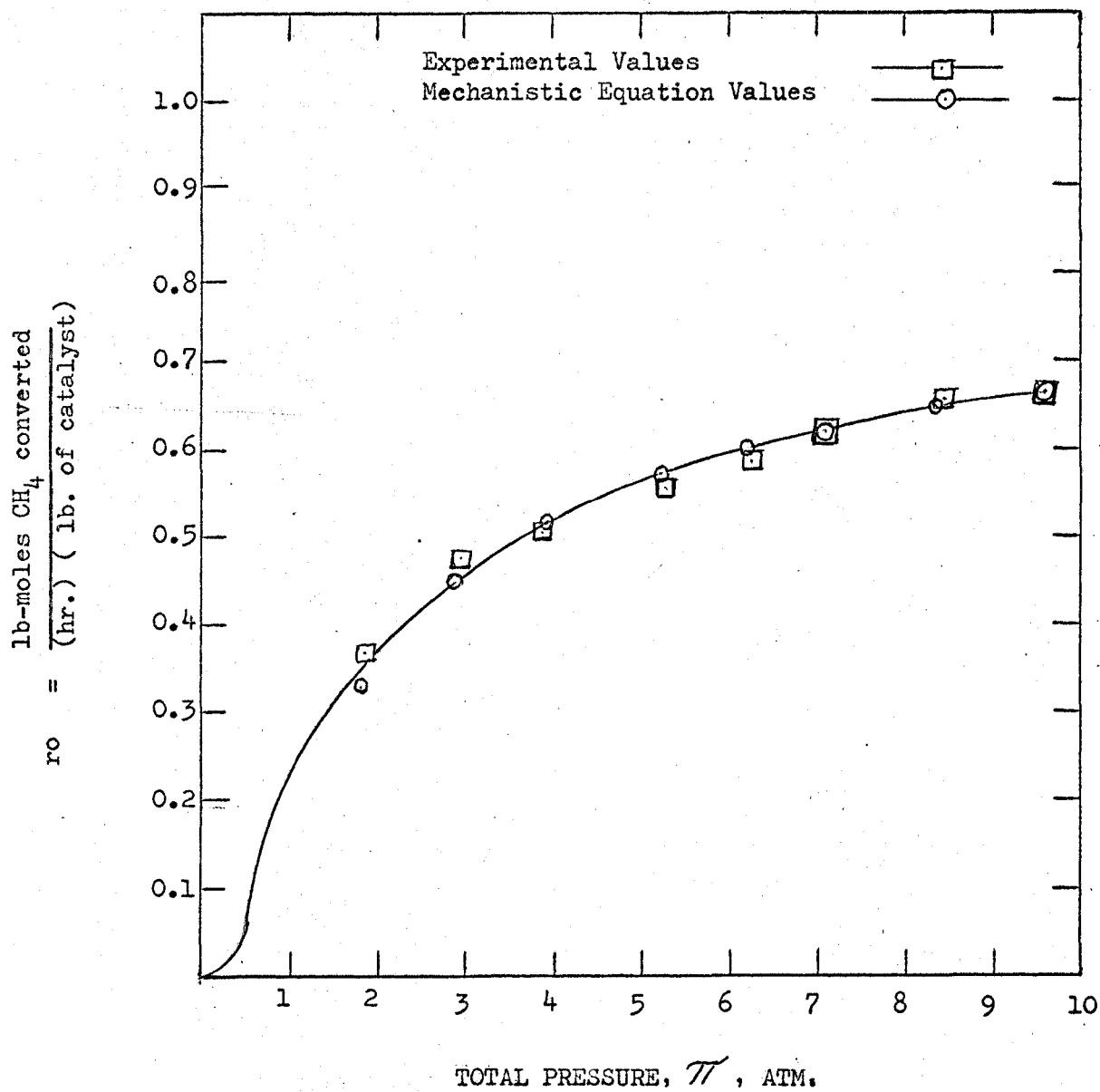
Fig. 9 INITIAL RATE OF REACTION FROM MECHANISTIC EQUATION, 300°C
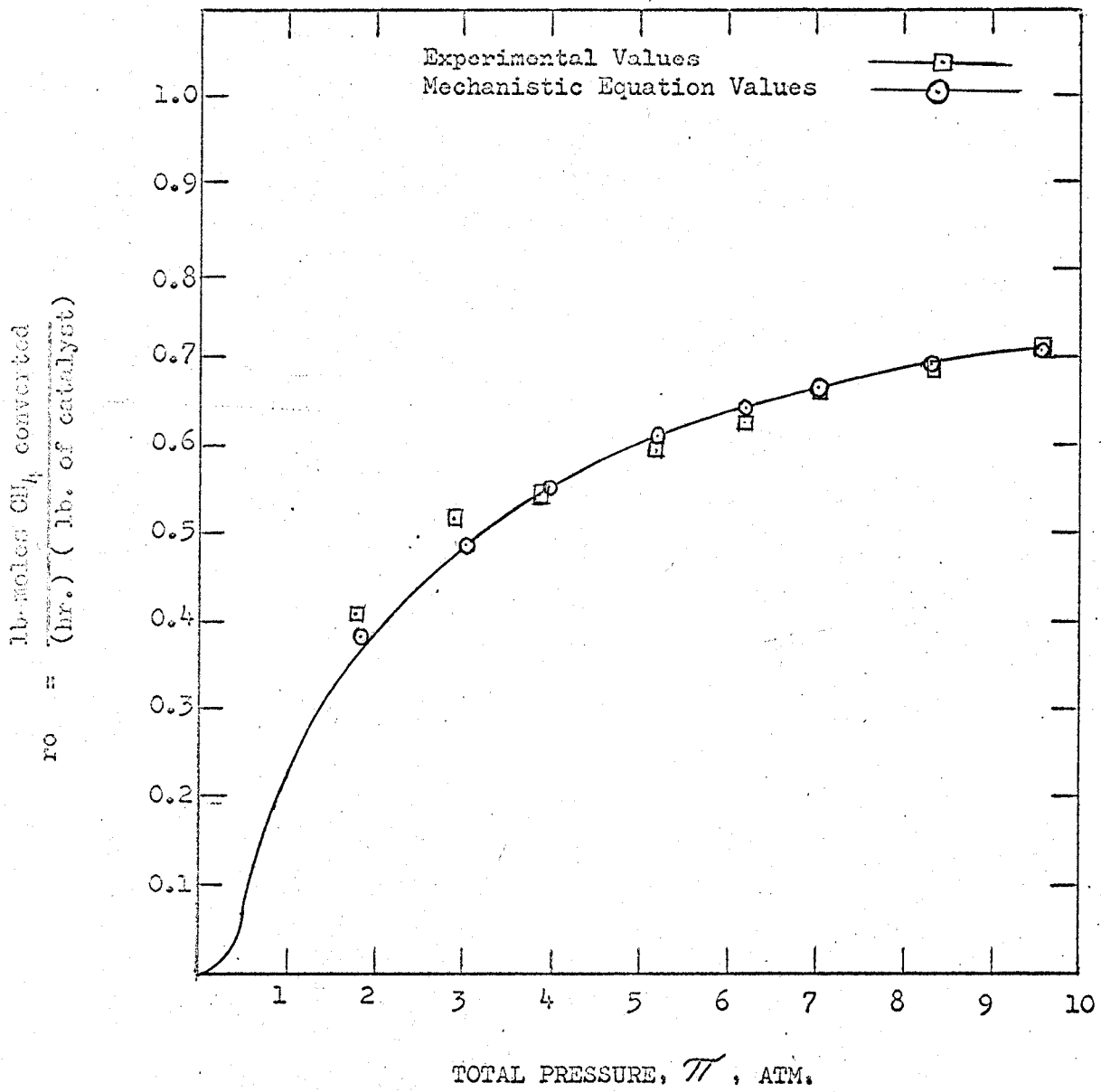
Fig. 10 INITIAL RATE OF REACTION FROM MECHANISTIC EQUATION, 320°C
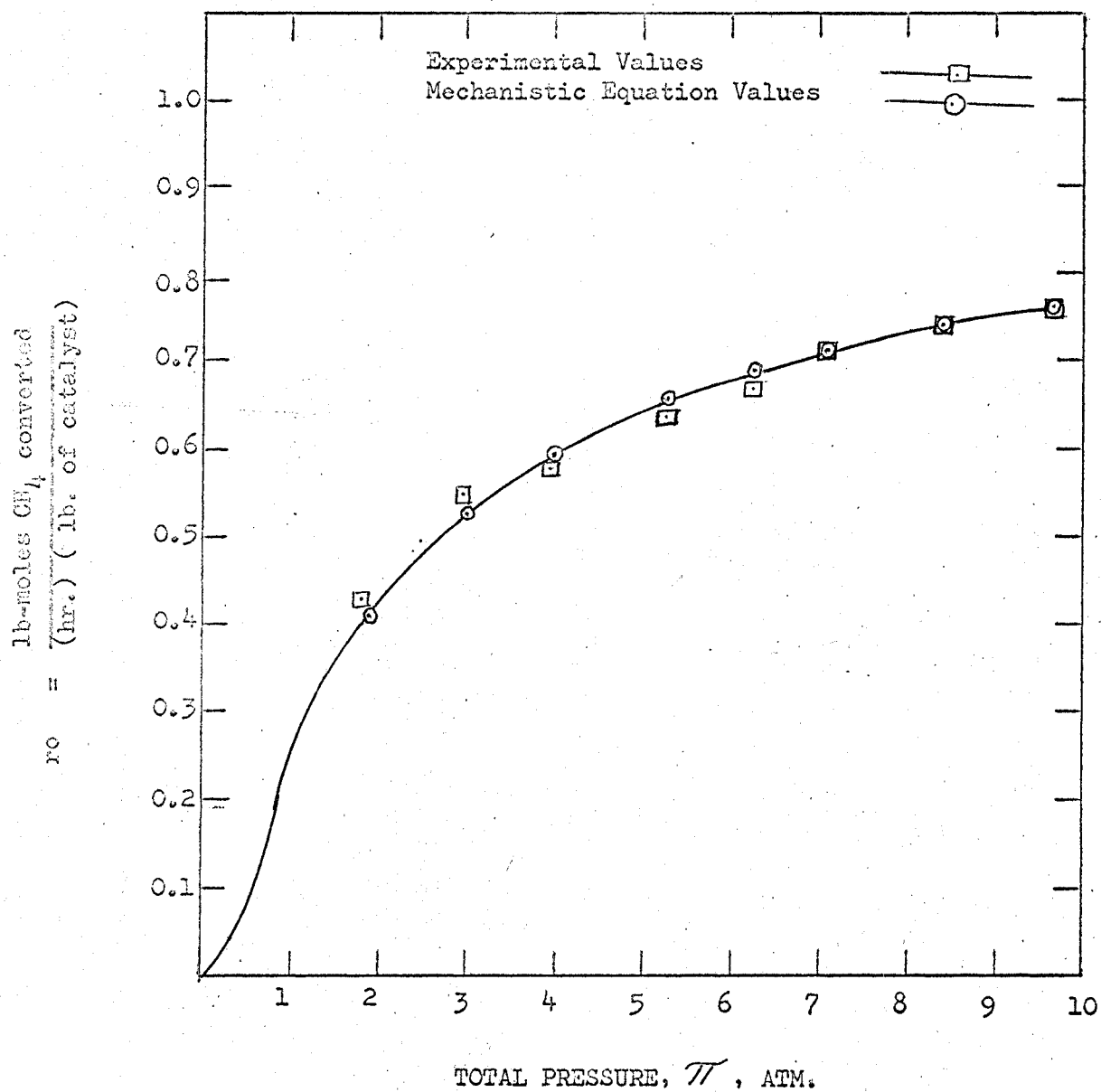
Fig. 11 INITIAL RATE OF REACTION FROM MECHANISTIC EQUATION, $340^\circ C$

Table 4-a

Results of Present Investigation VS Mezaki's Investigation

Temperature	Run No.	ro Experimental Value	Rate of Reaction from $R_o = \dfrac{a'[p_{CH_4}][p_{O_2}]^2}{[1+b'(p_{CH_4}+p_{O_2})]^3}$	% Variation of Ro from Experimental Value	Rate of Reaction from $R_o = \dfrac{a''[p_{CH_4}][p_{O_2}]^2}{[1+b''(p_{O_2})]^3}$	% Variation of Ro from Experimental Value
300°C	I - 1	0.373	0.3463	+ 7.16	0.296	- 20.8
	II - 1	0.796	0.723	+ 9.17	0.616	- 22.6
	III - 1	0.842	0.863	- 2.49	0.736	- 12.6
				Average 4.61%		Average 15.35%
320°C	I - 2	0.398	0.362	+ 9.04	0.309	- 22.4
	II - 2	0.836	0.836	+ 7.29	0.651	- 22.1
	III - 2	0.884	0.884	- 1.13	0.765	- 13.45
				Average 5.06%		Average 19.32%
340°C	I - 3	0.421	0.421	+ 6.22	0.336	- 20.2
	II - 3	0.882	0.882	+ 6.00	0.709	- 19.6
	III - 3	0.932	0.932	+ 4.42	0.831	- 10.8
				Average 2.60%		Average 16.87%

EMPIRICAL APPROACH

From the reactor design point of view, it is of interest to subject the oxidation data to a power law model. The following rate equation was used to find the empirical power law coefficients.

$$\text{Rate} = k \left[C_{CH_4} \right]^m \left[C_{O_2} \right]^n \tag{21}$$

Empirical coefficients for equation (21) were found by multiple regression technique[25]. The computer programme and results are given in Appendix V. The values of empirical coefficients are given in table 5. The average order of reaction was found to be 0.62.

The initial rates computed from the empirical equation (21), and their variation from experimental data, are given in table 5. The average deviation was found to be less than 1%. Figures 12, 13 and 14 graphically illustrate the agreement of computed rates with the observed reaction rates.

The proposed empirical rate equations have the form:

at $300^{\circ}C$, $r_o = 2.528 \left[C_{CH_4} \right]^{0.0763} \left[C_{O_2} \right]^{0.5429}$

at $320^{\circ}C$, $r_o = 2.635 \left[C_{CH_4} \right]^{0.06726} \left[C_{O_2} \right]^{0.5518}$

at $340^{\circ}C$, $r_o = 2.772 \left[C_{CH_4} \right]^{0.05932} \left[C_{O_2} \right]^{0.5613}$

Table - 5

Empirical Rate Equation Date (300°C)

$m = 0.0763$ $n = 0.5429$ $k = 2.528$

Run No.	Concentration of methane lb-moles C_{CH_4}	Concentration of oxygen lb-moles C_{O_2}	Rate of reaction Experimental	Rate of reaction from $r = k[C_{CH_4}]^m[C_{O_2}]^n$	% Variation from Experimental value
I - 1	0.00474	0.0664	0.373	0.3856	- 3.38
II - 1*	0.01179	0.0664	0.796	0.8140	- 2.37
III - 1*	0.0251	0.0664	0.842	0.8557	- 1.63
IV - 1	0.00628	0.0906	0.481	0.4663	+ 3.06
V - 1	0.007125	0.1029	0.503	0.5044	- 0.28
VI - 1	0.008160	0.1173	0.559	0.5473	+ 2.09
VII - 1	0.008800	0.1270	0.594	0.5748	+ 4.91
VIII - 1	0.009610	0.1392	0.624	0.6081	+ 2.55
IX - 1	0.01117	0.1610	0.655	0.6658	- 1.65
X - 1	0.01231	0.1753	0.671	0.7009	- 4.45

Average - 0.11%

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Table - 5 (Cont'd)

Empirical Rate Equation Data (320°C)

$m = 0.06726 \qquad n = 0.5518 \qquad k = 2.635$

Run No.	Concentration of methane lb-moles c_{CH_4}	Concentration of oxygen lb-moles c_{O_2}	Rate of reaction Experimental	Rate of reaction from $r_0 = \left[c_{CH_4}\right]^m \left[c_{O_2}\right]^n$	% Variation from Experimental value
I - 2	0.00481	0.0664	0.398	0.4121	- 3.54
II - 2*	0.01177	0.0664	0.836	0.8495	- 1.62
III - 2*	0.02497	0.0664	0.884	0.8677	+ 1.85
IV - 2	0.00632	0.0906	0.511	0.4981	+ 2.52
V - 2	0.00724	0.01029	0.531	0.5394	- 1.58
VI - 2	0.00812	0.01173	0.581	0.5843	- 0.56
VII - 2	0.00877	0.01270	0.616	0.6138	+ 0.36
VIII - 2	0.00958	0.01392	0.658	0.6494	+ 1.31
IX - 2	0.01123	0.01610	0.694	0.7114	+ 2.51
X - 2	0.01225	0.01753	0.712	0.7498	- 5.30

Average - 0.91%

Table - 5 (Cont'd)

Empirical Rate Equation Data (340°C)

$m = 0.05932 \qquad n = 0.5613 \qquad k = 2.772$

Run No.	Concentration of methane lb-moles C_{CH_4}	Concentration of oxygen lb-moles C_{O_2}	Rate of reaction Experimental	Rate of reaction from $r = k\left[C_{CH_4}\right]^m \left[C_{O_2}\right]^n$	% deviation from Experimental value
I - 3	0.00484	0.0664	0.4210	0.4512	- 7.17
II - 3 *	0.01175	0.0664	0.882	0.8607	- 2.42
III - 3 *	0.02531	0.0664	0.932	0.9473	+ 1.65
IV - 3	0.00639	0.0906	0.552	0.5321	+ 3.60
V - 3	0.00720	0.1029	0.580	0.5772	+ 0.48
VI - 3	0.00819	0.1173	0.640	0.6261	+ 2.17
VII - 3	0.00886	0.1270	0.673	0.6579	+ 2.24
VIII - 3	0.00971	0.1392	0.720	0.6961	+ 3.32
IX - 3	0.0112	0.1610	0.745	0.7619	- 2.27
X - 3	0.01232	0.1753	0.771	0.8037	- 4.24

Average - 0.26%

* Data of these runs not used in plots of initial rate against total pressure, at constant feed composition. These runs have different feed composition
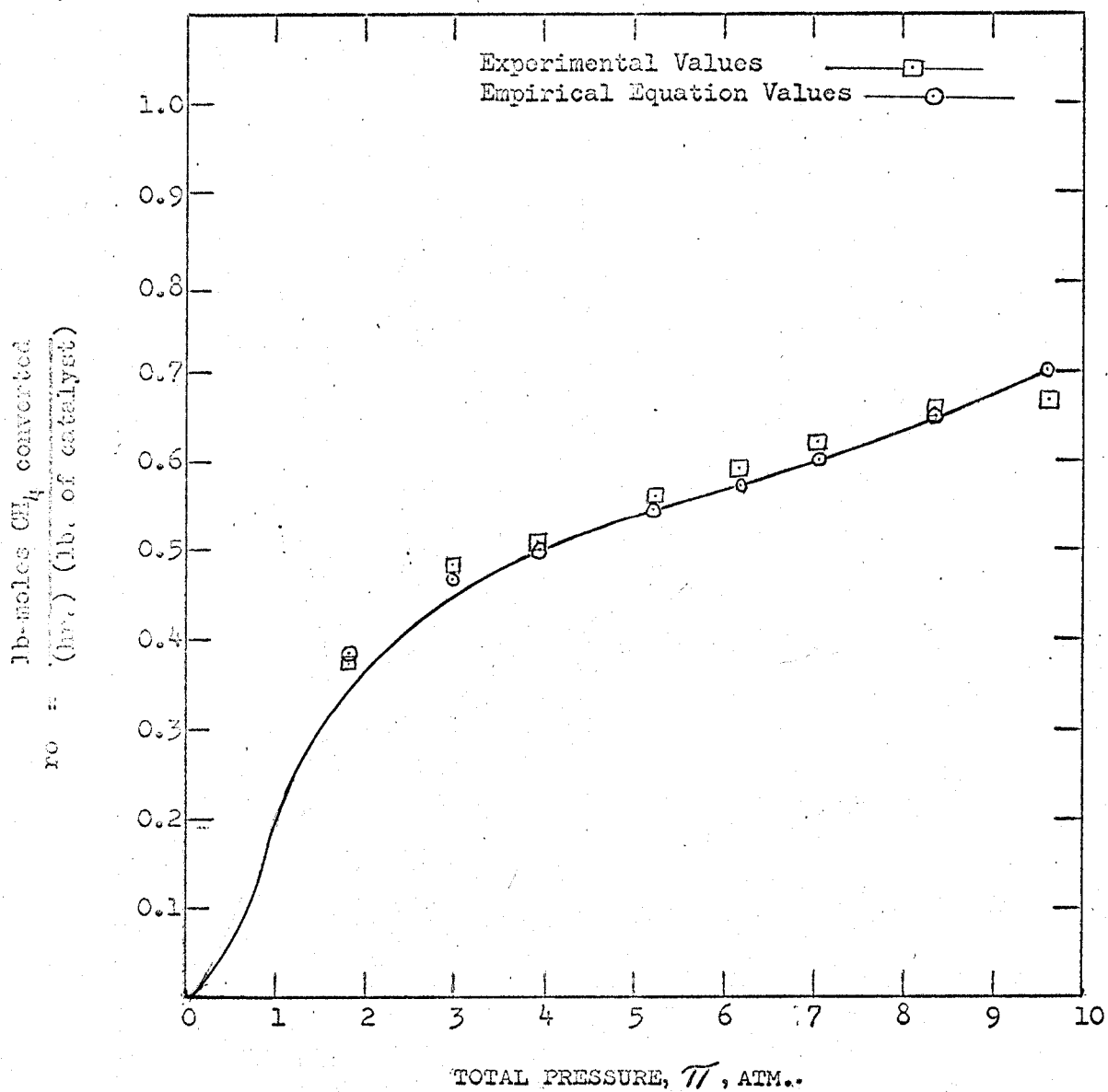
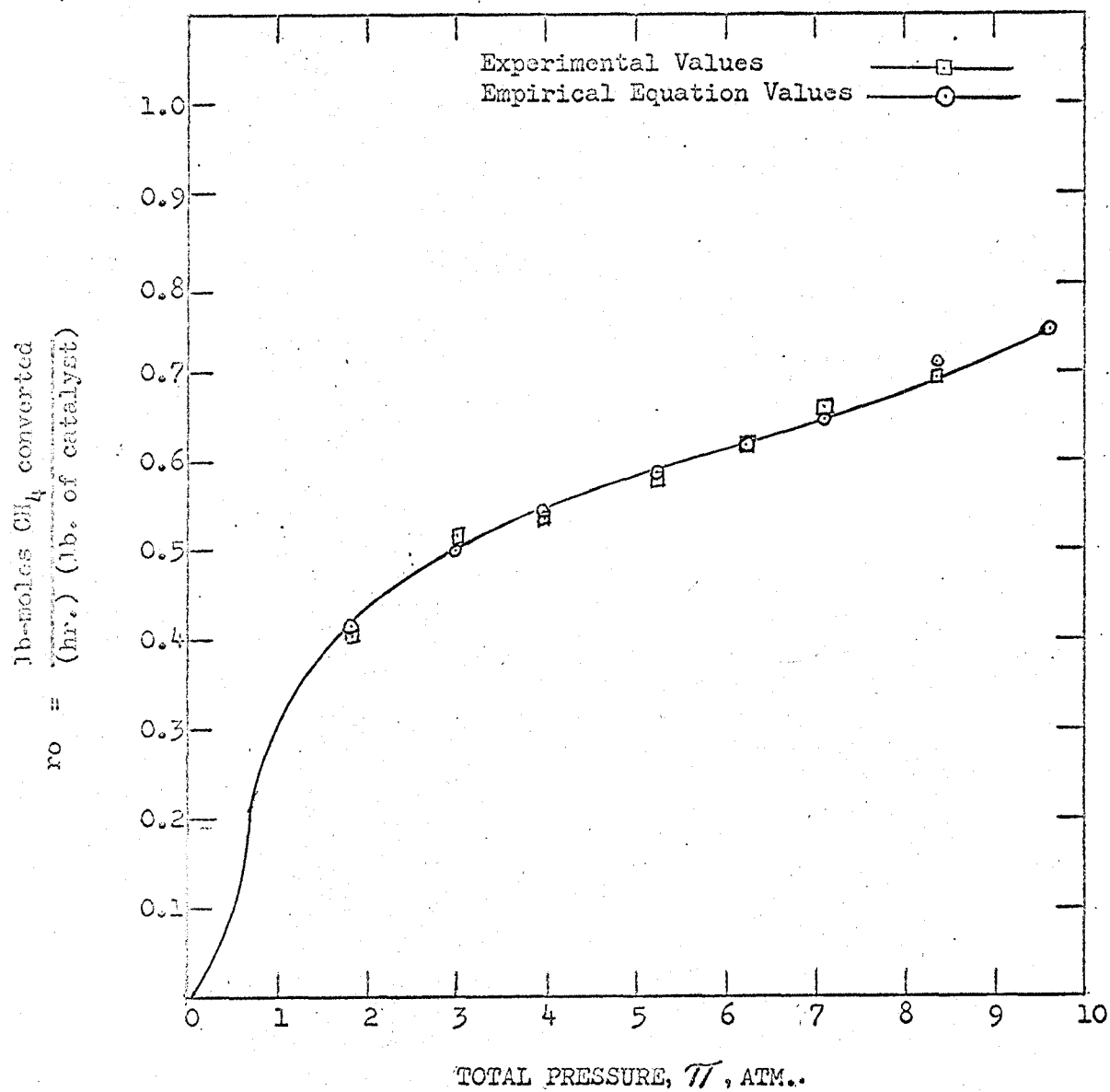Fig. 12 INITIAL RATE OF REACTION FROM EMPIRICAL EQUATION, 300°C

Fig. 13   INITIAL RATE OF REACTION FROM EMPIRICAL EQUATION, 320°C
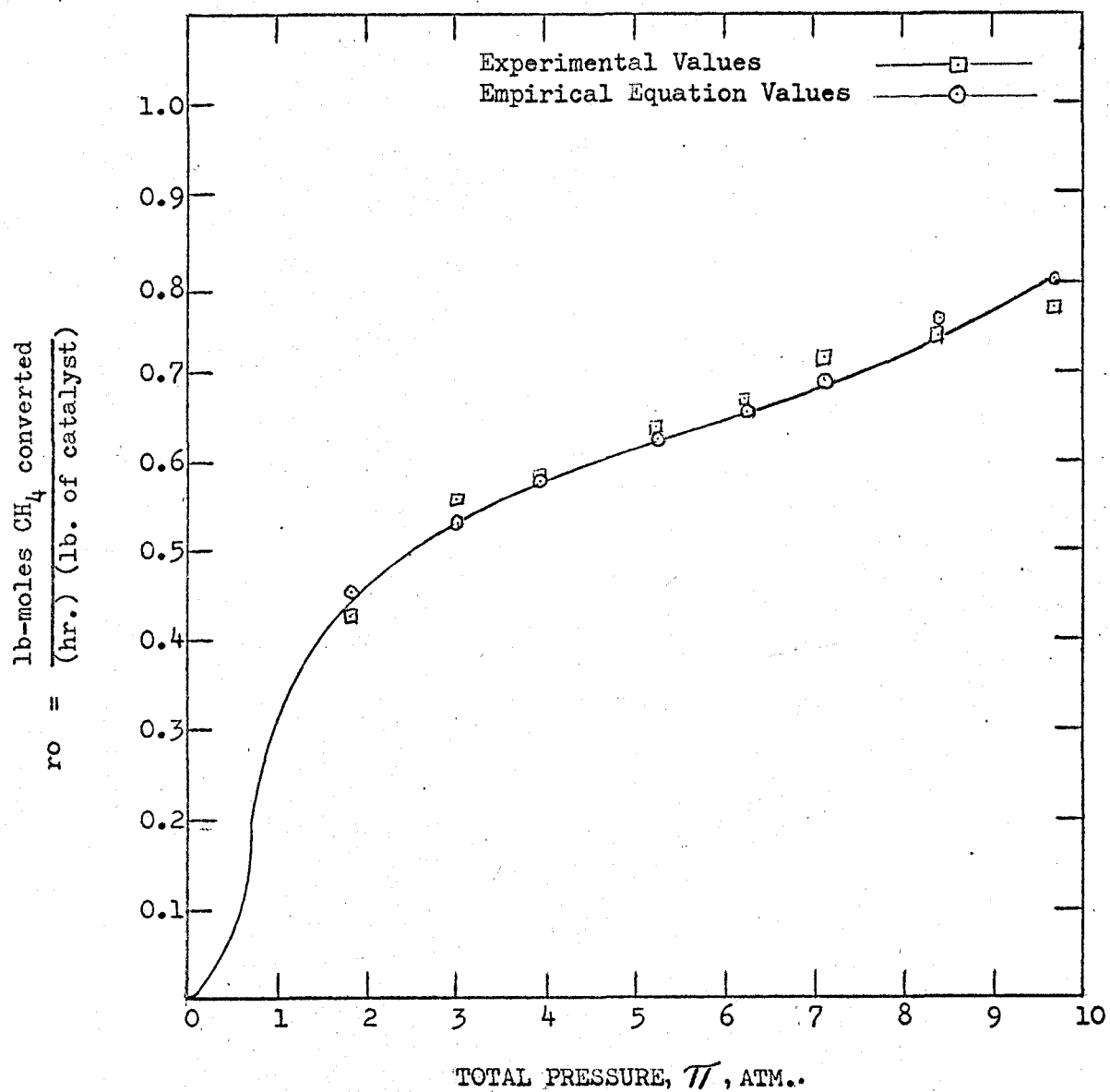
Fig. 14 INITIAL RATE OF REACTION FROM EMPIRICAL EQUATION, $340°C$

CHAPTER VII

CONCLUSIONS

The mechanism for the catalytic oxidation of methane has been established experimentally by applying the inital rate approach.

The plots of initial rate against total pressure gave useful qualitative information and thus some implausible mechanisms could be rejected. The determination of linearised regression coefficients and application of the criteria of best fit was then used to reject mechanisms showing wide variation from experimental data. Negative coefficients for some rate mechanisms also helped to eliminate them as possible mechanisms.

The data of initial rates at varying pressures and constant feed composition was not sufficient to establish the controlling mechanism. Plots of initial rate against varying feed composition served as a very useful tool in finding the controlling mechanism. The experimental results showed that there is no shift in mechanism within the range of operating temperature and other operating conditions. The proposed reaction mechanism is as follows:

"Oxygen not dissociated and adsorbed molecularly on dual or single sites, methane adsorbed, carbon dioxide and water adsorbed, surface reaction rate controlling."

The rate equation based on the mechanism as
deduced in the present investigation is only in
partial agreement with the mechanistic equation ar-
rived at by Mezaki[19].

NOMENCLATURE

a, b, c	constants in initial rate equations
A, B, C	constants for linearised rate equations
a_i	activity coefficient for the species i
a_p	surface area per single catalyst pellet
a_m	surface area of pellets per unit mass
A_p	area of constriction
C_p	heat capacity at constant pressure
C_r	coefficient of discharge for a flowmeter
C_v	heat capacity at constant volume
$D_A m$	mean diffusivity of component A in a gas mixture
D_p	effective particle diameter
F	feed rate, moles per unit time
G	mass velocity $lb/(hr.)(ft^2)$
ΔH_A	molar heat of reaction of component A
k_{sr}	reaction velocity constant where surface reaction is rate controlling
k_i	reaction velocity constant where adsorption of component i is controlling
K	overall equilibrium constant
K_i	odsorption equilibrium constant for component i
L	total number of available active sites
m, n	constants in empirical rate equation
p_i	partial pressure of component i
p_f	pressure factor
p_c	critical pressure
p_r	reduced pressure
r	rate of reaction, lb moles/(hr.)(lb. of catalyst)

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ro	initial rate of reaction' referred to methane
R	gas constant
Re	Reynolds number
T	absolute temperature
t	temperature, C^o
Tc	critical temperature, K^o
W	flow rate, lb./hr.
w	mass of catalyst
Xi	fraction of i converted

Greek

μ	visocity
π	total pressure, atm.
ρ	density
α', α''	constants

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        Methods for Engineers and Scientists". International
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APPENDIX I

Tables 6, 7, 8, 9, 10 and 11

Table 6[6]

Composition of Auto Exhaust Gases under Different
Operating Conditions - I

Operating Condition	Hydrocarbons (%)	Carbon Monoxide (%)
Idling	0.05 - 0.1	4.6
Accelrating	0.005 - 0.05	0.6
Cruising	0.02 - 0.03	1.4
Decelerating	0.4 - 1.2	2.4

Table 7[(6)]

Composition of Auto Exhaust Gases under Different
Operating Conditions - III

Constituent (Volume %, dry basis)	Operating Condition	
	Idling	Cruise 30-50m.p.h.
Hydrocarbons C_1 and higher	0.08 - 0.15	0.02 - 0.08
Carbon Dioxide	5 - 10	3 - 14
Carbon Monoxide	3 - 10	0.2 - 5
Hydrogen	0 - 4	0 - 2
Oxygen	0 - 2	0 - 2
Nitrogen	78 - 85	78 - 85

Water vapour generally varies from 5 - 15%

Table 8[6]

Composition of Auto Exhaust Gases under Different
Operating Conditions - II

Constituent	Concentration p.p.m.
Methane	63 - 292
Ethane	15 - 28
Ethylene	114 - 130
Acetylene	41 - 196
Propylene and n-Butane	35 - 83
Butene	0 - 61

Car Condition 30 m.p.h.

Table 9

Correlation between Space Velocity and Conversion
of Methane[13]

Space Velocity (hr.$^{-1}$)	Conversion (%)
4,000	100
6,000	100
8,000	92
10,000	88
20,000	61

Table 10

The Analysis of C.P. Grade Methane

Constituent	Percentage
Methane	99.05
Ethane	0.12
Carbon Dioxide	0.20
Nitrogen	0.60
Propane	0.03
Oxygen	50 p.p.m.

Table 11

Operating Data for Chromatographic Analysis

Column Bath Temperature	$60^{\circ}C$
Injector Bath Temperature	$110^{\circ}C$
Detector Bath Temperature	$110^{\circ}C$
Detector Filament Current	250 milliammeters
Helium Gas Flow-rate	0.25 cc. per second

APPENDIX II

Calibration Curves
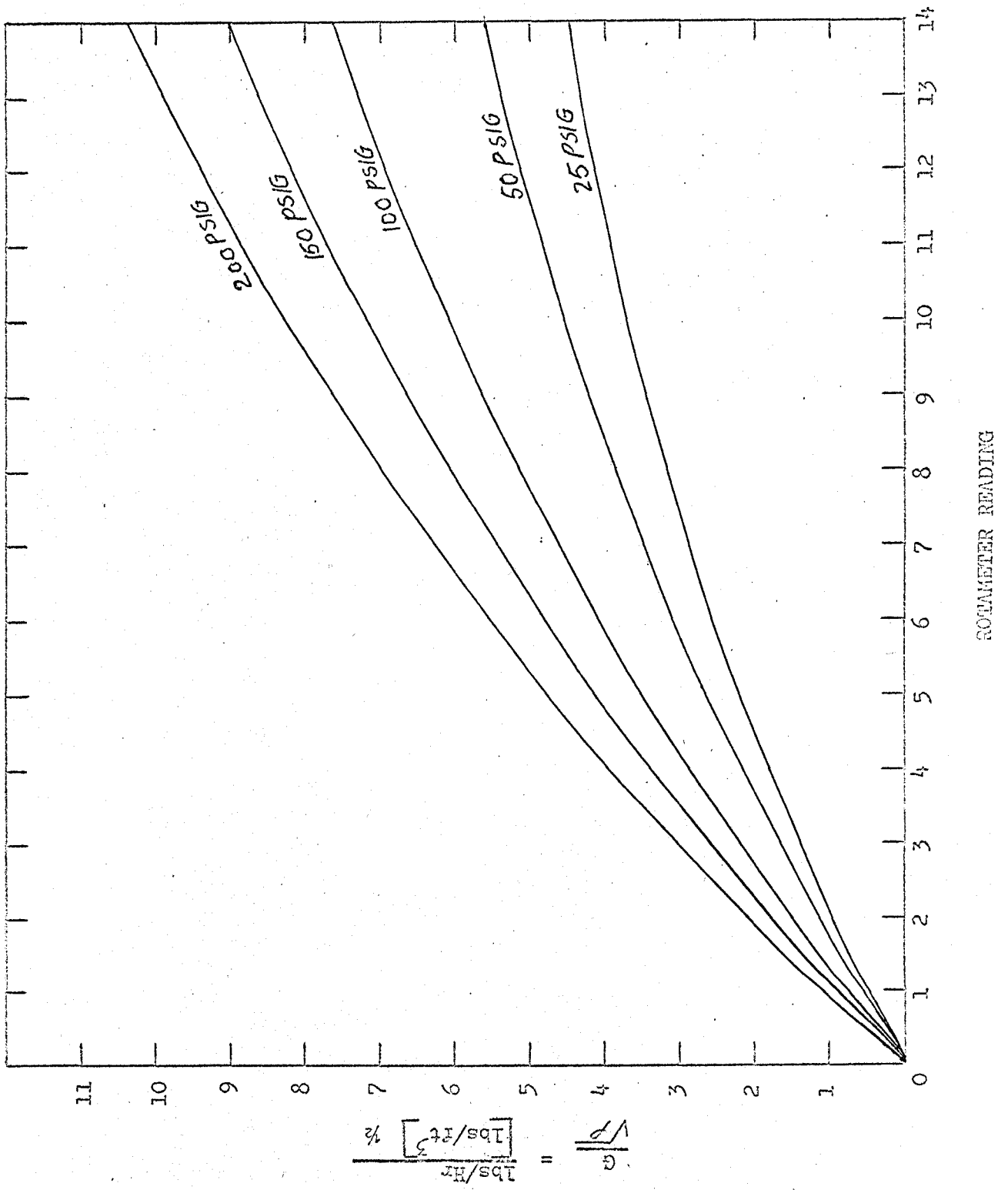
Fig. 15 CALIBRATION CURVES FOR OXYGEN ROTAMETER

$$\frac{G}{\sqrt{\rho}} = \frac{lbs/Hr}{\left[lbs/ft^3\right]^{\frac{1}{2}}}$$
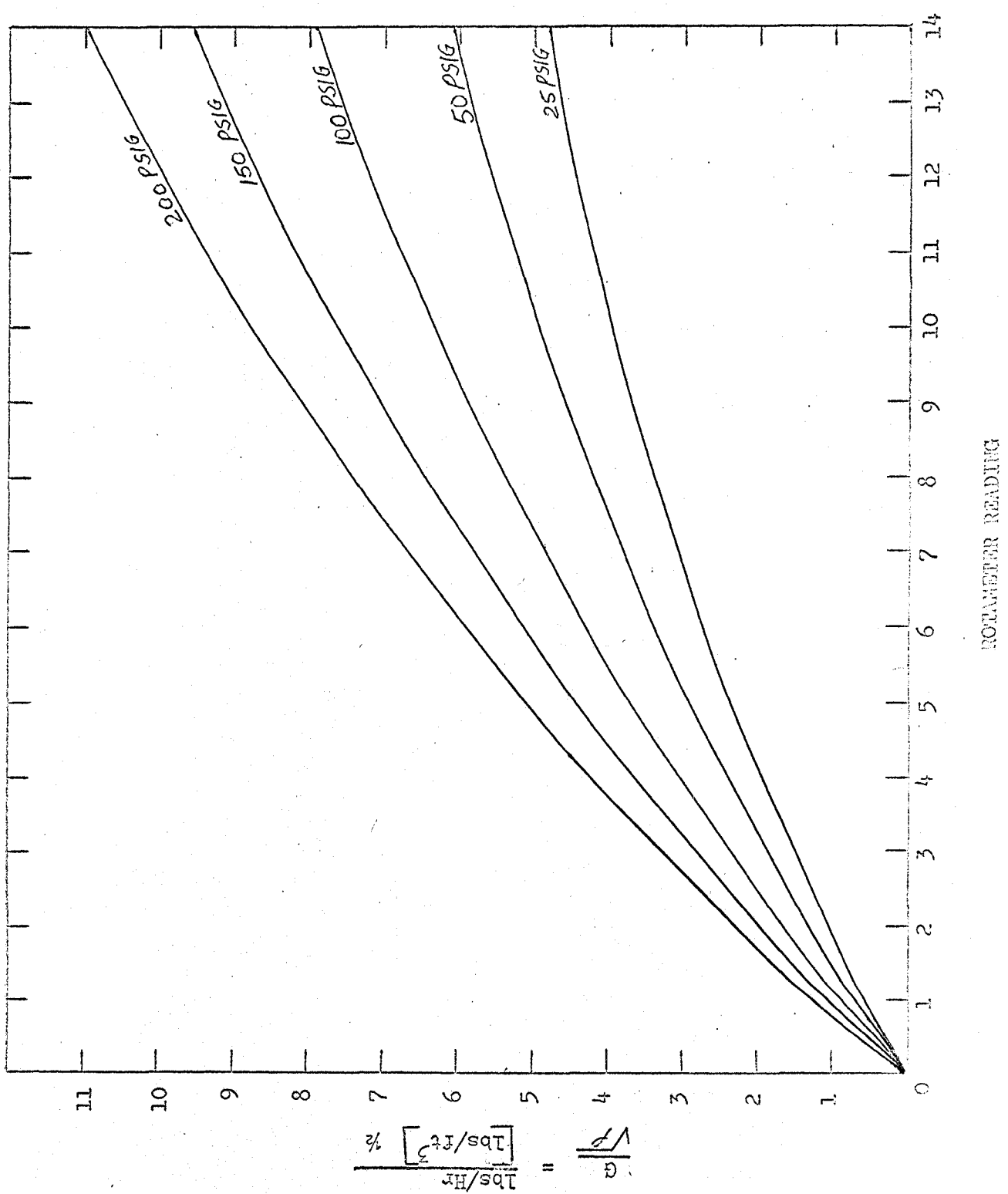
Fig. 16 CALIBRATION CURVES FOR METHANE ROTAMETER
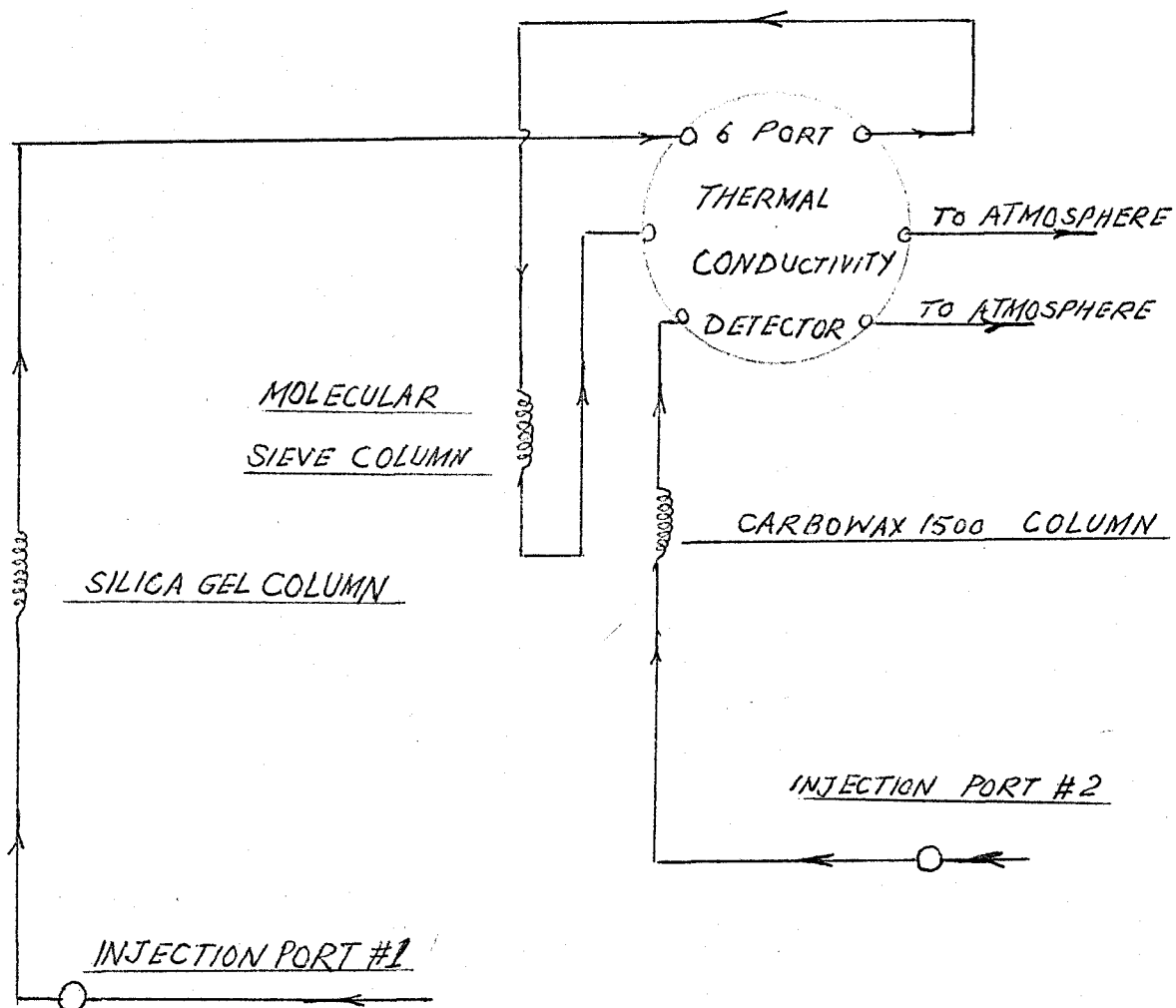
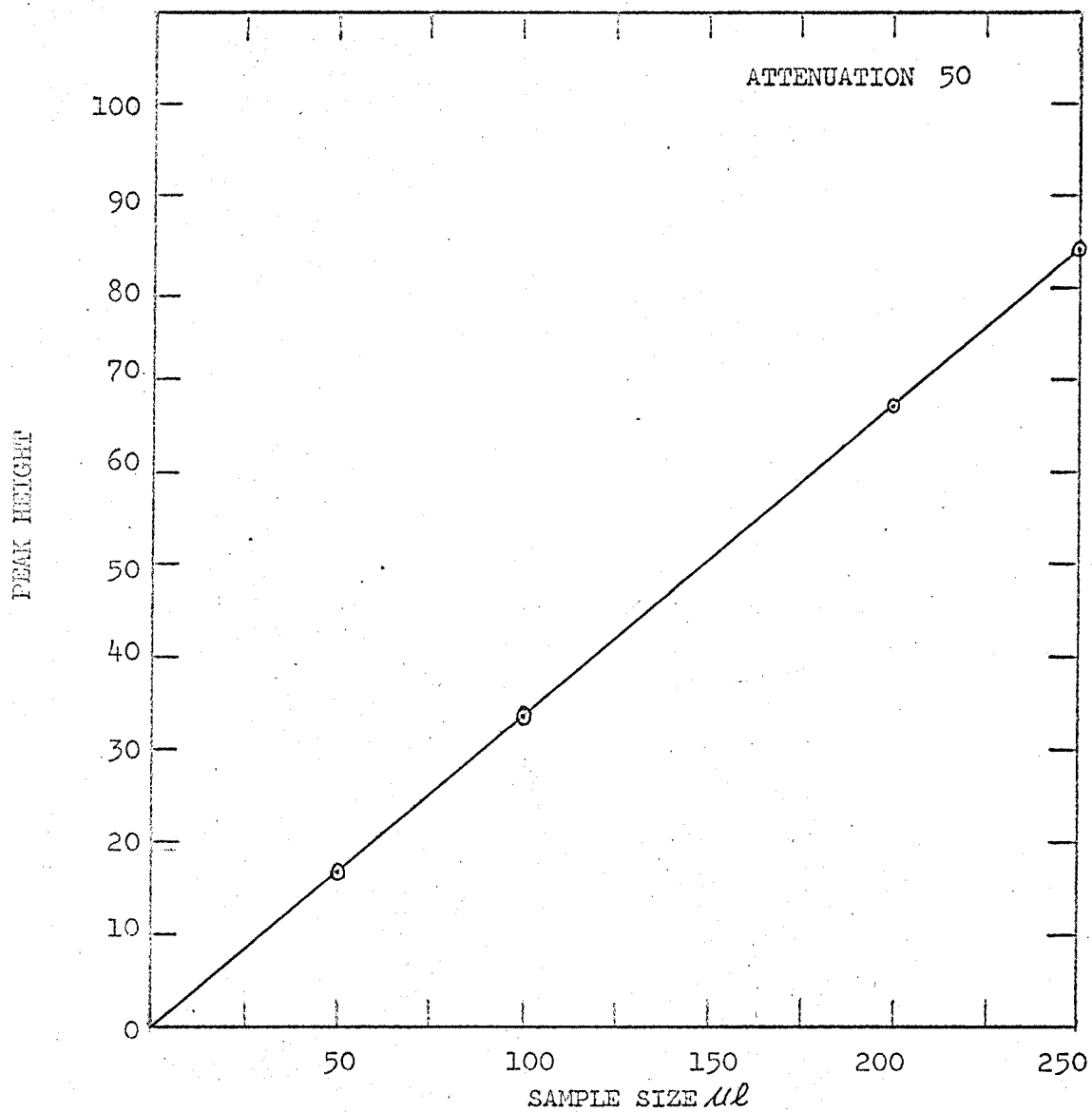FIG. 17 ARRANGEMENT OF COLUMNS FOR 6-PORT DETECTOR

Fig. 18   CHROMATOGRAPHIC CALIBRATION FOR CARBON DIOXIDE
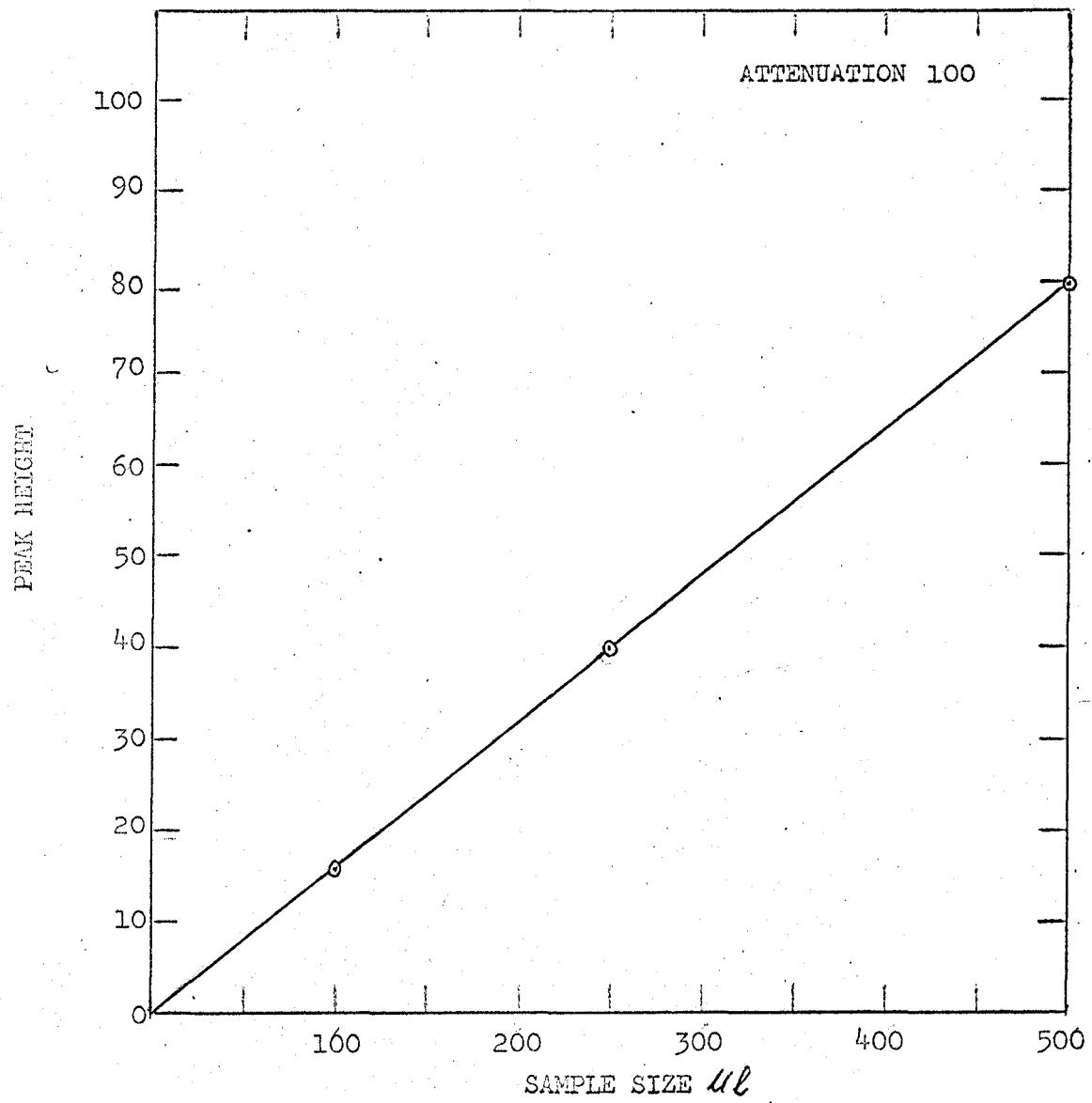
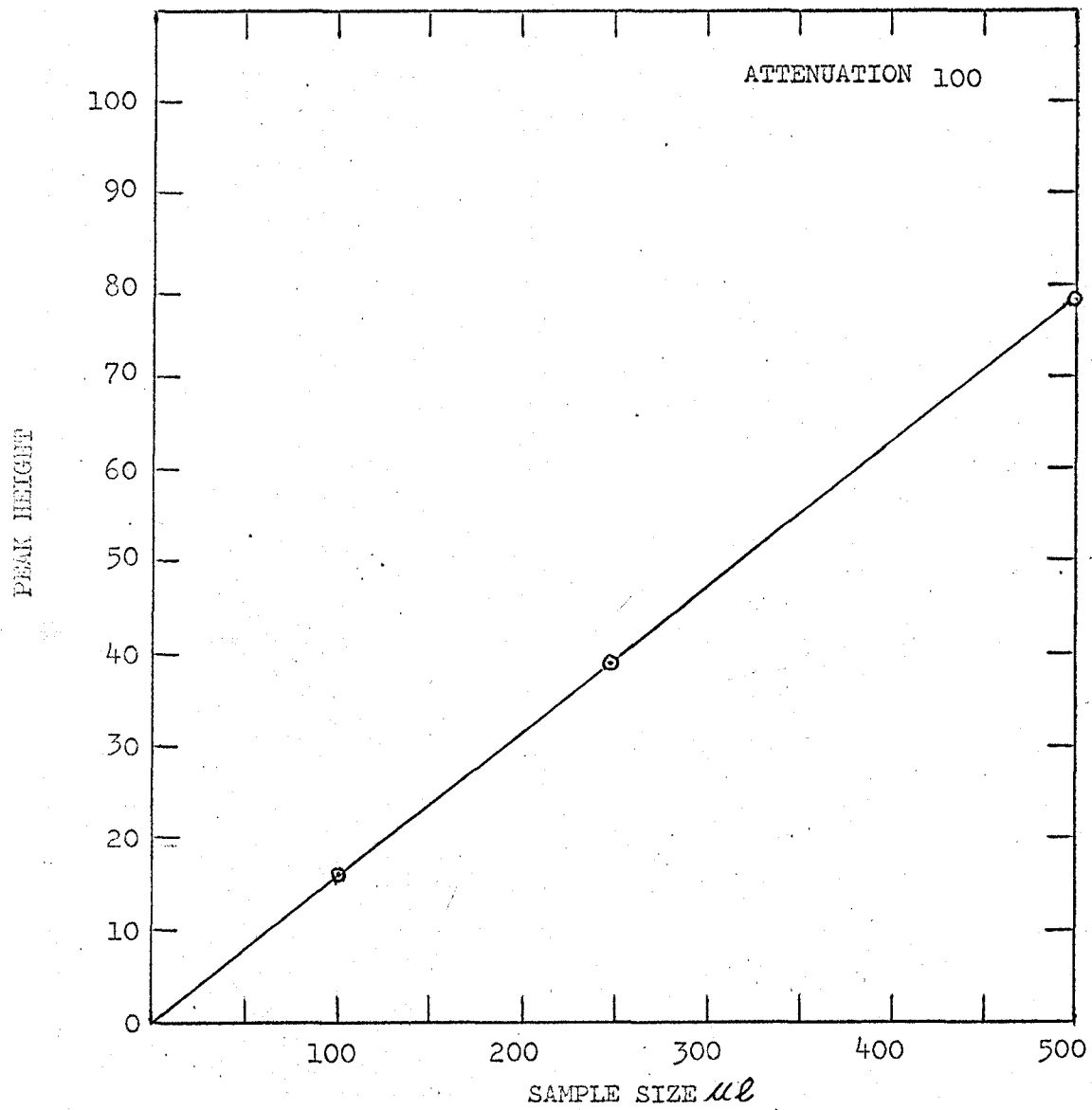Fig. 19 CHROMATOGRAPHIC CALIBRATION FOR OXYGEN

Fig. 20 CHROMATOGRAPHIC CALIBRATION FOR NITROGEN
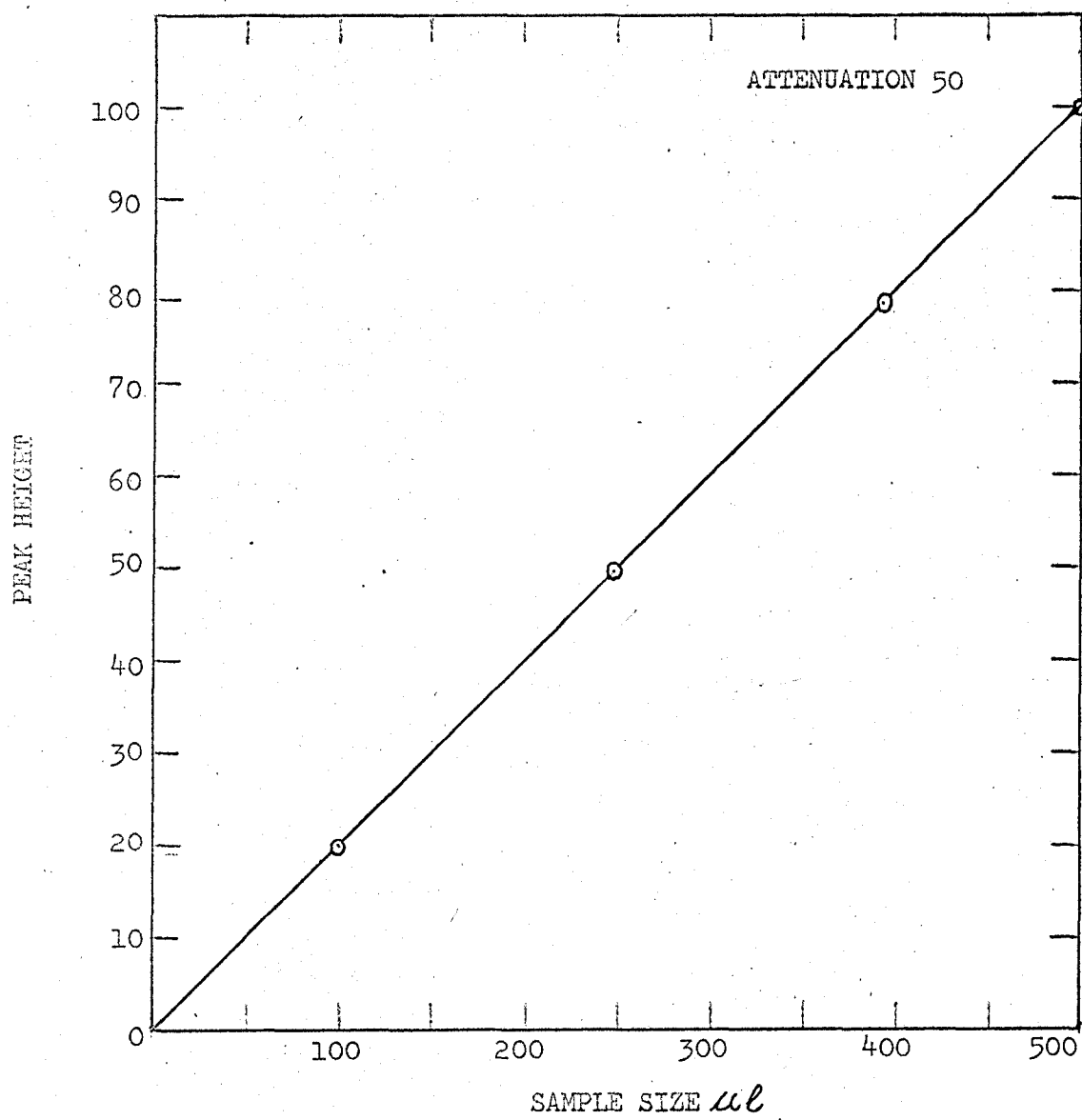
Fig. 21 CHROMATOGRAPHIC CALIBRATION FOR METHANE
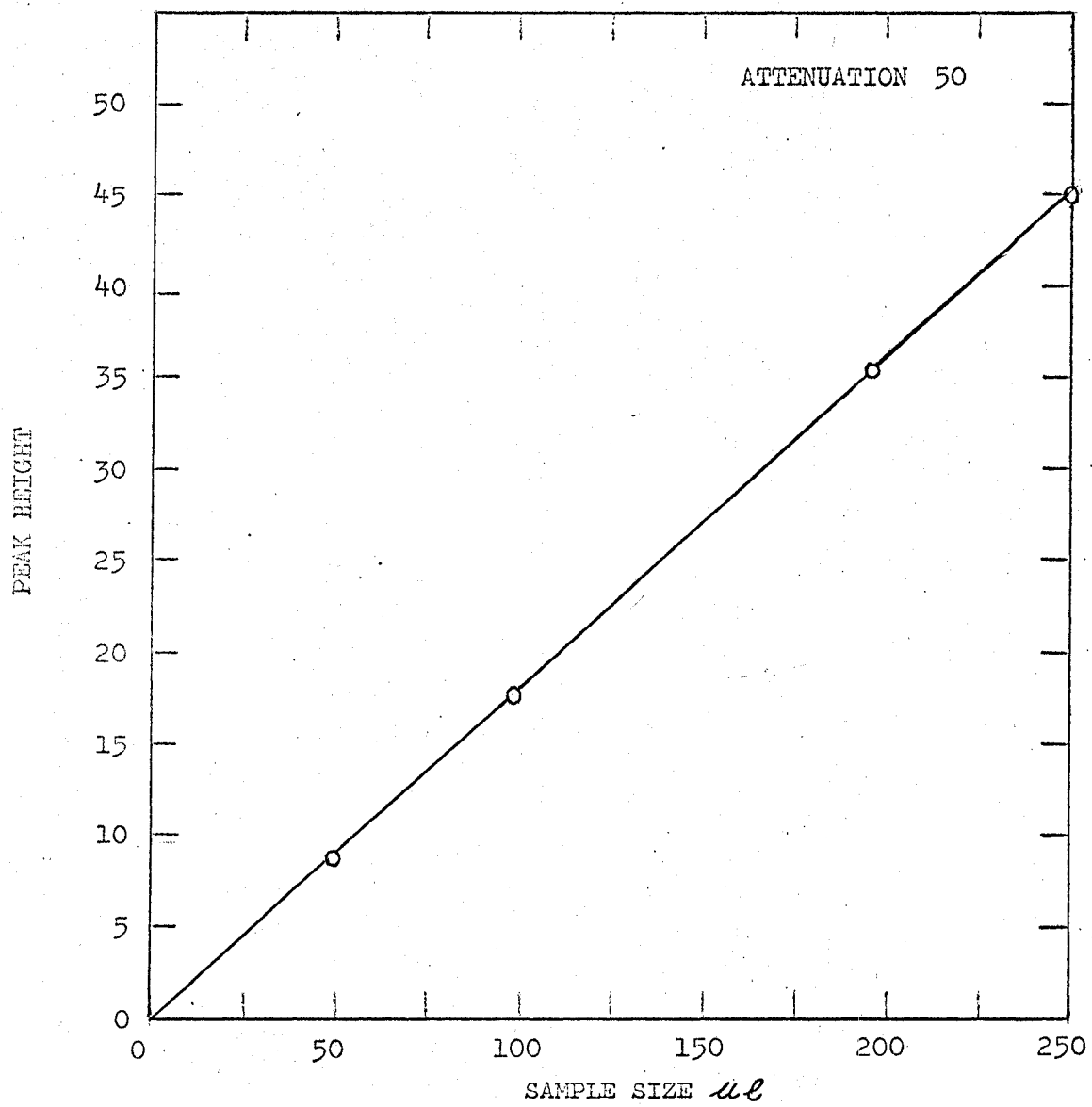
Fig. 22 CHROMATOGRAPHIC CALIBRATION FOR CARBON MONOXIDE

APPENDIX III

Sample Calculation of Initial Rate
from Experimental Data

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APPENDIX III

The sample calculation is illustrated for run I-1, at
1.817 Atm. and 300°C

OXYGEN ROTAMETER

$$\text{Rotameter reading} = 9.0$$
$$\text{Upstream pressure} = 40 \text{ psig}$$
$$\text{Temperature} = 25°C$$

$$\frac{G}{\sqrt{P}} \text{ from calibration chart (fig.15)} = 3.80$$

$$G = 3.80 \times 0.552 \qquad \text{lbs/hr.}$$

$$= \frac{3.80 \times 0.552}{32} = 0.0664 \text{ lb moles/hr.}$$

weight of catalyst used = 0.498 gm.

$$W = 0.498/453.6 = 1.10 \times 10^{-3} \text{ lb.}$$

Product Analysis

Carbon Dioxide peak height = 24.2   (Attenuation 2)

Oxygen peak height = 76.1   (Attenuation 100)

Nitrogen peak height = 0.8   (Attenuation 100)

Methane peak height = 31.4   (Attenuation 10)

Volumes of indiviual gases in products

$$\text{Carbon dioxide} = 24.2 \times \frac{250}{84 \times 25} = 2.985 \ \mu l$$

$$\text{Oxygen} = 76.1 \times \frac{500}{81} = 470 \ \mu l$$

$$\text{Nitrogen} = 0.8 \times \frac{500}{78} = 5.08 \ \mu l$$

$$\text{Methane} = 31.4 \times \frac{500}{100 \times 5} = 31.4 \ \mu l$$

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Water vapour $= 2 \times 2.985 = 5.970$ $\mu\ell$

$$\overline{\text{Total } 515.435 \ \mu\ell}$$

Composition of Gases in product:

Carbon Dioxide $= \dfrac{2.985}{515.435} \times 100 = 0.579\%$

Methane $= \dfrac{31.4}{515.435} \times 100 = 6.09\%$

Conversion $= \dfrac{0.579}{(0.579 + 6.09)} \times 100 = 8.66\%$

As methane Rotameter was at very low rotameter reading, its feed rate was not calculated on rotameter reading basis, but on percentage of methane in feed gas

Methane in feed gas $= 6.669\%$ ←

Methane gas feed rate

$$= 0.0664 \times \frac{6.669}{93.331} = 0.474 \times 10^{-2} \ \text{lb-moles/hr.}$$

Rate of reaction is given by:

$$r_0 = \frac{(\text{Feed rate of methane}) \ (\% \ \text{conversion})}{(\text{Weight of catalyst}) \times 100}$$

$$= \frac{0.474 \times 10^{-2} \times 8.66}{1.1 \times 10^{-3} \times 100}$$

$$= 0.373 \ \frac{(\text{lb moles methane})}{(\text{hr.})(\text{lb. of catalyst})}$$

APPENDIX IV

Sample Calculation for Heat and Mass Transfer Effects

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Yang and Hougen[22] have detailed the equations for calculating heat and mass transfer effects.

The pressure drop ΔP for any component A from the main gas stream to the gas-solid interface is given by the expression

$$\frac{\Delta P_A}{P_A} = \frac{1}{\alpha}\left(\frac{\sqrt{a_p}\ r_A\ M_m\ P_f}{P_A\ \mu\ a_m}\right)\left(\frac{\mu}{D_{Am}}\right)_E\left(\frac{\sqrt{a_p}\ G}{\mu}\right)^{n-1}$$

The equation proposed for the temperature differential across the stagnant gas film from the catalyst surface to the main gas stream is:

$$\frac{\Delta T}{T} = \frac{1}{\alpha'}\left[\frac{r_A\ \Delta H_A\ \sqrt{a_p}}{a_m\cdot\mu\cdot C_p T}\right]\left[\frac{C_p\ \mu}{k}\right]_F^{2/3}\left[\frac{\sqrt{a_p}\ G}{\mu}\right]^{n-1}$$

Values of constants α, α' and n depend on Reynolds number

The result of run I-1, will be used to illustrate the method of estimating various quantities that appear in above expressions. For this run, the overall mass balance is shown below:

lb-moles/hr   lb-moles/hr

CH_4 0.00474 →   0.00433 → CH_4

REACTOR   0.00041 → CO_2

                      0.00082 → C_2O

O_2 0.06640 →   0.06558 → O_2

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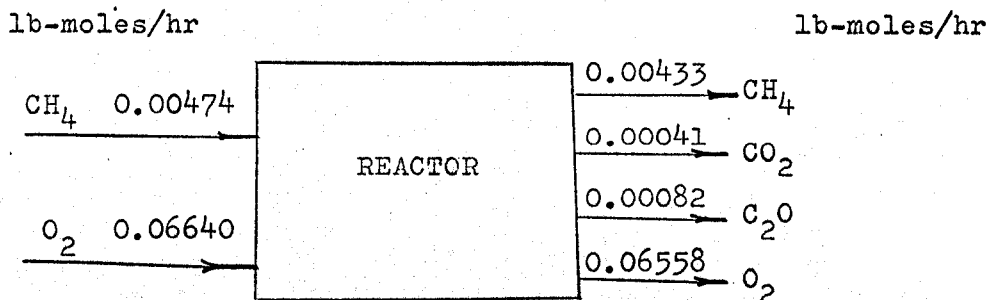
Partial Pressures

Inlet

$$p_{CH_4} = \frac{0.00474}{0.0714} \times 1.817 = 0.1210 \text{ atm.}$$

$$p_{O_2} = \frac{0.0664}{0.07114} \times 1.817 = 1.6960 \text{ atm.}$$

Outlet

$$p_{CO_2} = \frac{0.00041}{0.07114} \times 1.817 = 0.01045 \text{ atm.}$$

$$p_{H_2O} = \frac{0.00082}{0.07114} \times 1.817 = 0.0209 \text{ atm.}$$

$$p_{CH_4} = \frac{0.00433}{0.07114} \times 1.817 = 0.1105 \text{ atm.}$$

$$p_{O_2} = \frac{0.06558}{0.07114} \times 1.817 = 1.6755 \text{ atm.}$$

Average

$$p_{CH_4} = 0.1157 \text{ atm.}$$

$$p_{O_2} = 1.6857 \text{ atm.}$$

$$p_{CO_2} = 0.00523 \text{ atm.}$$

$$p_{H_2O} = 0.01045 \text{ atm.}$$

Physical Properties

Critical Temperature

$$T_{cm} = \sum_i X_i \ T_{Ci}$$

$$T_{cm} = (0.0638)(190.7)+(0.9275)(154.4)+(0.00279)(304.2)+ (0.00579)(647.4)$$

$$= 159.97^\circ \text{ K}$$

Molecular Weight

$$Mm = \sum_i X_i \ M_i$$

Mm $(0.0638)(16)+(0.9275)(32)+(0.00279)(44)+(0.00579)(18)$

$$= 30.7235$$

Viscosity

$$\mu_{cm} = \sum_i X_i \ \mu_{ci}$$

$$\mu_m = \mu_{cm} \ \mu_{rm}$$

cm $(0.0638)(159)+(0.9275)(250)+(0.00279)(343)+(0.00579)(495)$

$$= 245.84 \quad micropoise$$

The value of μ_{rm} can be read from figure 175, page 871, Reference (21)

$$Tr = 573/159.97 \quad 3.58$$
$$Pr \cong 0$$
$$\mu_{rm} = 1.2$$
$$\mu_m = (1.2)(245.84) = 295.01 \ micropoise$$
$$= 0.0956 \ lbs/(hr.)(ft.)$$

Density

$$\rho_m = \frac{30.7235 \times 1.817}{0.7302 \quad \times 1032}$$

$$= 0.0741 \ lbs/ft^3$$

Diffusivity

$$(1 - X_A) \ D_{Am} = X_B \ D_{AB} + X_C \ D_{AC} + \text{------------} \ X_i \ D_{Ai}$$

$$D_{AB} = \frac{0.0043 \ T^{3/2}}{\pi \left(V_A^{1/3} + V_B^{1/3} \right)} \sqrt{\frac{1}{M_A} + \frac{1}{M_B}}$$

$$D_{CH_4 - O_2} = \frac{(0.0043)(573)^{3/2}}{1.817\,(29.6^{1/3} + 25.6^{1/3})}\sqrt{\frac{1}{16} + \frac{1}{32}}$$

$$\doteq 0.48 \ cm^2/\ sec.$$

$$\doteq 1.856 \ ft^2/hr.$$

$$D_{CH_4 - CO_2} = \frac{(0.0043)(573)^{3/2}}{1.817\,(29.6^{1/3} + 34^{1/3})}\sqrt{\frac{1}{16} + \frac{1}{44}}$$

$$= 0.417 \ cm^2/sec.$$

$$= 1.615 \ ft^2/hr.$$

$$D_{CH_4 - H_2O} = \frac{(0.0043)(573)^{3/2}}{1.817(29.6^{1/3} + 18.9^{1/3})}\sqrt{\frac{1}{16} + \frac{1}{16}}$$

$$= 0.598 \ cm^2/sec.$$

$$= 2.315 \ ft^2/hr.$$

$$(1 - 0.0638)\ D_{CH_4 - m} = (1.856)(0.9275) + (1.615)(0.00279) + (2.315)(0.00579)$$

$$D_{CH_4 - m} = 1.85 \ ft^2/hr.$$

Pressure Film Factor
===

$$P_f = (\pi + \delta_A \ P_A)_m$$

$$= \pi + 0 = 1.817 \ atm.$$

Modified Reynolds Number
===

$$N'_{re} = \frac{\sqrt{ap.}\ G}{\mu}$$

$$G = F/A = \frac{0.00453 \times 16}{\left(\frac{\pi}{4}\right) \times \left(\frac{1.5}{12}\right)^2} = 5.91 \ lbs/(hr.)(ft^2)$$

$$D_p = (1.5)^{\frac{1}{2}} D = (1.5)^{\frac{1}{2}} (8\frac{1}{x\ 12}) = 0.0127 \text{ ft.}$$

$$a_p = \pi D^2_p = 0.000507 \text{ ft}^2$$

Modified Reynolds Number

$$N'_{Re} = \frac{(a_p)^{\frac{1}{2}} G}{\mu} = \frac{(0.000507)^{\frac{1}{2}} (5.91)}{0.0956}$$

$$= 1.391$$

Schmidt Number

$$S_c = \frac{\mu}{P\ D_{Am}} = \frac{0.0956}{(7.41 \times 10^{-2})(1.85)} = 0.698$$

$$A_m = 120 \text{ (metre)}^2/\text{gm} \qquad \text{(Suppliers Data)}$$

$$= \frac{120 \times (3.28)^2}{1/453.6} = 5.8 \times 10^5 \text{ (ft)}^2/\text{ lb.}$$

Pressure Drop

The pressure drop for methane from the main gas stream to the gas-solid interface is given as

$$\frac{\Delta P_A}{P_A} = \frac{1}{\measuredangle} \left[\frac{\sqrt{a_p}\ r_A\ M_m\ P_f}{P_A\ \mu\ a_m} \right] \left[\frac{\mu}{P\ D_{Am}} \right]_f \left[\frac{\sqrt{a_p} G}{\mu} \right]^{n-1}$$

for $N'_{re} < 620$, $\measuredangle = 2.44$ and $n = 0.51$

$$\therefore \frac{\Delta p}{p} = \frac{1}{2.44} \left[\frac{(0.000507)^{\frac{1}{2}}(0.373)(30.7235)(1.817)}{(0.1157)(0.0956)(5.8 \times 10^5)} \right] (0.698)^{2/3}(1.391)^{-0.5}$$

$$\frac{\Delta p}{p} = 2.01 \times 10^{-3}$$

$$\Delta P = 2.01 \times 10^{-3} \times 0.1157 = 2.33 \times 10^{-4} \text{ atm.}$$

Specific Heat

$$C_{pm} = \sum_i X_i C_{p_i}$$

$$= (0.0638)(12.32)+(0.9275)(7.68)+(0.00279)(11.2)+$$
$$(0.00579)(3.96)$$

$$= 7.957 \quad \text{Btu/(lb-mole)}(R^\circ)$$

$$= 7.957 \quad \text{Cal/(gm-mole)}(K^\circ)$$

Prandtl Number

$$Pr = \frac{C_p \mu}{k}$$

A relation recommended by Hougen and Watson [21], is given on page 990, equation (51).

$$\frac{C_p \mu}{k} = \frac{4}{\left[9 - 5 \frac{Cv}{Cp}\right]}$$

$$\left[\frac{Cp \mu}{k}\right]^{2/3} = \left[\frac{4}{9 - \left(5 \times \frac{1}{13.1}\right)}\right]^{2/3} = 0.844$$

Heat of Reaction

$$\Delta Hr = -191 \quad \text{K. Cal/g-mole at } 500^\circ K$$

Temperature Drop

The temperature differential ΔT across the stagnant gas film from the catalyst surface to the main gas stream is

$$\frac{\Delta T}{T} = \frac{1}{\alpha'} \left[\frac{r_A \, \Delta H_A}{a_m} \, \frac{(a_p)^{1/2}}{C_p T} \right] \left[\frac{C_p \mu}{k} \right]_f^{2/3} \left[\frac{(a_p)^{1/2} \, G}{\mu} \right]^{n-1}$$

For $N'_{re} < 620$ $\qquad \alpha' = 2.62 \qquad n = 0.51$

$$\therefore \quad \frac{\Delta T}{T} = \frac{1}{2.62} \left[\frac{0.373 \times 1.91 \times 10^5 \times 2.255 \times 10^{-2}}{5.8 \times 10^5 \times 0.0956 \times \left(\frac{7.957}{30.7235}\right) \times 573} \right] (0.844)(1.391)^{1-0.51}$$

$$= 1.345 \times 10^{-4}$$

$$\Delta T = 1.345 \times 10^{-4} \times 573 = 0.077\,°C$$

It is evident, that mass transfer and heat transfer effects are quite negligible. For other runs, the mass and heat transfer contributions were found to be of the same order of magnitude as this particular run.

APPENDIX V

Computer Programmes and Results

92

```
C   C   O. P. AHUJA
C       REGRESSION  COEFFICIENTS  FOR  THE  MECHANISM  EQUATIONS  NO. 1
        DIMENSION X(10),      SIGY(10),SIGYY(10),XY(10),A(10),B(10),P(10
       1R(10),Y(10,10)
    1 READ 2, (P(K),K=1,8),(R(K),K=1,8)
        C = 8
        F = 1./3.
        DO 3 K = 1,8
        X(K) = P(K)
        Y(1,K) = P(K)/SQRTF(R(K))
        Y(2,K) =  P(K)/R(K)**F
        Y(3,K) = (P(K)**1.5)/SQRTF(R(K))
        Y(4,K) = (P(K)**3.)/R(K)
        Y(5,K) = P(K)/R(K)
        Y(6,K) = (SQRTF(P(K)))/R(K)**.25
        Y(7,K) = (P(K)**.75)/R(K)**.25
    3 Y(8,K) = P(K)/R(K)
        SIGX = 0
        SIGXX = 0
        DO 4 J = 1,8
        SIGY(J) = 0
    4 XY(J) = 0
        DO 5 J = 1,8
        DO 5 K = 1,8
        SIGY(J) = SIGY(J) + Y(J,K)
    5 XY(J) = XY(J) + X(K) * Y(J,K)
        DO 6 K = 1,8
        SIGX = SIGX + X(K)
    6 SIGXX = SIGXX + X(K)*X(K)
        DO 7 J = 1,8
        A(J) = (SIGXX*SIGY(J)-SIGX*XY(J))/(C*SIGXX-SIGX*SIGX)
    7 B(J) = (C*XY(J)-SIGX*SIGY(J))/(C*SIGXX-SIGX*SIGX)
        PUNCH 10
        DO 9 J = 1,8
    9 PUNCH 8,J,A(J),B(J)
    2 FORMAT(8F8.3/(8F8.3))
   10 FORMAT(5X,1HN,15X,1HA,20X,1HB//)
    8 FORMAT(5X,I1, 2(10X,F12.6))
        GO TO 1
        END
```

1817	2975	3925	5220	6240	7130	8410	97
373	481	503	559	594	624	655	671
1817	2975	3925	5220	6240	7130	8410	97
398	511	531	581	616	658	694	712
1817	2975	3925	5220	6240	7130	8410	97
421	552	580	640	673	720	745	771

O. P. AHUJA

REGRESSION COEFFICIENTS FOR THE MECHANISM EQUATIONS NO. 1

TEMPRATURE 300 DEGREES C

N	A	B
1	1.034149	1.119909
2	.622627	1.082035
3	-4.980518	4.172677
4	-471.924620	164.676080
5	2.818439	1.208295
6	1.448114	.214024
7	1.218984	.511810
8	2.818439	1.208295

TEMPRATURE 320 DEGREES C

N	A	B
1	1.018676	1.088979
2	.619577	1.061949
3	-4.797862	4.055110
4	-443.534080	155.399770
5	2.692498	1.143425
6	1.429209	.211230
7	1.205102	.504798
8	2.692498	1.143425

TEMPRATURE 340 DEGREES C

N	A	B
1	.973950	1.045676
2	.599482	1.033754
3	-4.642242	3.898043
4	-411.557960	143.724510
5	2.484799	1.052355
6	1.402137	.206615
7	1.180958	.494457
8	2.484799	1.052355

```
C        O. P. AHUJA
C        REGRESSION COEFFICIENTS FOR MECHANISM EQUATION NO. 9
         DIMENSIONX(15),Y(15),Z(15),P(15),R(15)
6 READ 5, (P(K),K=1,8),(R(K),K=1,8)
  DO 1 J=1,8
  X(J) = P(J)
  Y(J) = SQRTF(P(J))
1 Z(J) = (P(J)**0.6)/(R(J)**.2)
  SIGX = 0
  SIGY = 0
  SIGZ = 0
  SIGXX = 0
  SIGYY = 0
  SIGXY = 0
  SIGYZ = 0
  SIGZX = 0
  DO 2 J = 1,8
  SIGX = SIGX + X(J)
  SIGY = SIGY + Y(J)
  SIGZ = SIGZ + Z(J)
  SIGXX = SIGXX + X(J)*X(J)
  SIGYY = SIGYY + Y(J)*Y(J)
  SIGXY = SIGXY + X(J)*Y(J)
  SIGYZ = SIGYZ + Y(J)*Z(J)
2 SIGZX = SIGZX + Z(J)*X(J)
  PUNCH 3,SIGZ,SIGX,SIGY
  PUNCH 4,SIGZX,SIGX,SIGXX,SIGXY
  PUNCH 4,SIGYZ,SIGY,SIGXY,SIGYY
3 FORMAT(F9.4,2H =,6H   8 B0,3H + ,2HB1,F9.4,2H +,3H B2,F9.4//)
4 FORMAT(F9.4,5H      =,3H B0,F9.4,2H +,3H B1,F9.4,3H + ,2HB2,F9.4//)
5 FORMAT(8F8.3/(8F8.3))
  GO TO 6
  END
1817      2975      3925      5220      6240      7130      8410      97
 373       481       503       559       594       624       655      671
1817      2975      3925      5220      6240      7130      8410      97
 398       511       531       581       616       658       694      712
1817      2975      3925      5220      6240      7130      8410      97
 421       552       580       640       673       720       745      771
```

O. P. AHUJA

REGRESSION COEFFICIENTS FOR MECHANISM EQUATION NO. 9

TEMPRATURE = 300 DEGREES C

$24.6427 = 8 \ B0 + B1 \ 45.4170 + B2 \ 18.5213$

$155.9711 = B0 \ 45.4170 + B1 \ 309.3987 + B2 \ 116.5084$

$60.6336 = B0 \ 18.5213 + B1 \ 116.5084 + B2 \ 45.4169$

TEMPRATURE = 320 DEGREES C

$24.3854 = 8 \ B0 + B1 \ 45.4170 + B2 \ 18.5213$

$154.3376 = B0 \ 45.4170 + B1 \ 309.3987 + B2 \ 116.5084$

$60.0016 = B0 \ 18.5213 + B1 \ 116.5084 + B2 \ 45.4169$

TEMPRATURE = 340 DEGREES C

$23.9883 = 8 \ B0 + B1 \ 45.4170 + B2 \ 18.5213$

$151.8152 = B0 \ 45.4170 + B1 \ 309.3987 + B2 \ 116.5084$

$59.0200 = B0 \ 18.5213 + B1 \ 116.5084 + B2 \ 45.4169$

```
C       O. P. AHUJA                                                    95
C       COEFFICIENTS  FOR  THE  EMPIRICAL  RATE  EQUATION
        DIMENSION X(15),Y(15),Z(15),A(15),B(15),R(15)
      6 READ 5,(A(J),J=1,10),(B(J),J=1,10),(R(J),J=1,10)
        DO 1 J=1,10
        X(J)  = LOGF(A(J))
        Y(J)  = LOGF(B(J))
      1 Z(J)  = LOGF(R(J))
        SIGX  = 0
        SIGY  = 0
        SIGZ  = 0
        SIGXX = 0
        SIGYY = 0
        SIGXY = 0
        SIGYZ = 0
        SIGZX = 0
        DO 2 J = 1,10
        SIGX  = SIGX + X(J)
        SIGY  = SIGY + Y(J)
        SIGZ  = SIGZ + Z(J)
        SIGXX = SIGXX + X(J)*X(J)
        SIGYY = SIGYY + Y(J)*Y(J)
        SIGXY = SIGXY + X(J)*Y(J)
        SIGYZ = SIGYZ + Y(J)*Z(J)
      2 SIGZX = SIGZX + Z(J)*X(J)
        PUNCH 3,SIGZ,SIGX,SIGY
        PUNCH 4,SIGZX,SIGX,SIGXX,SIGXY
        PUNCH 4,SIGYZ,SIGY,SIGXY,SIGYY
      3 FORMAT(F9.4,2H =,6H 10 B0,3H + ,2HB1,F9.4,2H +,3H B2,F9.4//)
      4 FORMAT(F9.4,5H      =,3H B0,F9.4,2H +,3H B1,F9.4,3H + ,2HB2,F9.4//)
      5 FORMAT(10F6.6/(10F6.4)/(10F6.3))
        GO TO 6
        END
 4740   6280   7125   8160   8800   9610  11171  12310  11793    251
  664    906   1029   1173   1270   1392   1610   1753    664    664
  373    481    503    559    594    624    655    671    796    842
  481    632    724    812    877    958   1123   1225   1177   2497
  664    906   1029   1173   1270   1392   1610   1753    664    664
  398    511    531    581    616    658    694    712    836    884
  484    639     72    819    886    971    112   1232   1175   2531
  664    906   1029   1173   1270   1392   1610   1753    664    664
  421    552    580    640    673    720    745    771    882    932
```

O. P. AHUJA

COEFFICIENTS FOR THE EMPIRICAL RATE EQUATION

TEMPRATURE = 300 DEGREES C

$-5.2015 = 10 \; B0 + B1 \; -46.5696 + B2 \; -22.5575$

$25.1416 \quad = B0 \; -46.5696 + B1 \; 218.7236 + B2 \; 105.0645$

$11.7985 \quad = B0 \; -22.5575 + B1 \; 105.0645 + B2 \quad 52.1096$

TEMPRATURE = 320 DEGREE C

$-4.6791 = 10 \; B0 + B1 \; -46.5508 + B2 \; -22.5575$

$22.6762 \quad = B0 \; -46.5508 + B1 \; 218.5045 + B2 \; 105.0151$

$10.6178 \quad = B0 \; -22.5575 + B1 \; 105.0151 + B2 \quad 52.1096$

TEMPRATURE = 340 DEGREES C

$-3.9252 = 10 \; B0 + B1 \; -46.4920 + B2 \; -22.5575$

$19.1228 \quad = B0 \; -46.4920 + B1 \; 217.9665 + B2 \; 104.8812$

$8.9551 \quad = B0 \; -22.5575 + B1 \; 104.8812 + B2 \quad 52.1096$

1937	Born Om Parkash Ahuja on June 8, 1937, in Bhera, Surgodha. India.
1953	Completed science matriculation at Arya High School, Panipat, India.
1957	Graduated in science, D.S. College, Karnal, India.
1961	Graduated in Chemical Engineering, Indian Institute of Technology, Kharagpur, India.
1961-64	Employed in Design and Development section of DCM Chemical Works, New Delhi, India.
1964	Accepted into the Graduate School of University of Windsor as Candidate for the degree of M. A. Sc. in Chemical Engineering.
1966	Working as project Engineer, Canadian Celanese, Drummondville (Quebec).